

COMP 410 Lecture I

Kyle Dewey

About Me

- I research automated testing techniques and their intersection with CS education
- My dissertation used logic programming extensively
- This is my second time teaching this class

About this Class

- See something wrong? Want something improved? Email me about it!
(kyle.dewey@csun.edu)
- I generally operate based on feedback

Bad Feedback

- This guy sucks.
- This class is boring.
- This material is useless.

-I can't do anything in response to this

Good Feedback

- This guy sucks, *I can't read his writing.*
- This class is boring, *it's way too slow.*
- This material is useless, *I don't see how it relates to anything in reality.*

- I can't fix anything if I don't know what's wrong

-I can actually do something about this!

What is Logic Programming?

- Major programming paradigm – a way of thinking about problems
- Emphasizes thinking about exactly what the problem is, as opposed to exactly how to solve it. This is called declarative programming.
- For example: it's generally easier to say what constraints must hold for a valid Sudoku solution, as opposed to directly finding a valid Sudoku solution.
- Somewhat related to functional programming – we generally lack mutable state
- Unlike any other major paradigm, the distinction between inputs and outputs is intentionally blurred. You can take advantage of this.
- Basis in formal logic. It's the only major paradigm where “=” has the same meaning as it does in math.

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What is this Course?

- Strong emphasis on programming and using logic programming languages
- I want you to think in this paradigm, not merely force Java into it
- The ideas can be applied in non-logical languages, and your first assignment will force you to write in a logical way outside of a logic programming language (though you won't realize that's what you're doing yet)
- Little bit of theory

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- Applying logic programming without a logic programming language

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- Artificial intelligence

- "Artificial intelligence" used to refer to search techniques, which is relevant to logic programming. Now the term largely refers to machine learning. What it means is a moving target.

- Machine learning (we won't do any sort of statistics)

- You can spend a career on the theory behind this stuff. I know some, but it's not my speciality.

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Syllabus

Outline

- Abstract Syntax Trees and evaluation
- SAT and Semantic Tableau

Abstract Syntax Trees and Evaluation

Abstract Syntax Tree

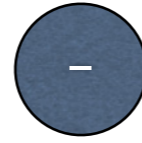
- Abbreviation:AST
- Unambiguous tree-based representation of a sentence in a language
- Very commonly used in compilers, interpreters, and related software

-Generally we work with ASTs instead of Strings or any other code representation

$$(1 + 2) - 3 * 4$$

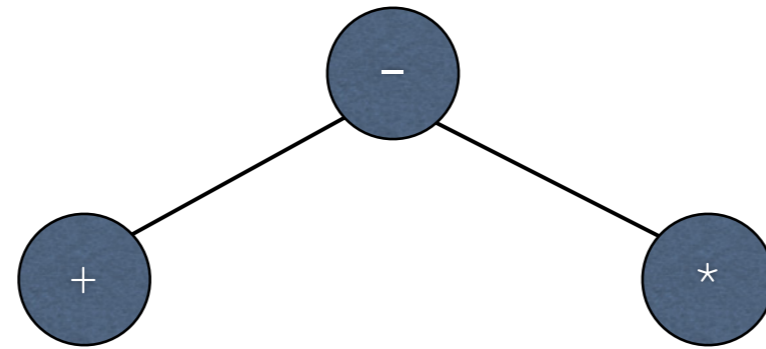
-Key parts: we need parentheses to direct that $1 + 2$ happens first. We know that the $3 * 4$ should happen after the part in parentheses from PEMDAS rules

$(1 + 2) - 3 * 4$



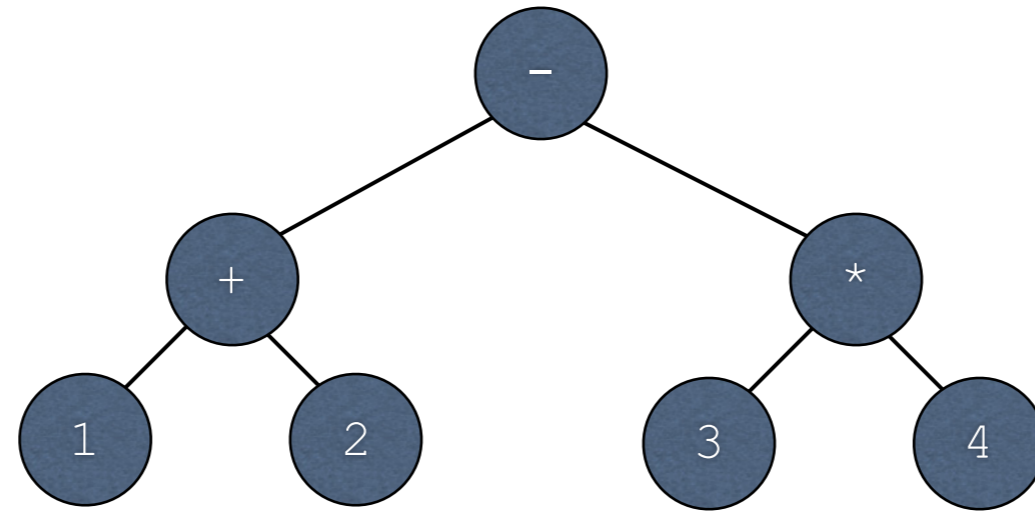
-Lowest priority thing ends up in the top of the tree

(1 + 2) - 3 * 4



-Next level of priority

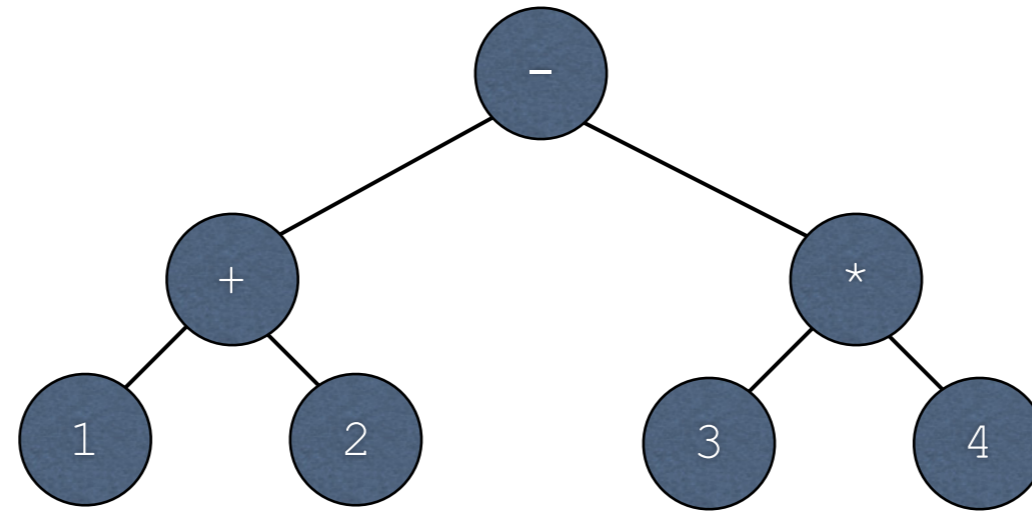
$$(1 + 2) - 3 * 4$$



-Next level of priority

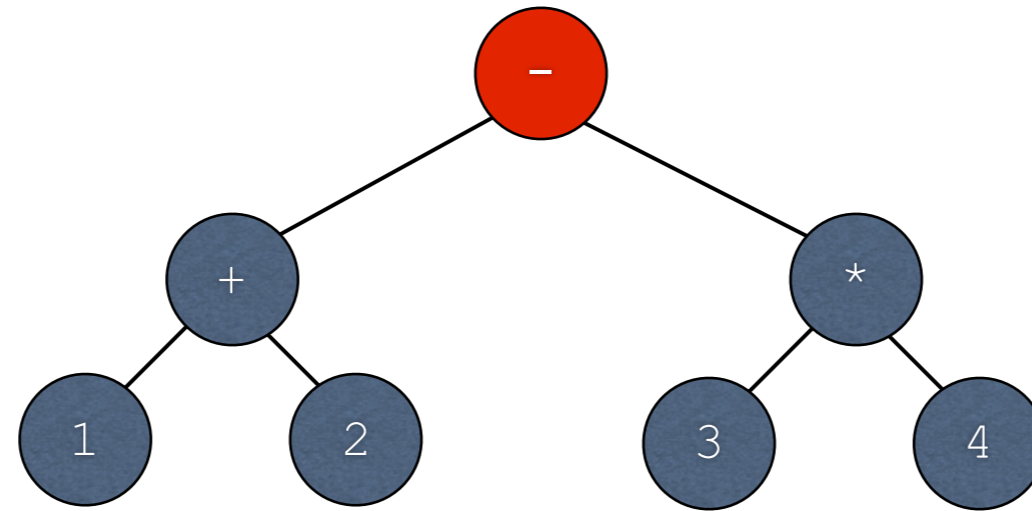
Exercise: First Side of AST/Evaluation Sheet

Evaluation



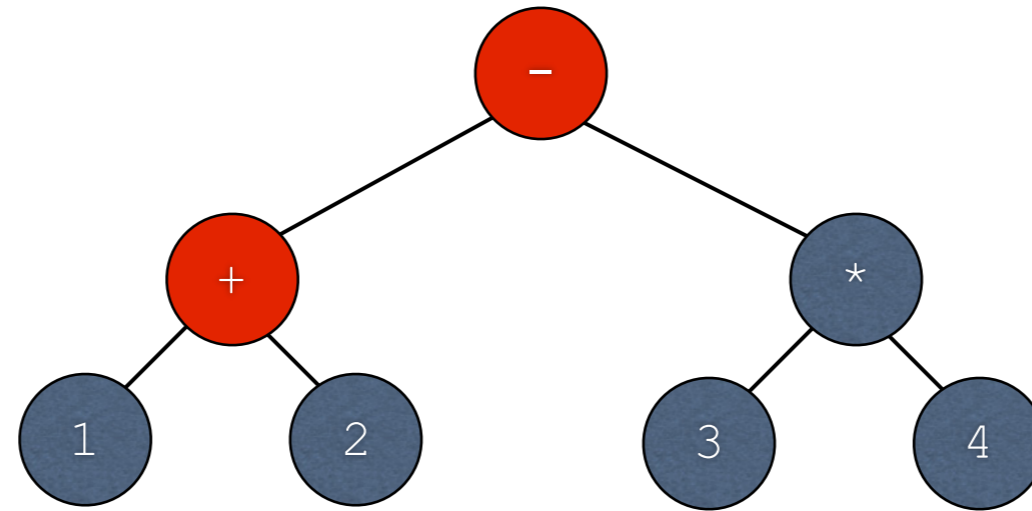
- Key point: bubble-up values from the leaves
- This can be implemented in code via a recursive function starting from the root (code in a bit later)

Evaluation



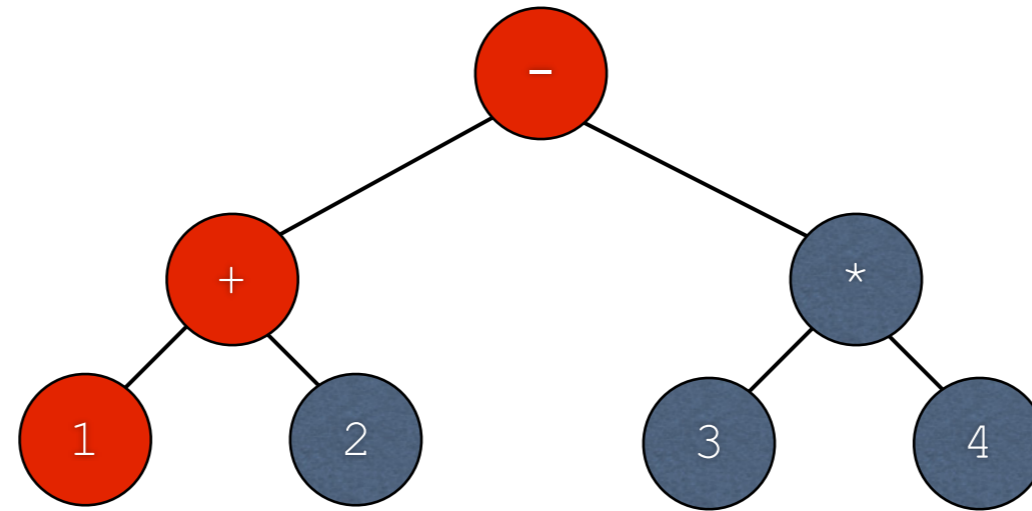
-We start evaluation from the root...

Evaluation



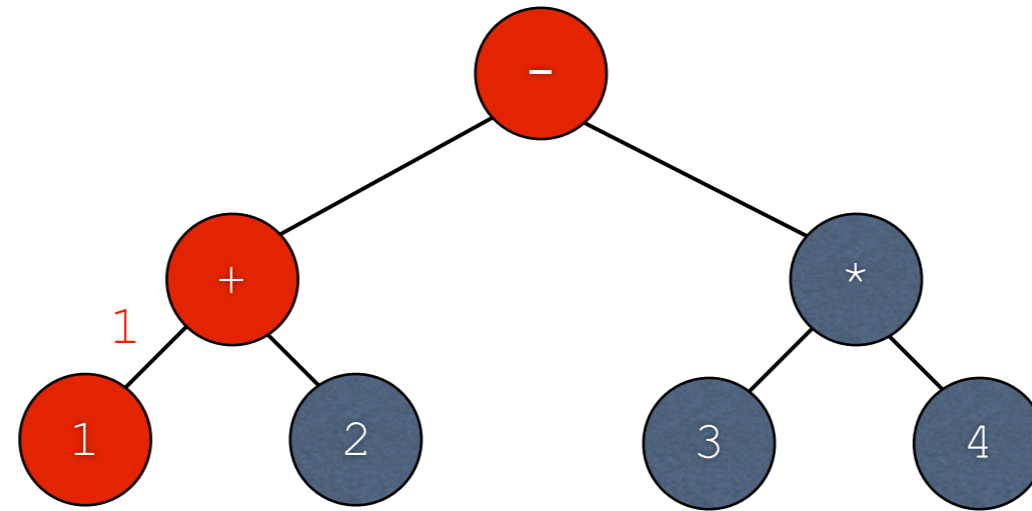
-In order to evaluate the root, we need to evaluate the left subtree of the root (+)

Evaluation



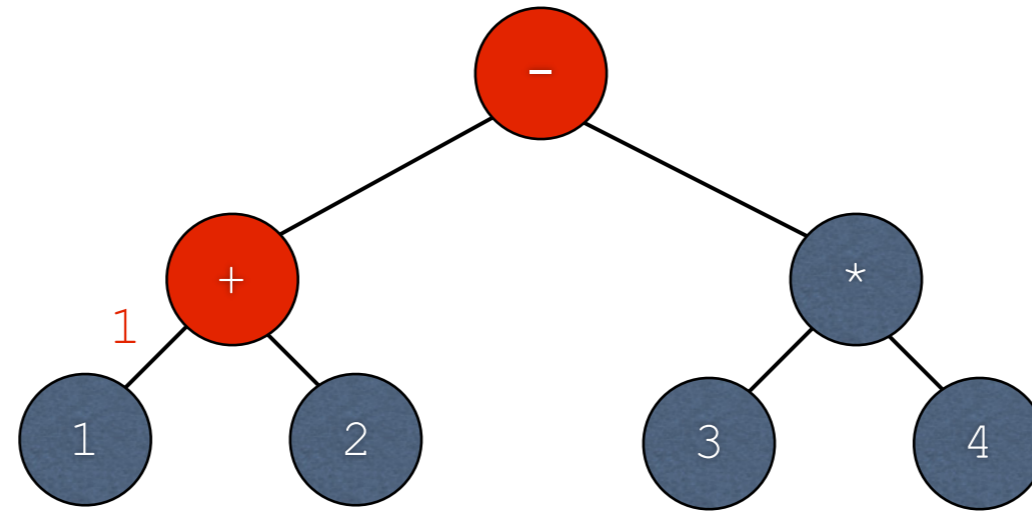
-In order to evaluate +, we need to evaluate the left subtree (as with the root)

Evaluation



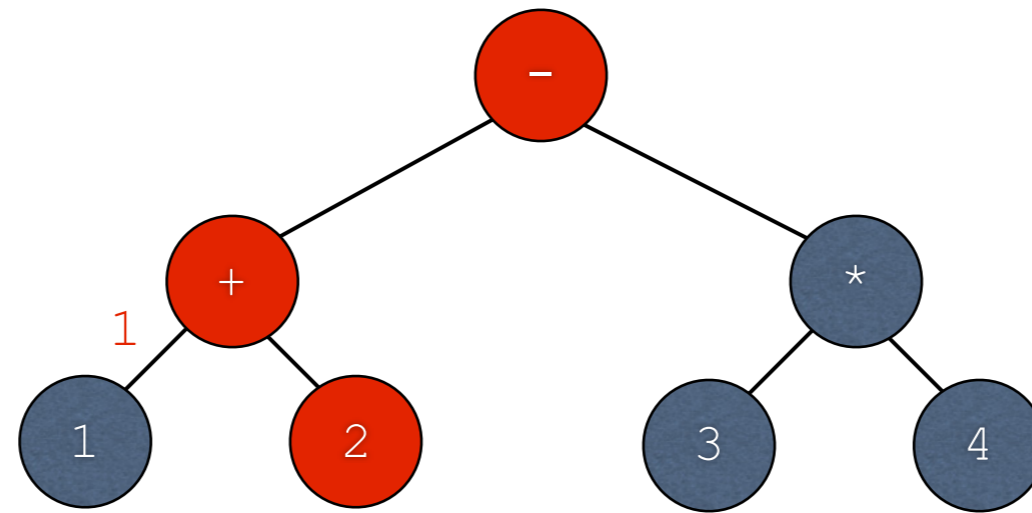
- For arithmetic, leaves are simply numbers
- Evaluating a leaf returns the number held within

Evaluation



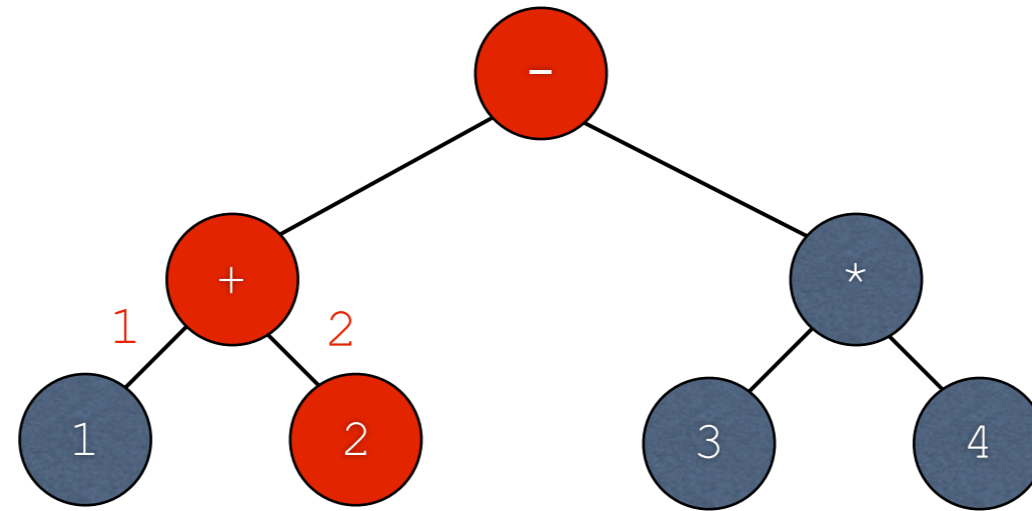
- The left subtree of + has now been evaluated
- Now + needs the value of the right subtree

Evaluation



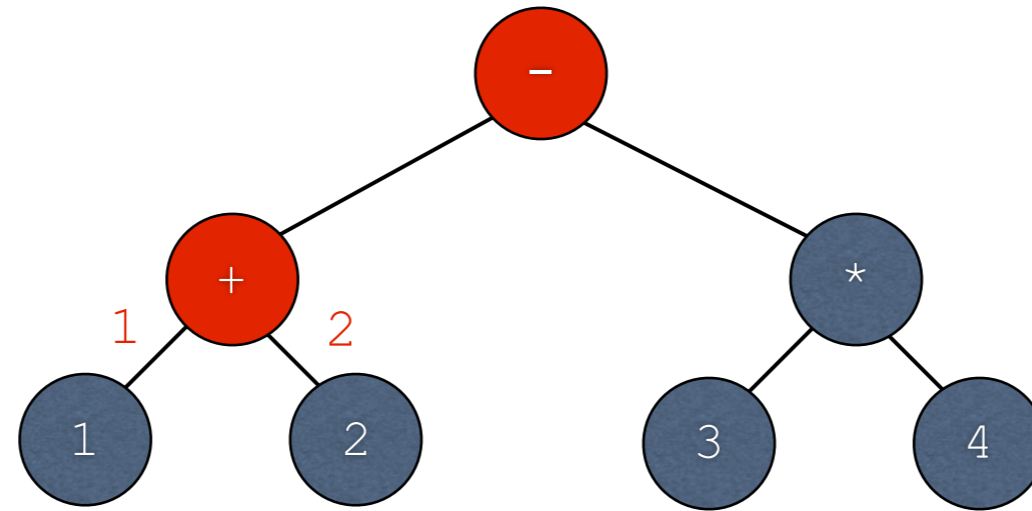
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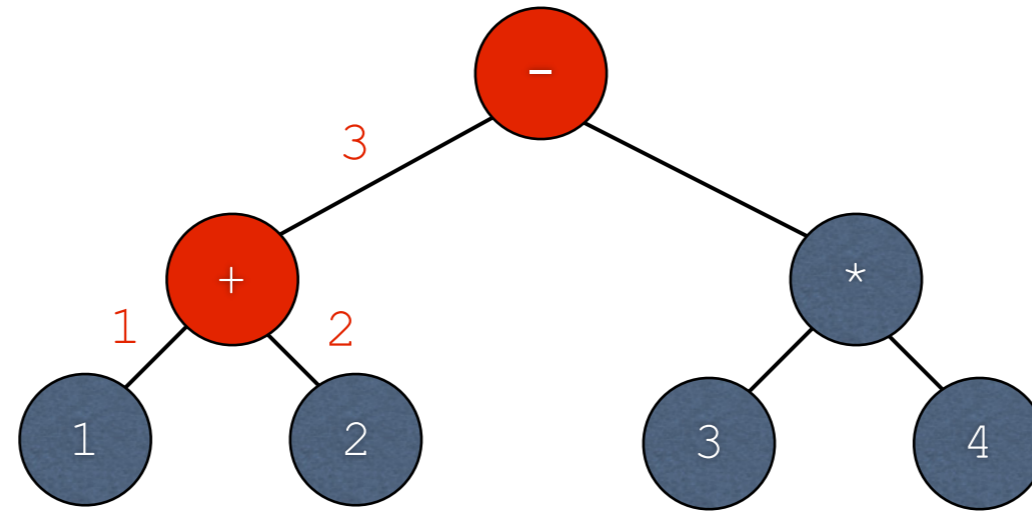
-As before, leaves just return the value held within

Evaluation



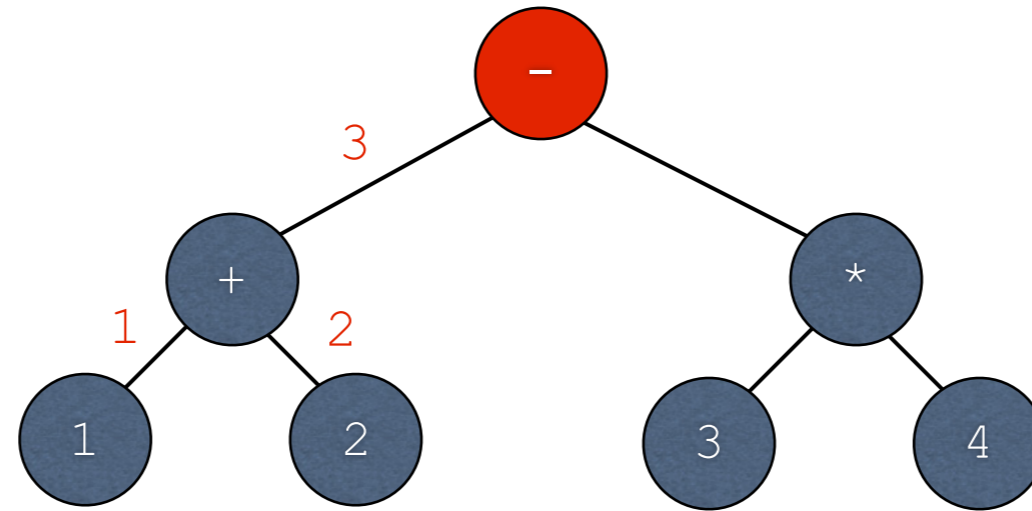
- Subtrees of + are now taken care of
- Now + has two values that it needs to work with...

Evaluation



-+ performs the actual addition

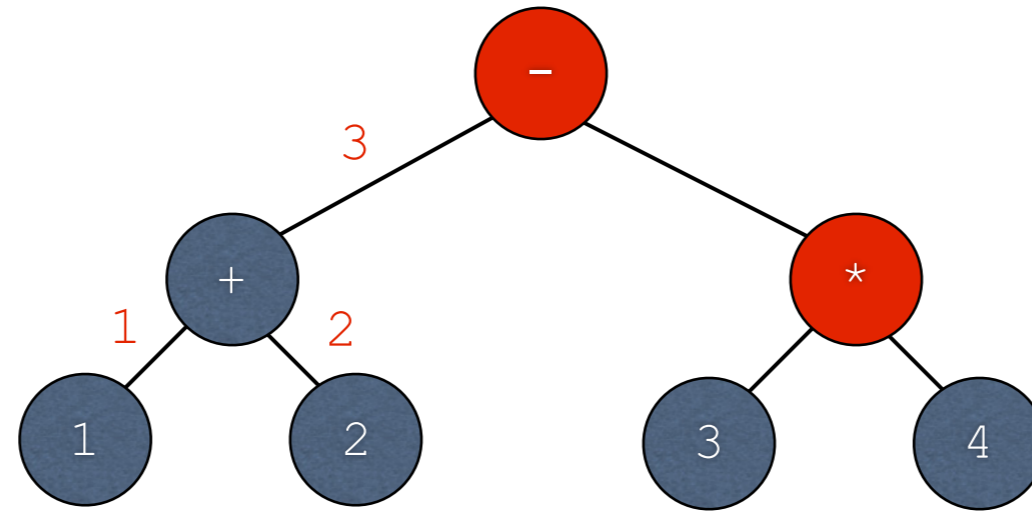
Evaluation



-Now + is taken care of

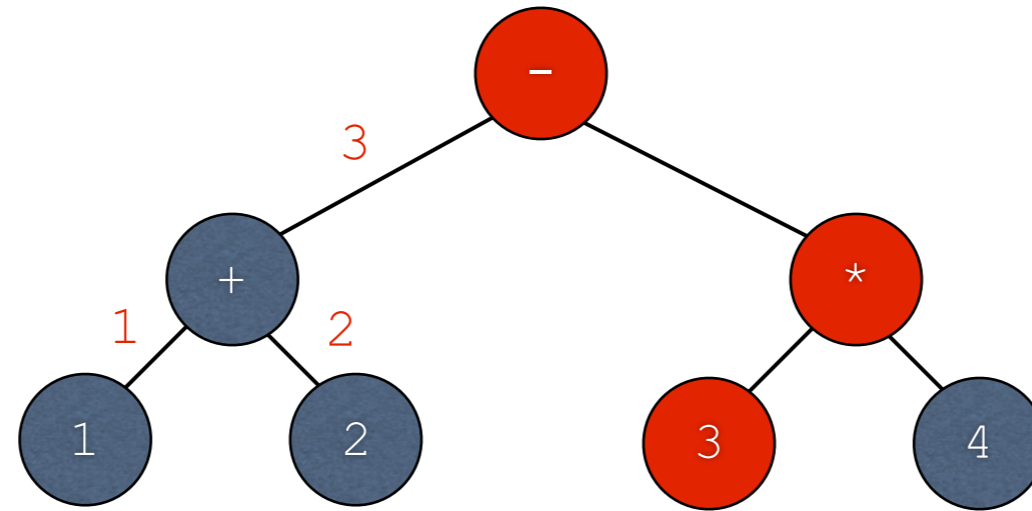
-Going back to -, - now has the value of the left subtree, and it needs the value of the right subtree

Evaluation



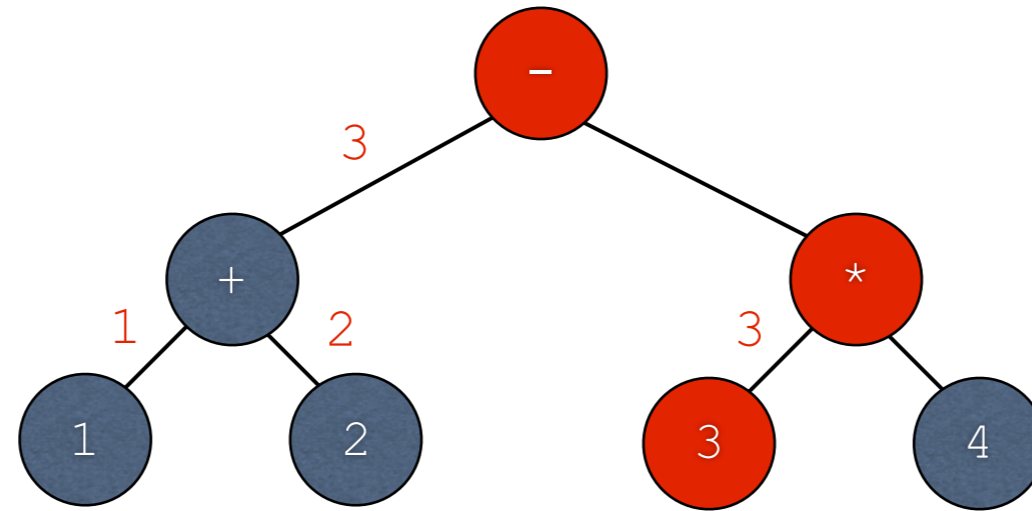
-Now we're on *, which needs the value of the left subtree...

Evaluation



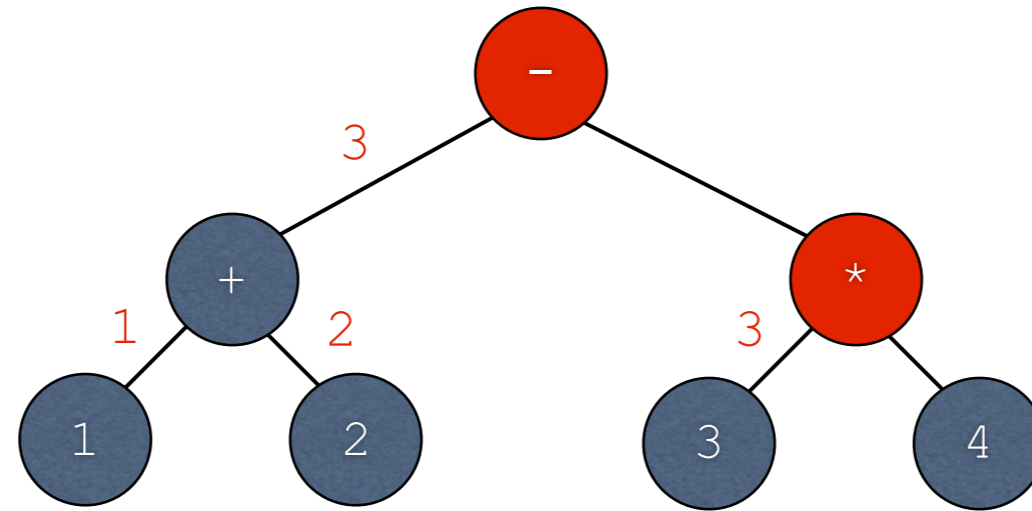
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Evaluation



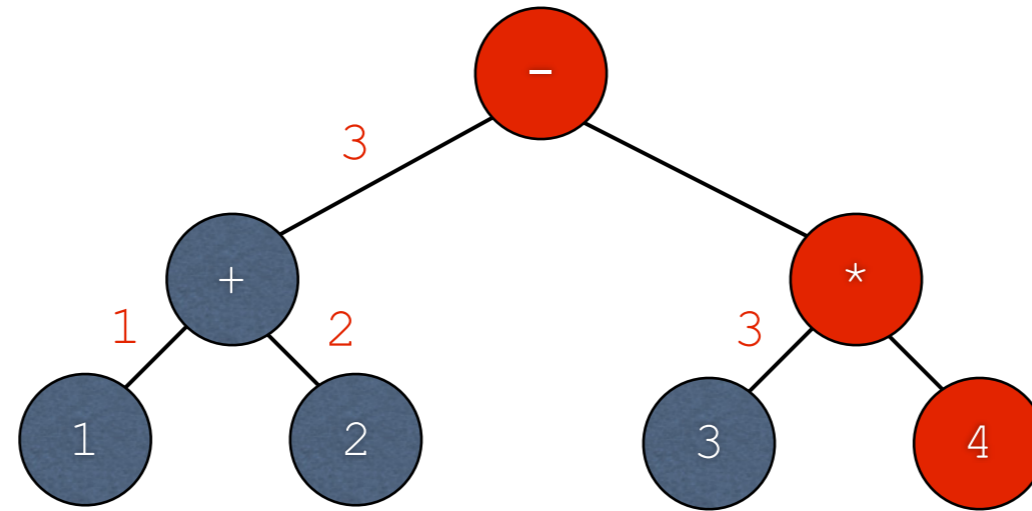
-Leaves again return the values held within...

Evaluation



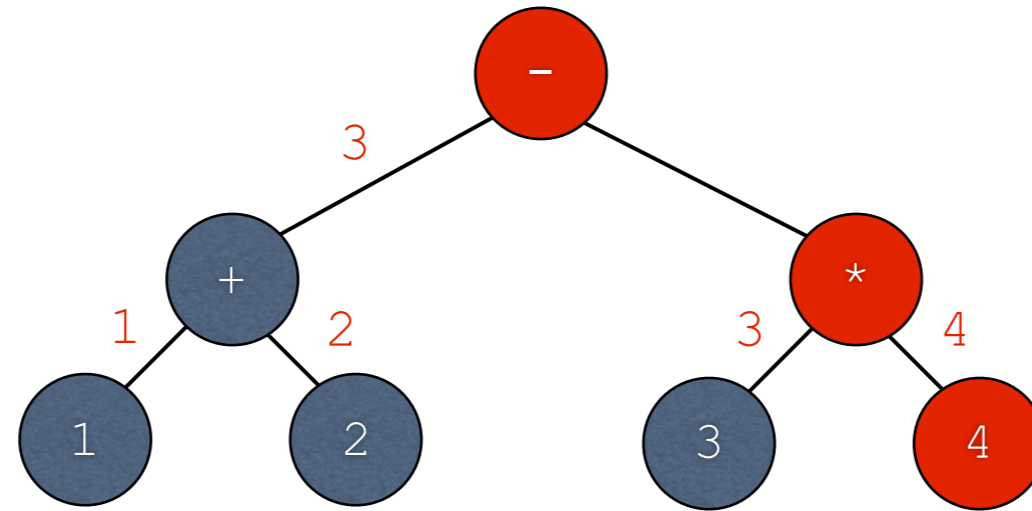
-Left subtree done; * now needs the value of the right subtree...

Evaluation



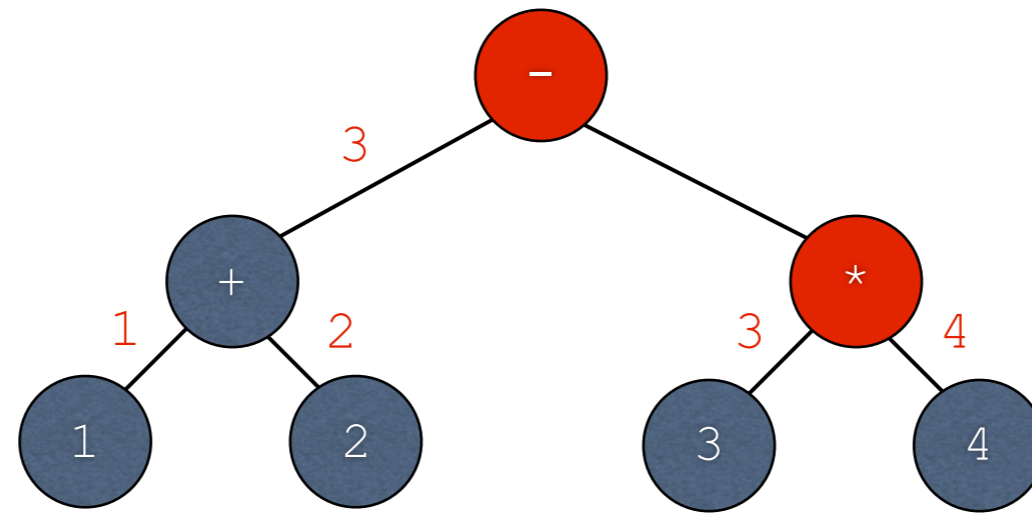
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Evaluation



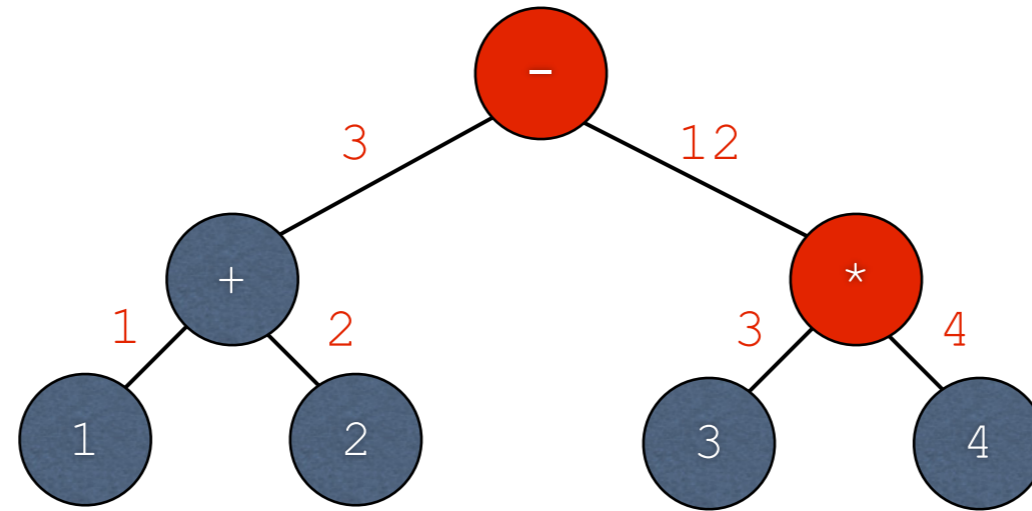
-Leaf returns value held within

Evaluation



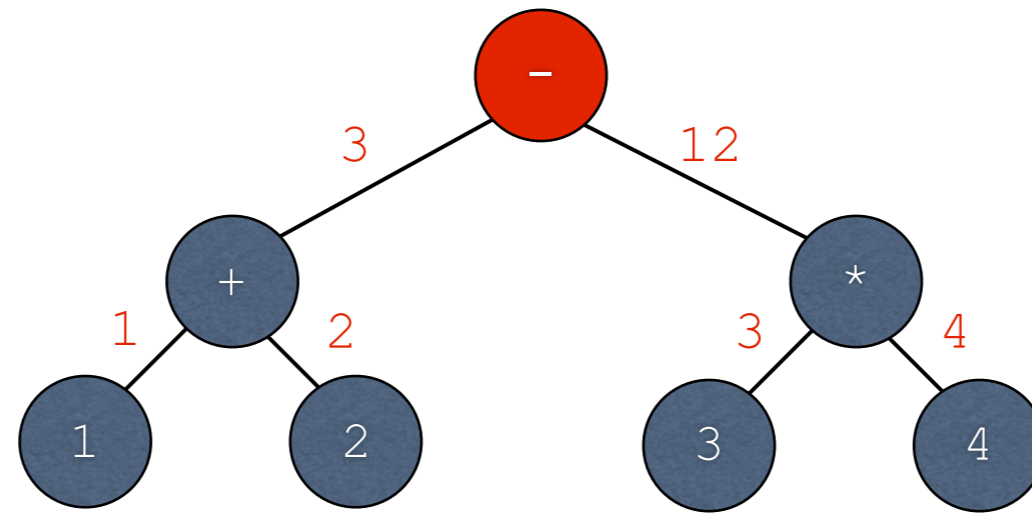
-Leaf is done. * now has both operands it needs...

Evaluation



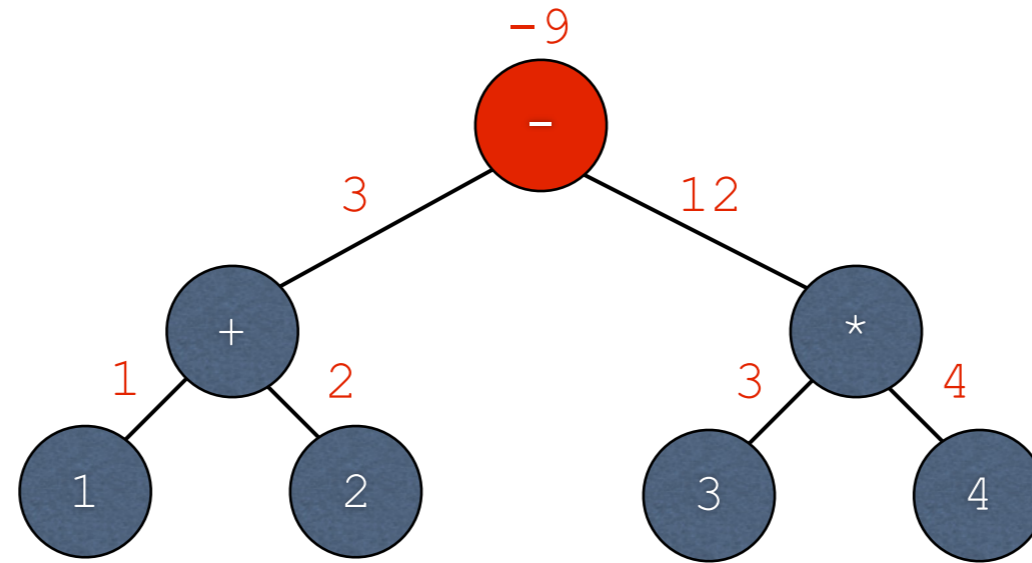
-* performs the multiplication and returns the value

Evaluation



-The root - node now has both operands...

Evaluation



-...and it returns the result of the subtraction

Exercise: Second Side of AST/Evaluation Sheet

Evaluator Example:

`arithmetic_evaluator.py`

-Complete example online; we'll live-code this in class

SAT and Semantic Tableau

SAT Background

SAT

- Short for the Boolean satisfiability problem
- Given a Boolean formula with variables, is there an assignment of true/false to the variables which makes the formula true?

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$$(x \vee \neg y) \wedge (\neg x \vee z)$$

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Yes: x is true, z is true

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$$(x \wedge \neg x)$$

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$$(x \wedge \neg x)$$

No

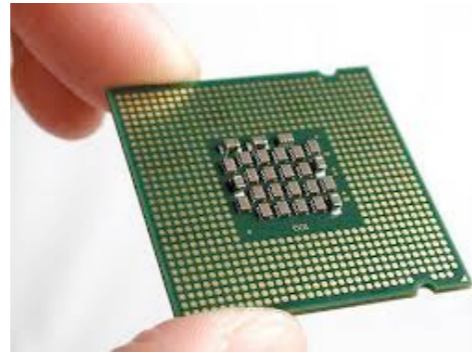
Relevance

Widespread usage in hardware and software verification

- Verification as in proving the system does what we intend
- Much stronger guarantees than testing
- Testing can prove the existence of a bug (a failed test), whereas verification proves the absence of bugs (relative to the theorems proven)

Relevance

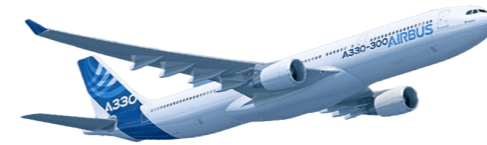
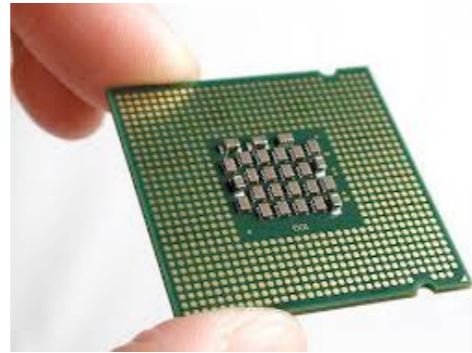
Widespread usage in hardware and software verification



- Circuits can be represented as Boolean formulas
- Can basically phrase proofs as $\text{Circuit} \wedge \text{BadThing}$. If unsatisfiable, then BadThing cannot occur. If satisfiable, then the solution gives the circumstance under which BadThing occurs.
- Many details omitted (entire careers are based on this stuff)

Relevance

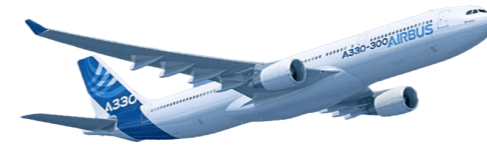
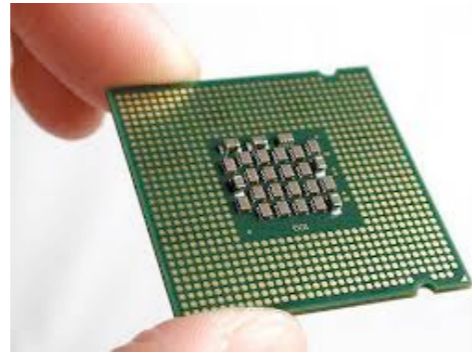
Widespread usage in hardware and software verification



- (Likely) used by AirBus to verify that flight control software does the right thing
- Lots of proprietary details so it's not 100% clear how this verification works, but SAT is still relevant to the problem

Relevance

Widespread usage in hardware and software verification



-Nasa uses software verification for a variety of tasks; SAT is relevant, though other techniques are used, too

Relevance to Logic Programming

- Methods for solving SAT can be used to execute logic programs
- Logic programming can be phrased as SAT with some additional stuff

Semantic Tableau

- One method for solving SAT instances
- Basic idea: iterate over the formula
 - Maintain subformulas that must be true
 - Learn which variables must be true/false
 - Stop at conflicts (unsatisfiable), or when no subformulas remain (have solution)

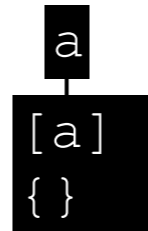
-There are many methods to this

Positive Literals

a

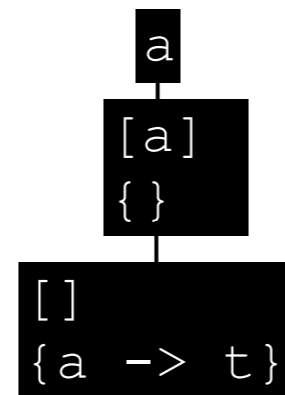
-As in, the input formula is simply "a"

Positive Literals



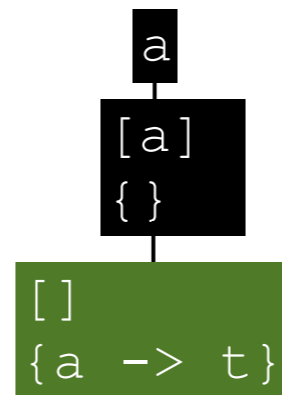
- One subformula must be true: a
- Initially, we don't know what any variables must map to

Positive Literals



-For formula "a" to be true, it must be the case that a is true

Positive Literals



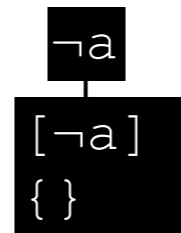
-No subformulas remain, so we are done. The satisfying solution is that a must be true.

Negative Literals

$\neg a$

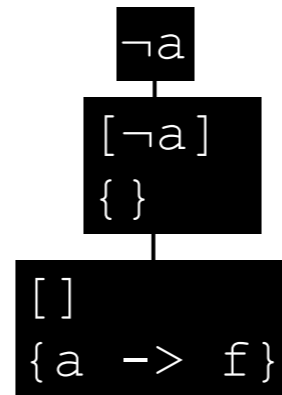
-As in, the input formula is simply " $\neg a$ "

Negative Literals



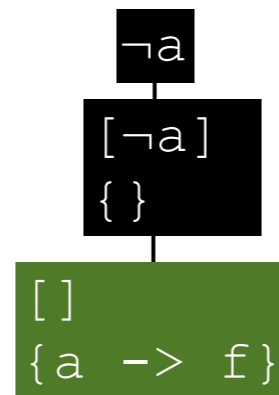
- One subformula must be true: $\neg a$
- Initially, we don't know what any variables must map to

Negative Literals



-For subformula " $\neg a$ " to be true, it must be the case that a is false

Negative Literals

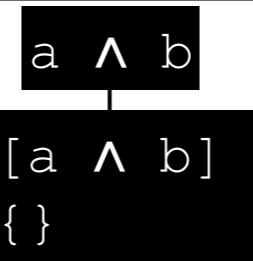


-No subformulas remain, so we are done. The satisfying solution is that “a” must be false.

Logical And

$a \wedge b$

Logical And



- Initially, one subformula must be true: $a \wedge b$
- Initially, we don't know what any variable must map to

Logical And

$a \wedge b$

$[a \wedge b]$
{ }

$[a, b]$
{ }

-For $a \wedge b$ to be true, subformulas a and b must both be true

Logical And

$a \wedge b$

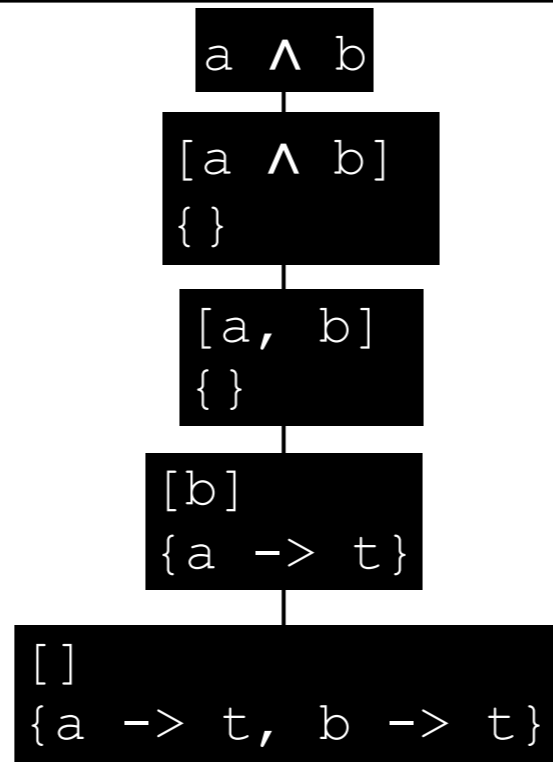
$[a \wedge b]$
{ }

$[a, b]$
{ }

$[b]$
{ $a \rightarrow t$ }

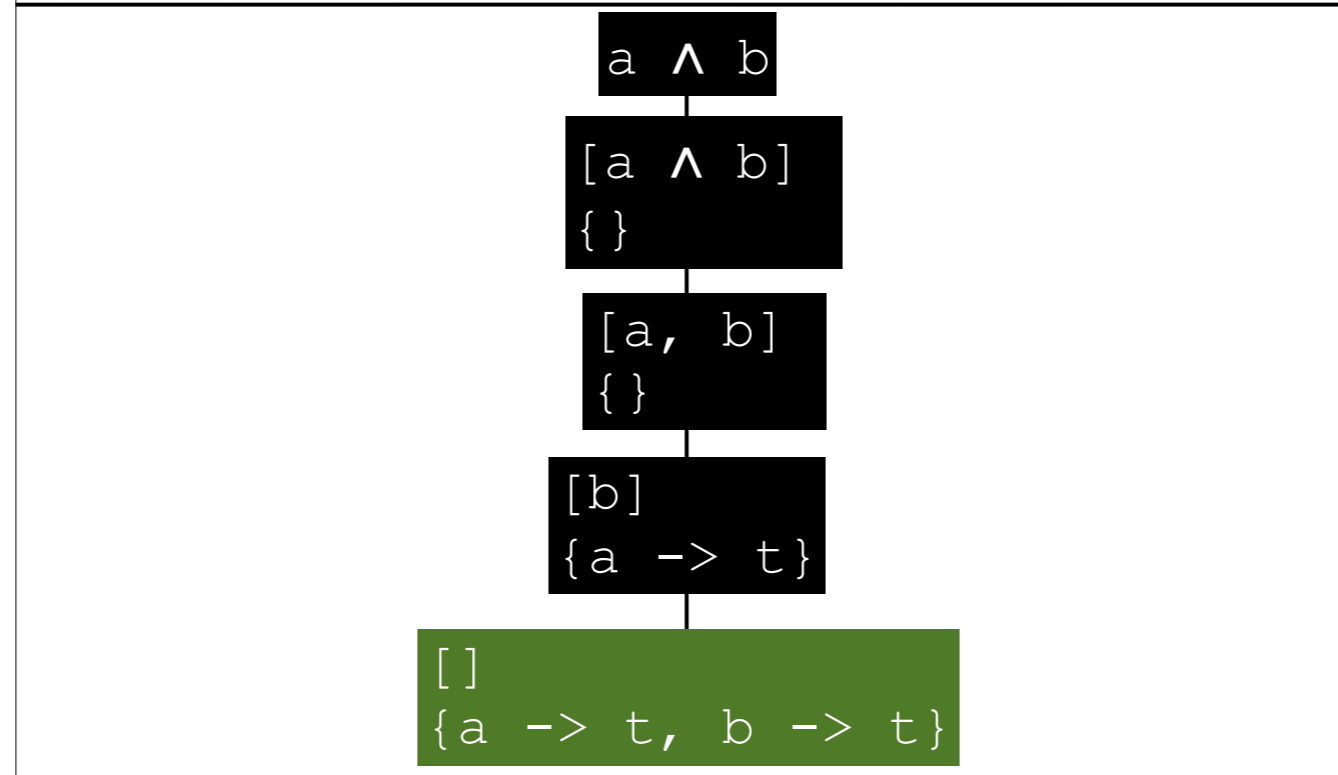
-From the positive literal case, for formula a to be true, variable a must be true

Logical And



-From the positive literal case, for formula b to be true, variable b must be true

Logical And



-No subformulas remain, so we are done with the solution that both a and b must be true

Logical And

$$a \wedge \neg a$$

-Alternative example, showing a conflict

Logical And

$a \wedge \neg a$

$[a \wedge \neg a]$
{ }

Logical And

$a \wedge \neg a$

$[a \wedge \neg a]$
{ }

$[\neg a]$
{ $a \rightarrow t$ }

Logical And

$a \wedge \neg a$

$[a \wedge \neg a]$
{ }

$[\neg a]$
{ $a \rightarrow t$ }



- Now we have a problem: for formula $\neg a$ to be true, it must be the case that variable a is false
- We've already recorded that variable a must be true, which is the opposite of what we expect.
- As such, we have a conflict - this formula is unsatisfiable

Exercise: First Side of SAT Sheet

Logical Or

$$a \vee \neg a$$

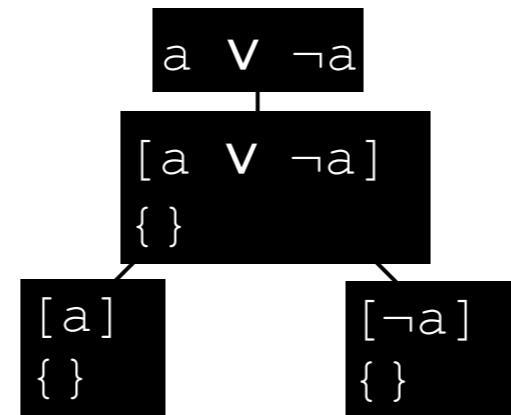
Logical Or

$a \vee \neg a$

$[a \vee \neg a]$

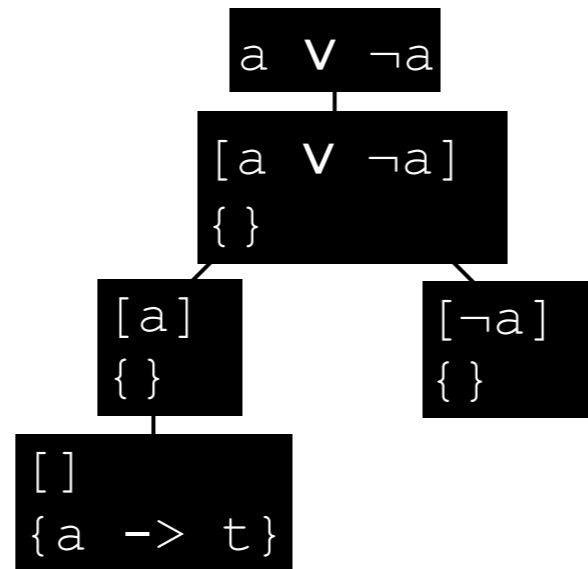
$\{\}$

Logical Or



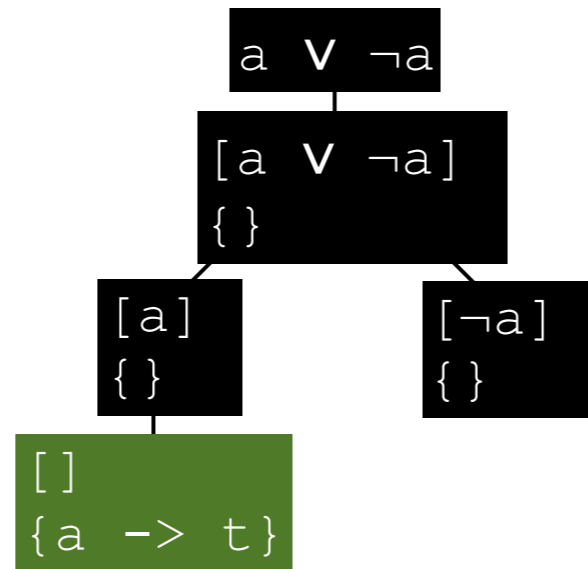
-World splits on or: in one world we pick the left subformula, and in another we pick the right

Logical Or



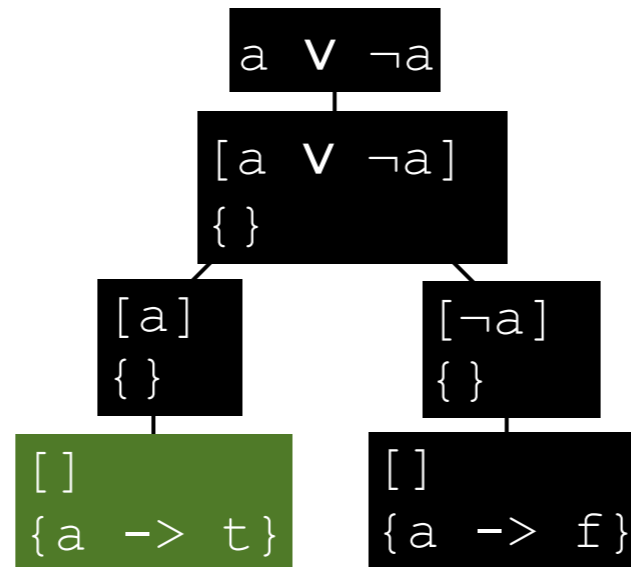
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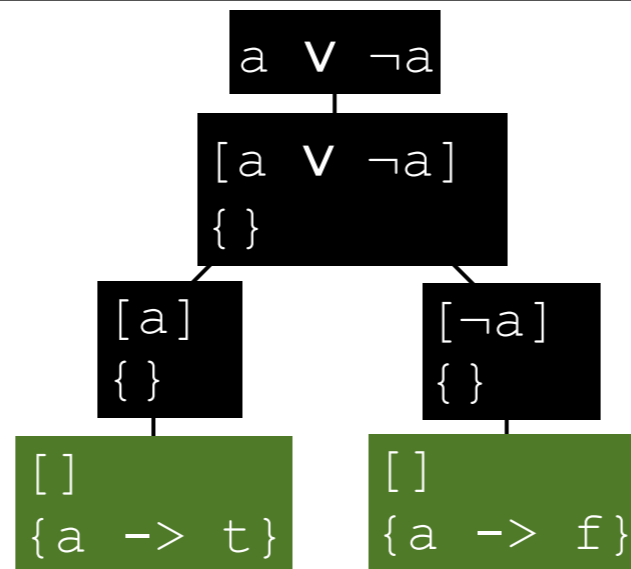
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Logical Or



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Logical Or



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Examples

Example 1:

$$(\neg b \vee a) \wedge b$$

$(\neg b \vee a) \wedge b$

$(\neg b \vee a) \wedge b$

$[(\neg b \vee a), b]$
 $\{\}$

$(\neg b \vee a) \wedge b$

$[(\neg b \vee a), b]$
 $\{\}$

$[\neg b, b]$
 $\{\}$

$(\neg b \vee a) \wedge b$

$[(\neg b \vee a), b]$
 $\{\}$

$[\neg b, b]$
 $\{\}$

$[b]$
 $\{b \rightarrow f\}$

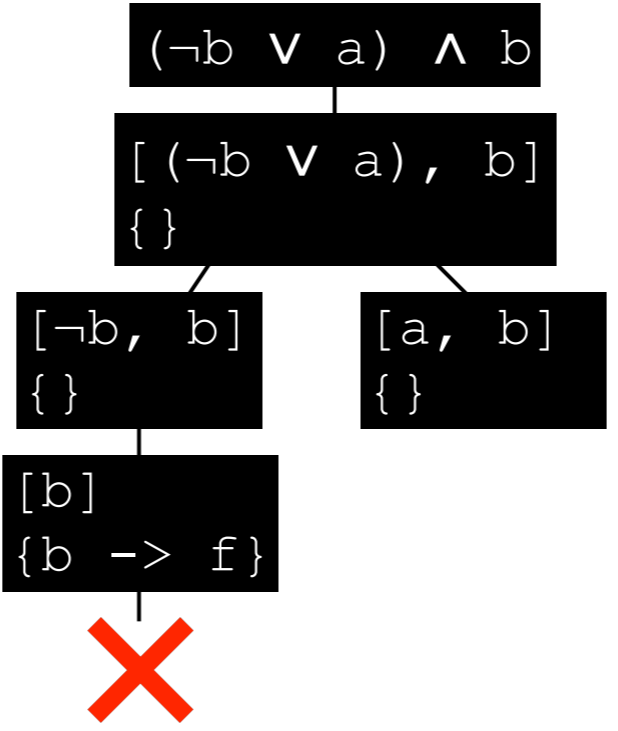
$(\neg b \vee a) \wedge b$

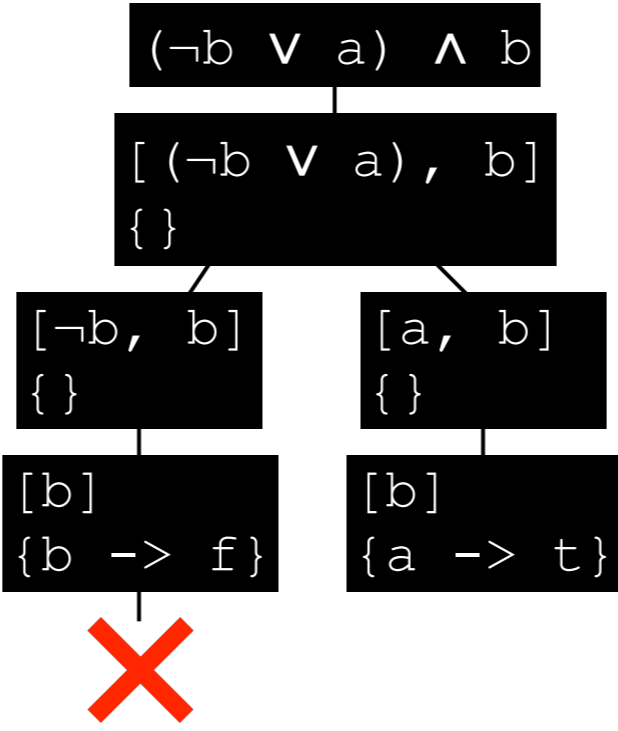
$[(\neg b \vee a), b]$
 $\{\}$

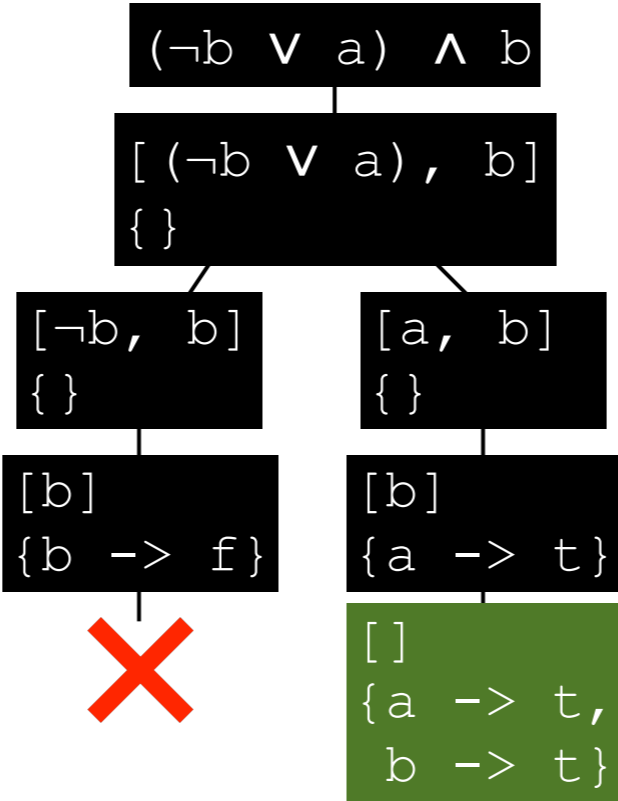
$[\neg b, b]$
 $\{\}$

$[b]$
 $\{b \rightarrow f\}$









Example 2:

$$(x \vee \neg y) \wedge (\neg x \vee z)$$

$$(x \vee \neg y) \wedge (\neg x \vee z)$$

$$(x \vee \neg y) \wedge (\neg x \vee z)$$
$$[(x \vee \neg y), (\neg x \vee z)]$$
$$\{\}$$

$(x \vee \neg y) \wedge (\neg x \vee z)$

$[(x \vee \neg y), (\neg x \vee z)]$
 $\{\}$

$[x, (\neg x \vee z)]$
 $\{\}$

$(x \vee \neg y) \wedge (\neg x \vee z)$

$[(x \vee \neg y), (\neg x \vee z)]$
 $\{\}$

$[x, (\neg x \vee z)]$
 $\{\}$

$[(\neg x \vee z)]$
 $\{x \rightarrow t\}$

$(x \vee \neg y) \wedge (\neg x \vee z)$

$[(x \vee \neg y), (\neg x \vee z)]$
 $\{\}$

$[x, (\neg x \vee z)]$
 $\{\}$

$[(\neg x \vee z)]$
 $\{x \rightarrow t\}$

$[\neg x]$
 $\{x \rightarrow t\}$

$(x \vee \neg y) \wedge (\neg x \vee z)$

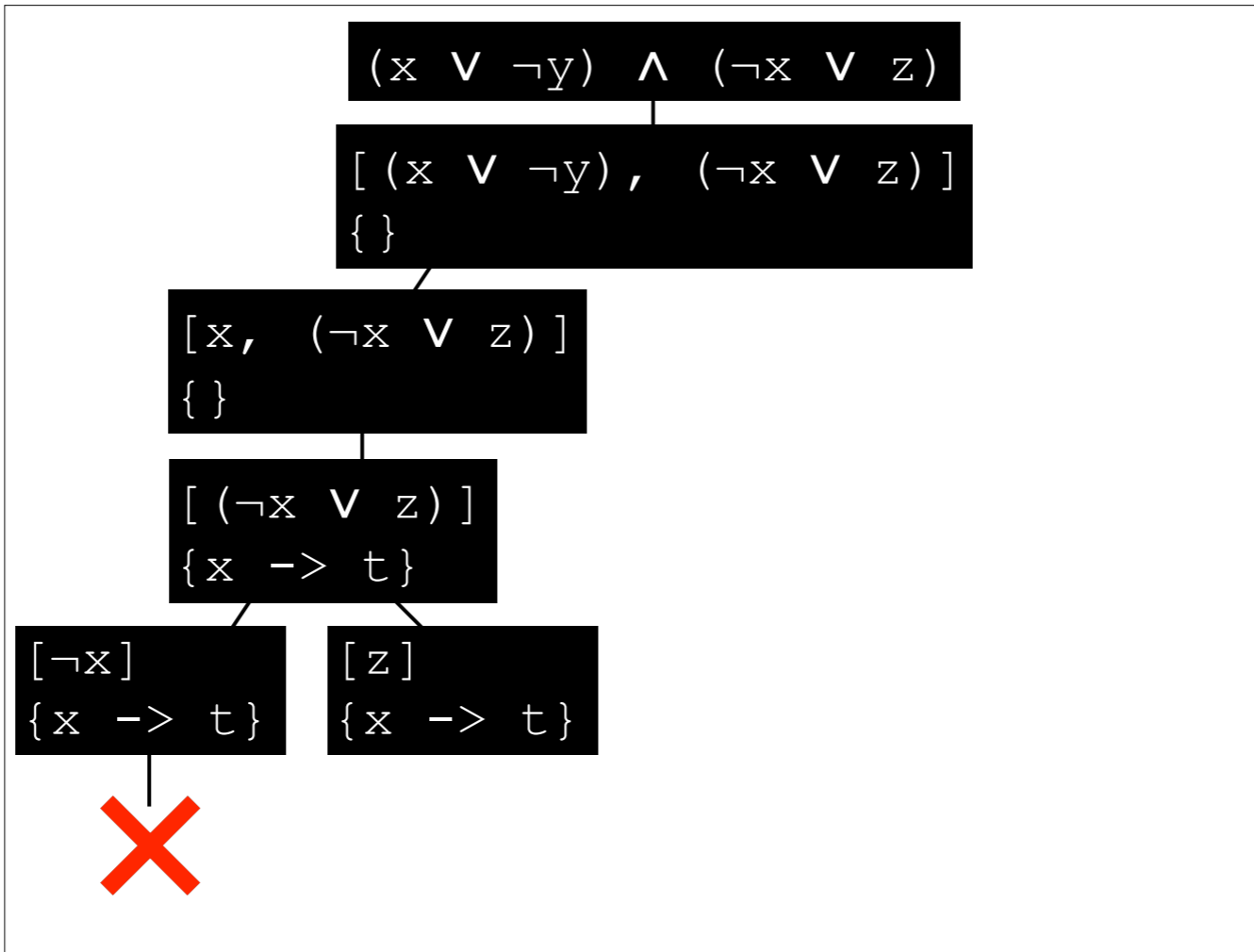
$[(x \vee \neg y), (\neg x \vee z)]$
 $\{\}$

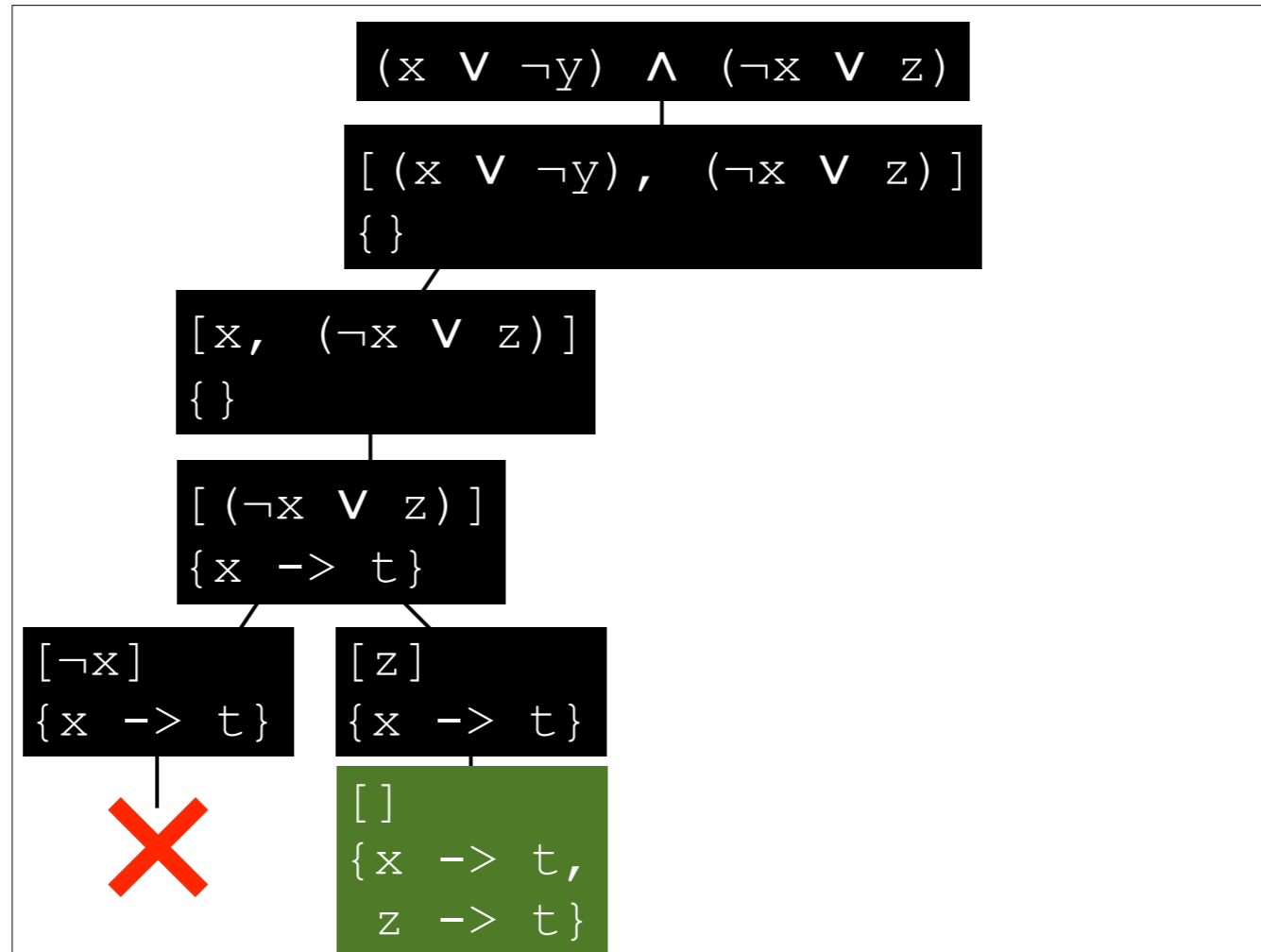
$[x, (\neg x \vee z)]$
 $\{\}$

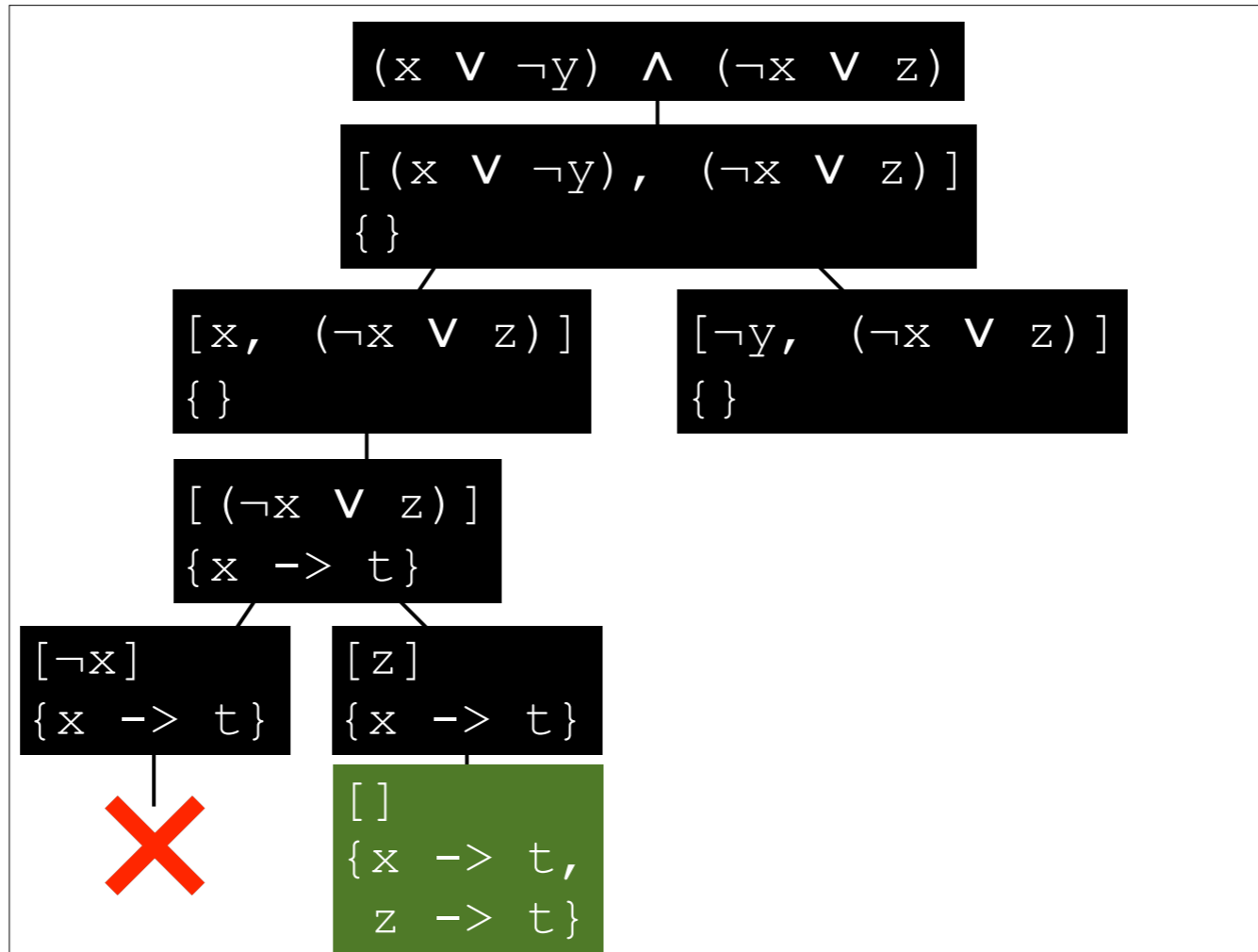
$[(\neg x \vee z)]$
 $\{x \rightarrow t\}$

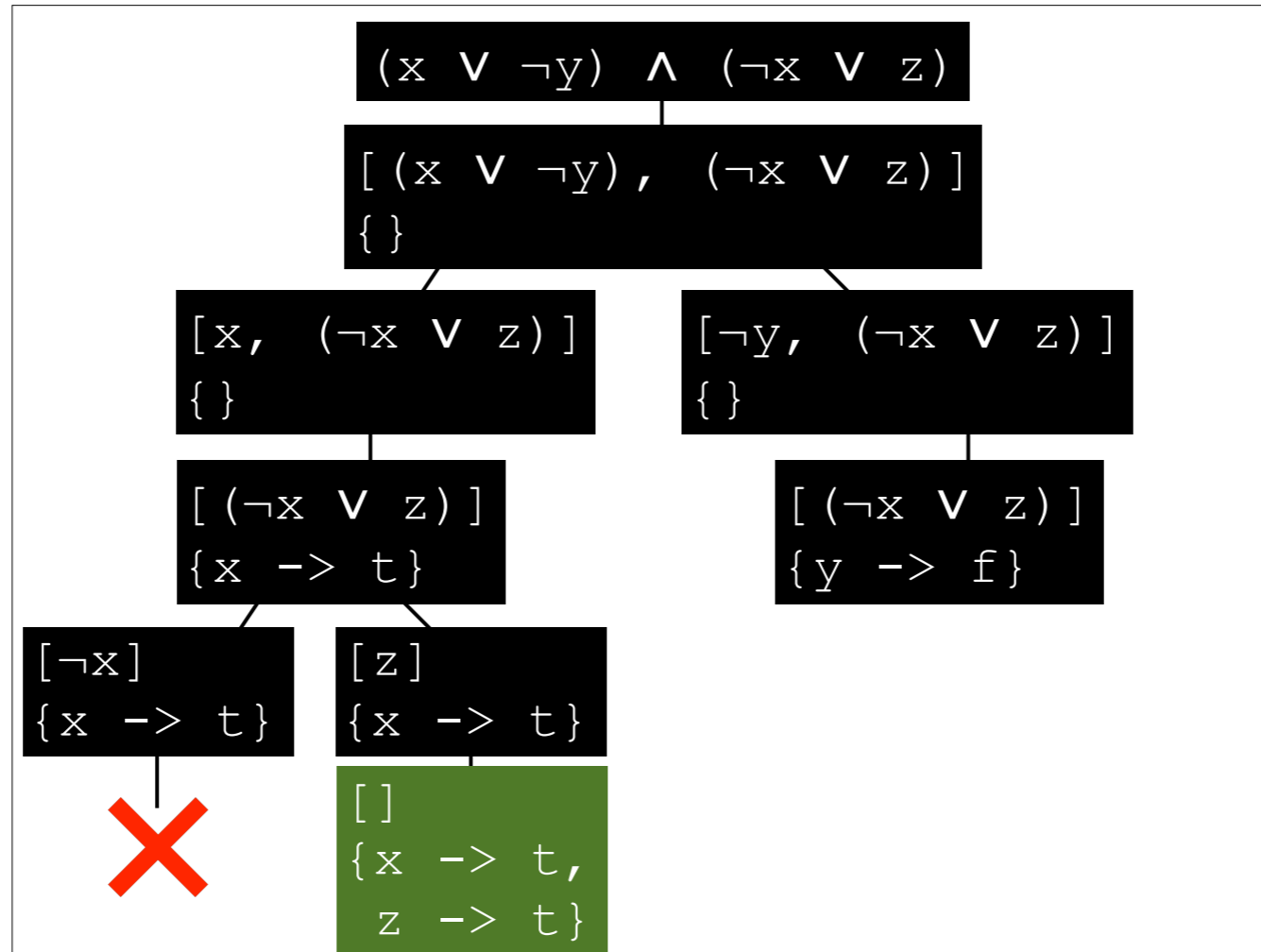
$[\neg x]$
 $\{x \rightarrow t\}$

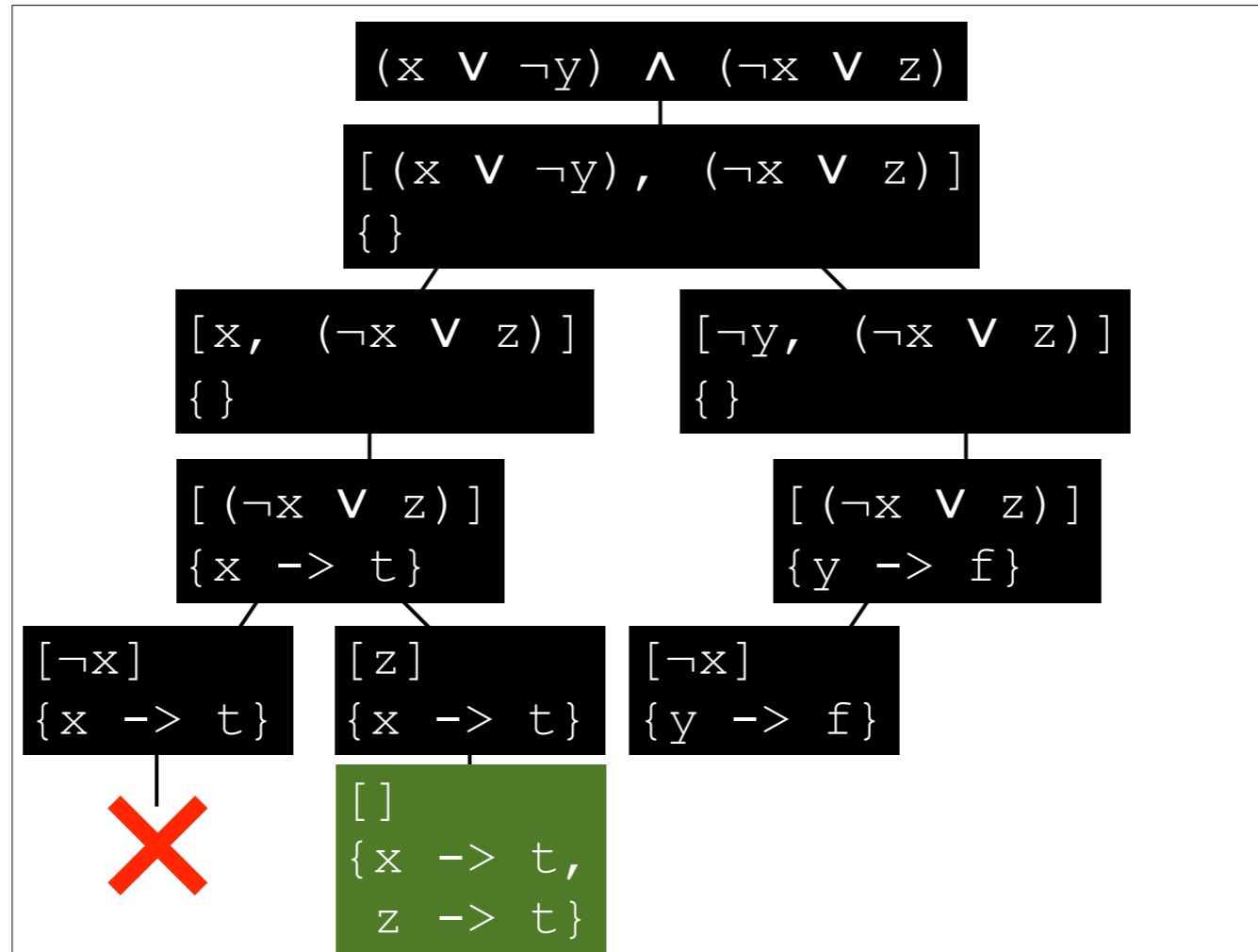


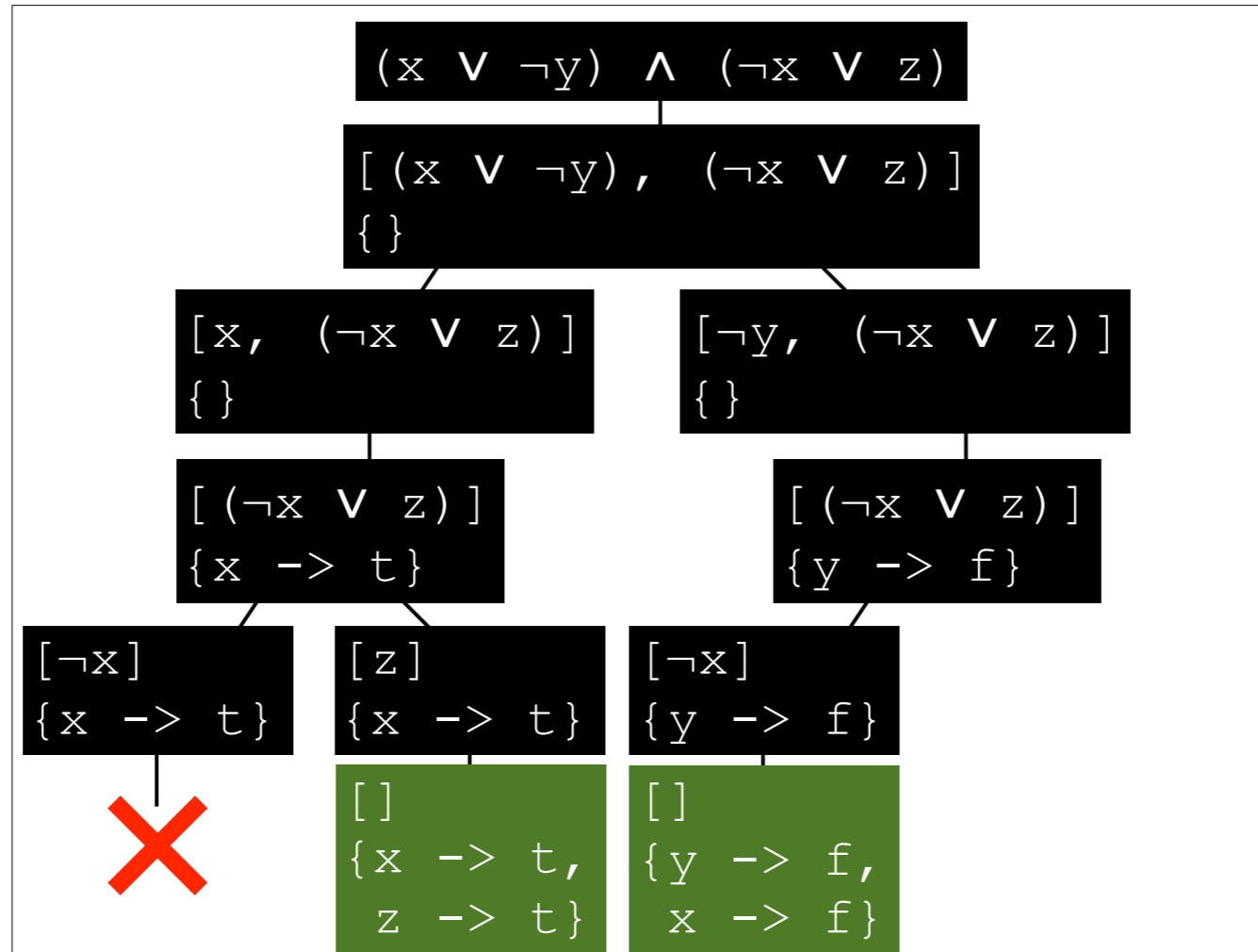


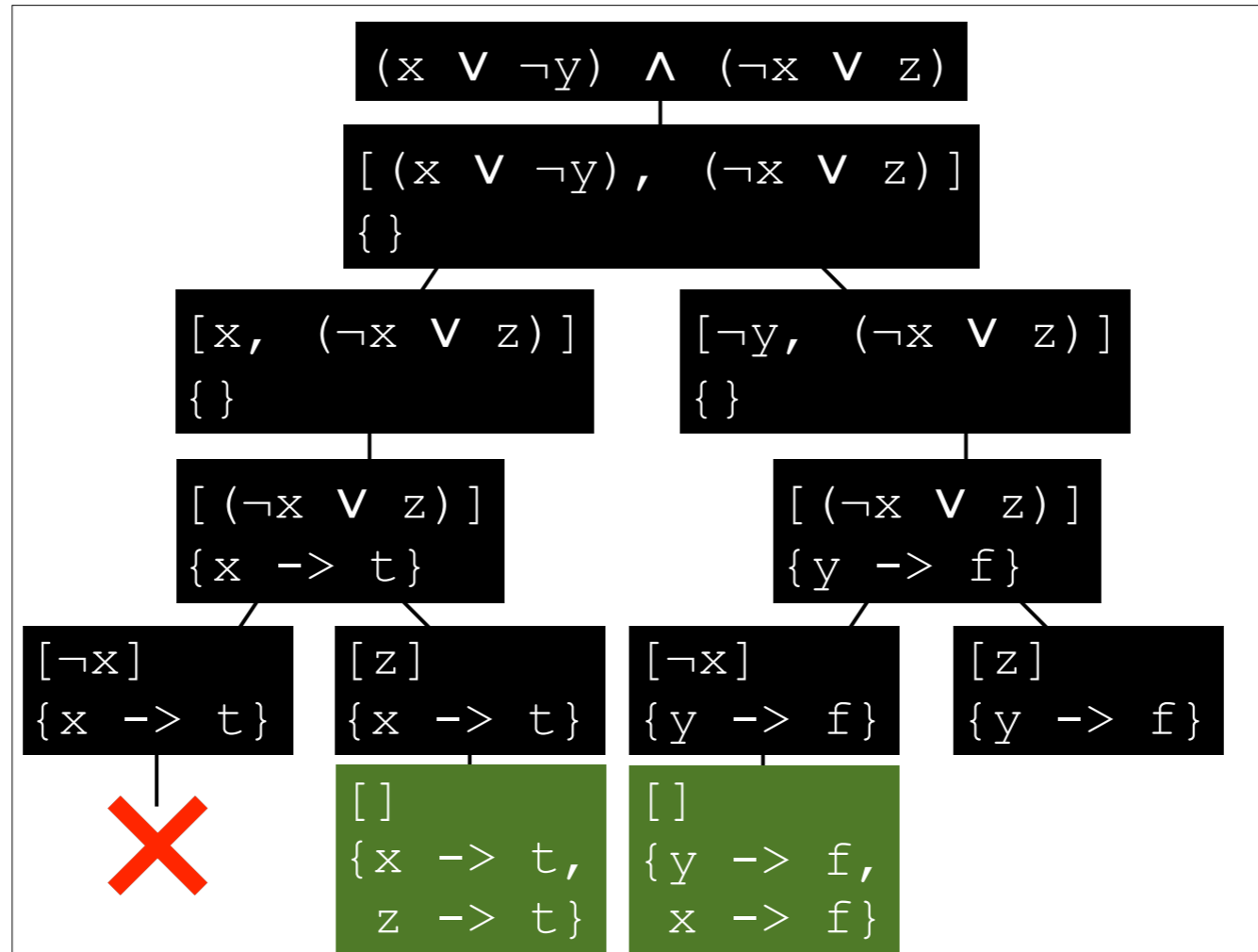


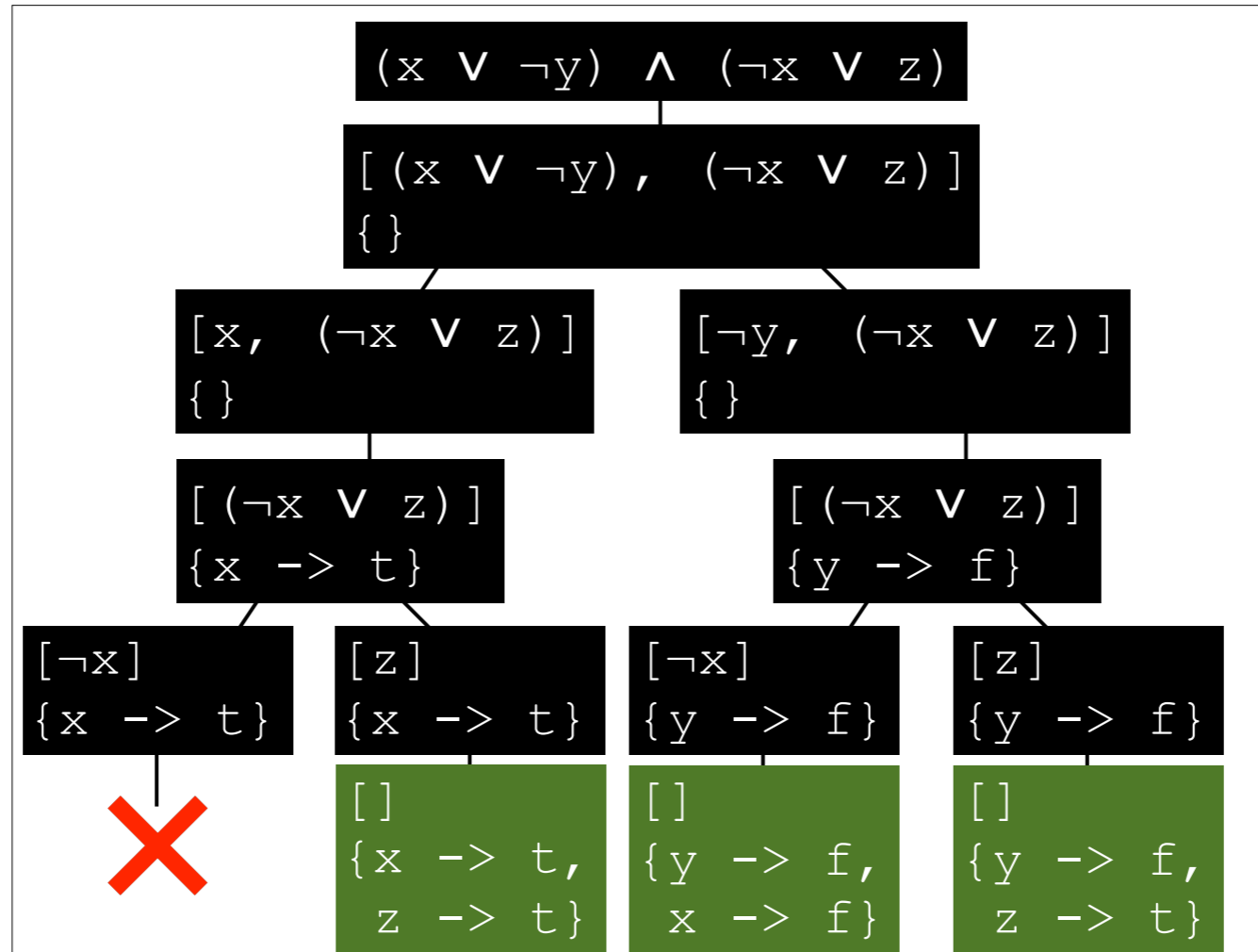












Exercise: Second Side of SAT Sheet