# COMP 410 Lecture 1

Kyle Dewey

### About Me

- My research
  - Automated program testing + CS education
  - Programming language design
- My dissertation used logic programming extensively
- I've taught this class a bunch

# About this Class

- See something wrong? Want something improved? Email me about it! (kyle.dewey@csun.edu)
- I generally operate based on feedback

# **Bad Feedback**

- This guy sucks.
- This class is boring.
- This material is useless.

-I can't do anything in response to this

# Good Feedback

- This guy sucks, I can't read his writing.
- This class is boring, it's way too slow.
- This material is useless, I don't see how it relates to anything in reality.
- I can't fix anything if I don't know what's wrong

-I can actually do something about this!

- -Major programming paradigm a way of thinking about problems
- -Emphases thinking about exactly \_what\_ the problem is, as opposed to exactly \_how\_ to solve it. This is called declarative programming.
- -For example: it's generally easier to say what constraints must hold for a valid Sudoku solution, as opposed to directly finding a valid Sudoku solution.
- -Somewhat related to functional programming we generally lack mutable state
- -Unlike any other major paradigm, the distinction between inputs and outputs is intentionally blurred. You can take advantage of this.
- -Basis in formal logic. It's the only major paradigm where "=" has the same meaning as it does in math.

• What, not how

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- -Strong emphasis on programming and using logic programming languages
- -I want you to think in this paradigm, not merely force Java into it
- -The ideas can be applied in non-logical languages, and your first assignment will force you to write in a logical way outside of a logic programming language (though you won't realize that's what you're doing yet)
- -Little bit of theory

# What is this Course?

• Programming, programming

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- Applying logic programming without a logic programming language

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## What this course isn't

Artificial intelligence

<sup>-&</sup>quot;Artificial intelligence" used to refer to search techniques, which is relevant to logic programming. Now the term largely refers to machine learning. What it means is a moving target.

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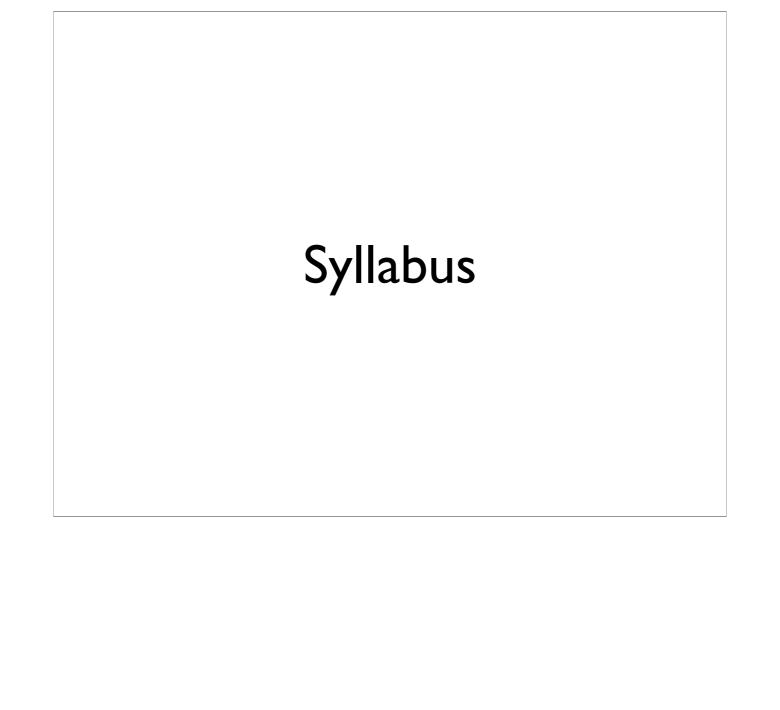
#### What this course isn't

- Artificial intelligence
- Machine learning
- Theoretical

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# SAT and Semantic Tableau

# SAT Background

- Short for the Boolean satisfiability problem
- Given a Boolean formula with variables, is there an assignment of true/false to the variables which makes the formula true?

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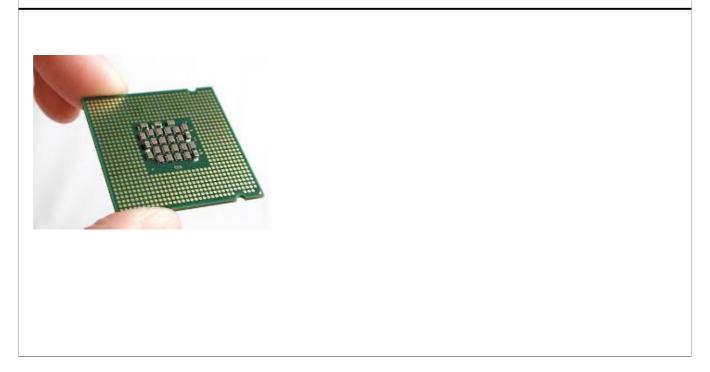
$$(x \land \neg x)$$

No

Widespread usage in hardware and software verification

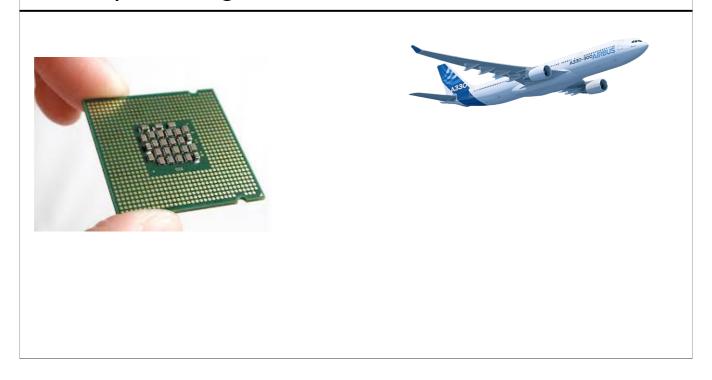
- -Verification as in \_proving\_ the system does what we intend
- -Much stronger guarantees than testing
- -Testing can prove the existence of a bug (a failed test), whereas verification proves the absence of bugs (relative to the theorems proven)

Widespread usage in hardware and software verification



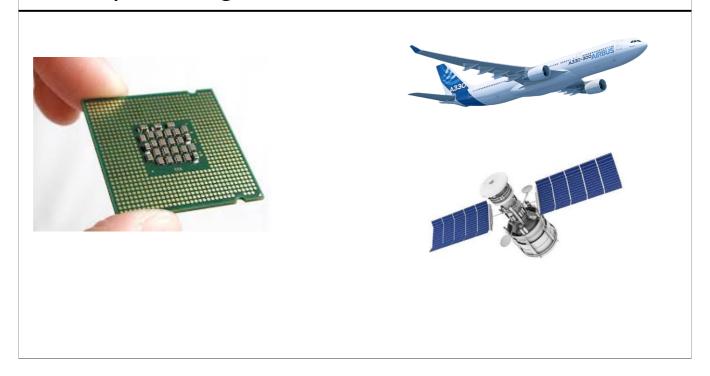
- -Circuits can be represented as Boolean formulas
- -Can basically phrase proofs as Circuit A BadThing. If unsatisfiable, then BadThing cannot occur. If satisfiable, then the solution gives the circumstance under which BadThing occurs.
- -Many details omitted (entire careers are based on this stuff)

Widespread usage in hardware and software verification



- -(Likely) used by AirBus to verify that flight control software does the right thing -Lots of proprietary details so it's not 100% clear how this verification works, but SAT is still relevant to the problem

Widespread usage in hardware and software verification



-Nasa uses software verification for a variety of tasks; SAT is relevant, though other techniques are used, too

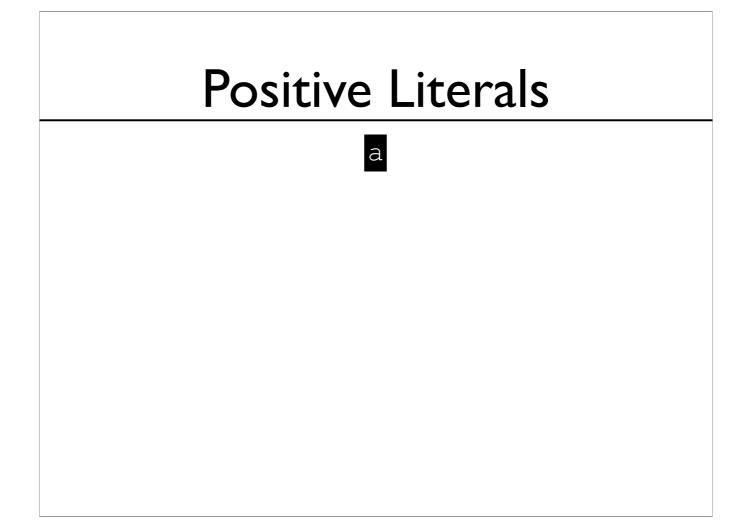
# Relevance to Logic Programming

- Methods for solving SAT can be used to execute logic programs
- Logic programming can be phrased as SAT with some additional stuff

## Semantic Tableau

- One method for solving SAT instances
- Basic idea: iterate over the formula
  - Maintain subformulas that must be true
  - Learn which variables must be true/false
  - Stop at conflicts (unsatisfiable), or when no subformulas remain (have solution)

-There are many methods to this



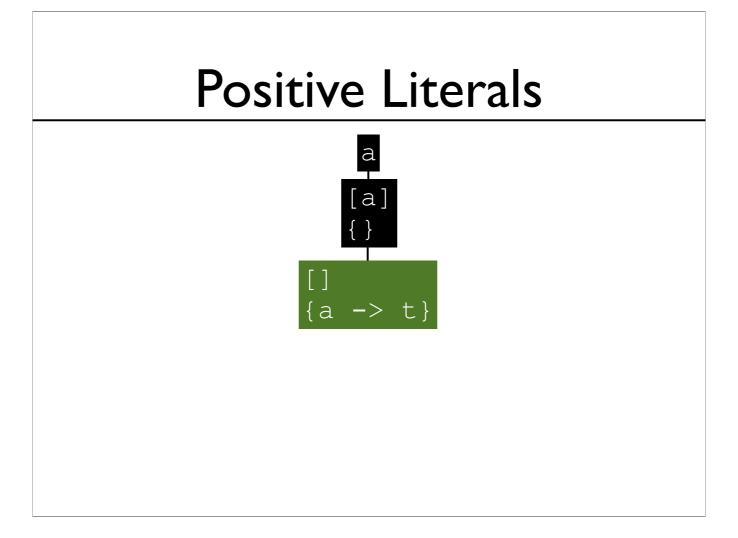
-As in, the input formula is simply "a"

# Positive Literals

- -One subformula must be true: a
- -Initially, we don't know what any variables must map to

# Positive Literals [a] [a] {a} [a] {a} [a] {a} -> t}

-For formula "a" to be true, it must be the case that a is true



-No subformulas remain, so we are done. The satisfying solution is that a must be true.

#### Negative Literals

-As in, the input formula is simply " $\neg a$ "

## Negative Literals

- -One subformula must be true: ¬a
- -Initially, we don't know what any variables must map to

# Negative Literals [7a] {} [a -> f}

-For subformula " $\neg$ a" to be true, it must be the case that a is false

# Negative Literals [-a] {} [a -> f}

-No subformulas remain, so we are done. The satisfying solution is that "a" must be false.

#### Logical And a 1 b



### Logical And a 1 b [a 1 b] {}

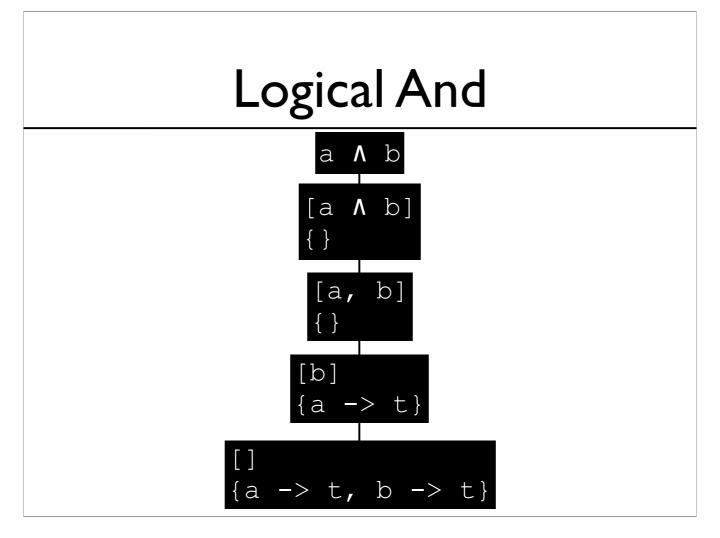
- -Initially, one subformula must be true: a  $\wedge$  b
- -Initially, we don't know what any variable must map to

# Logical And a 1 b [a 1 b] {} [a, b] {}

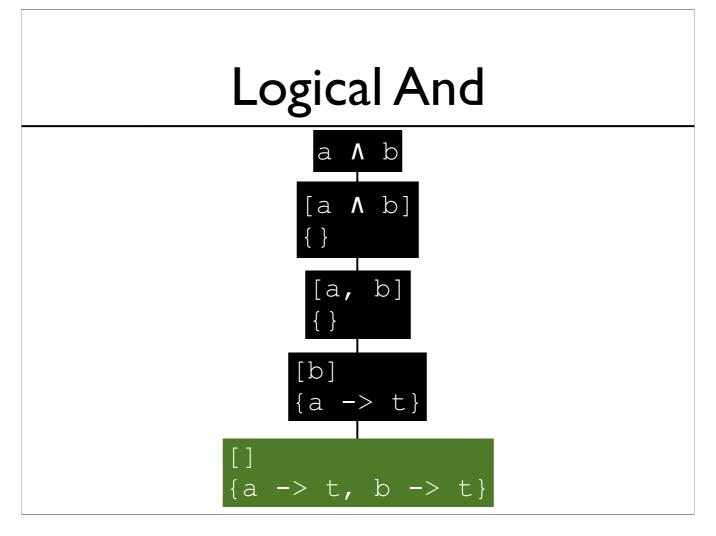
-For a  ${\scriptstyle \wedge}$  b to be true, subformulas a and b must both be true

# Logical And a \ b [a \ b] {a \ b] {b} [a, b] {b} [b] {a -> t}

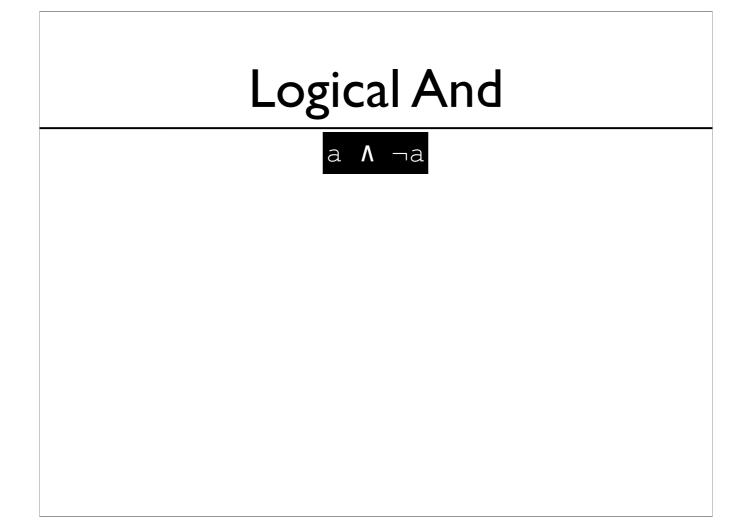
-From the positive literal case, for formula a to be true, variable a must be true



-From the positive literal case, for formula b to be true, variable b must be true

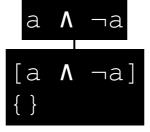


-No subformulas remain, so we are done with the solution that both a and b must be true

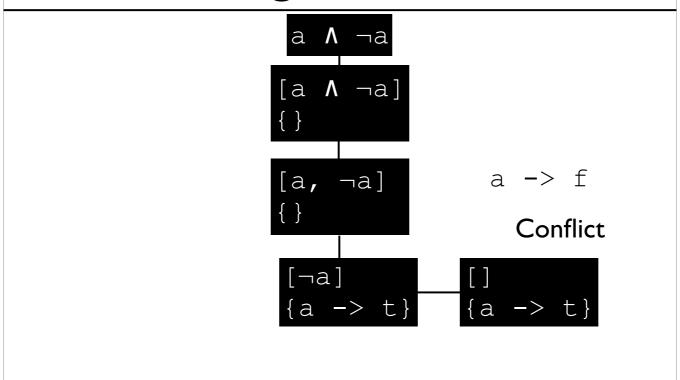


-Alternative example, showing a conflict

#### Logical And



#### Logical And



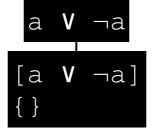
## Logical And a A ¬a [a A ¬a] {} [¬a] {a -> t}

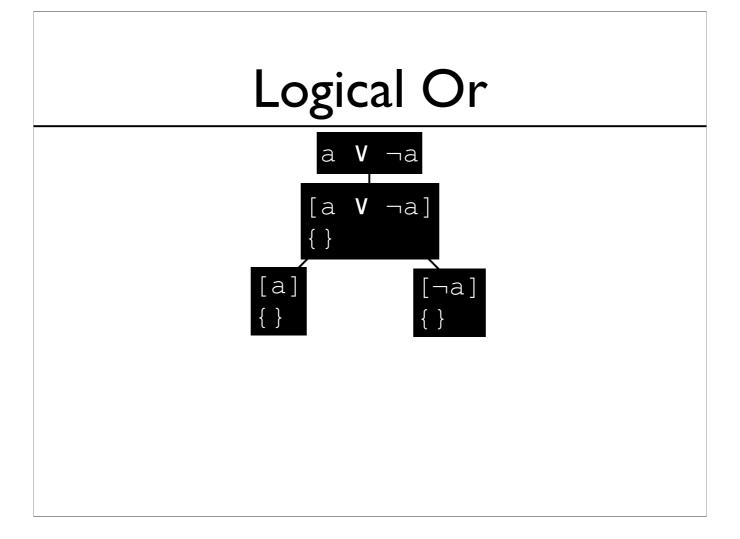
- -Now we have a problem: for formula  $\neg a$  to be true, it must be the case that variable a is false
- -We've already recorded that variable a must be true, which is the opposite of what we expect.
- -As such, we have a conflict this formula is unsatisfiable

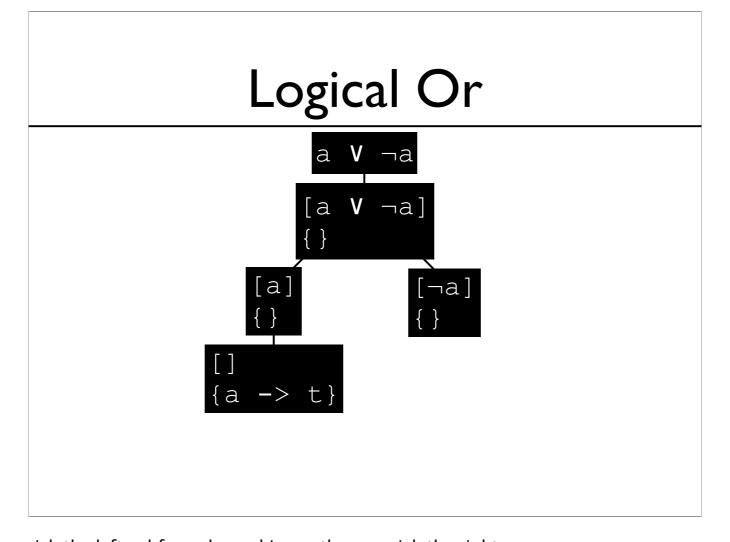
#### Exercise: First Side of SAT Sheet

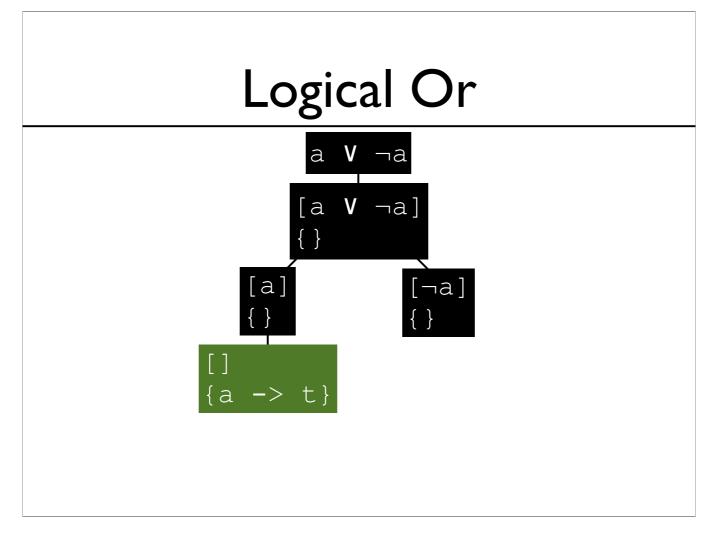
#### Logical Or a V ¬a

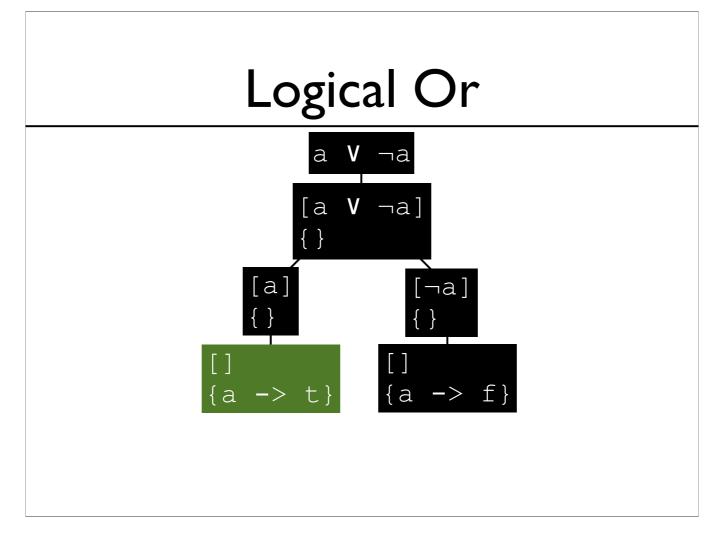
#### Logical Or

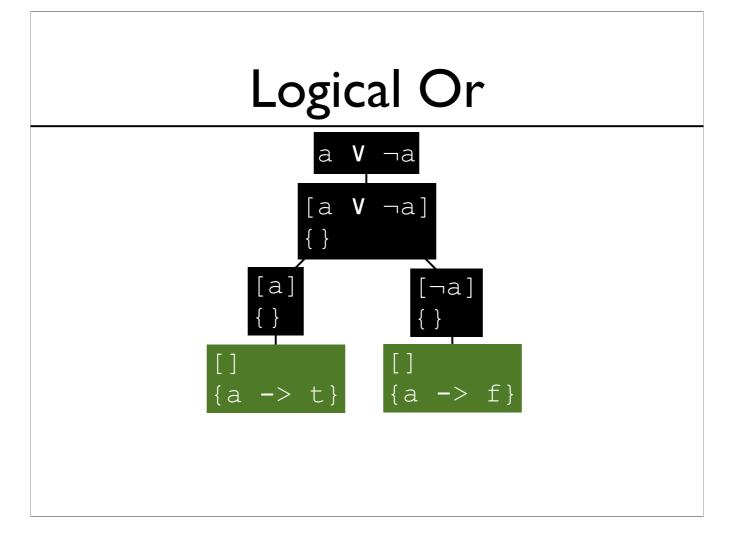


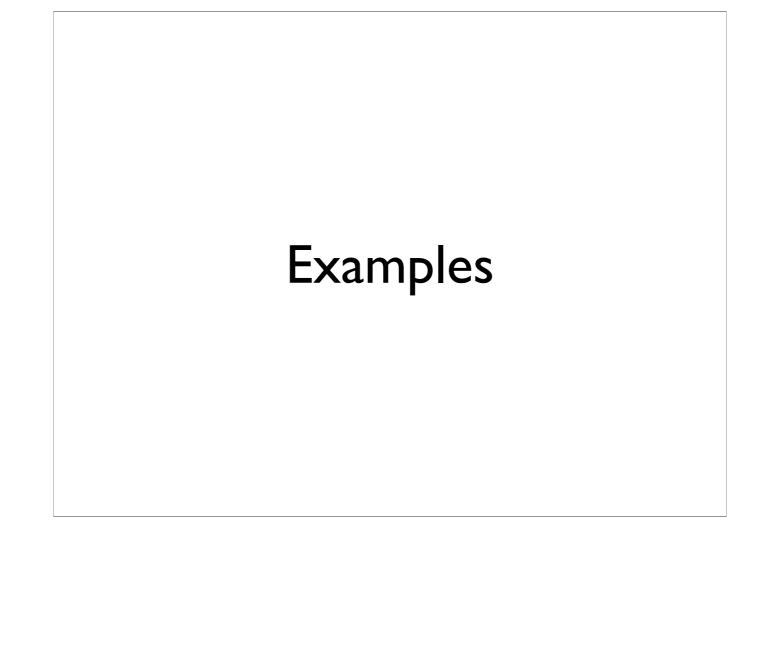








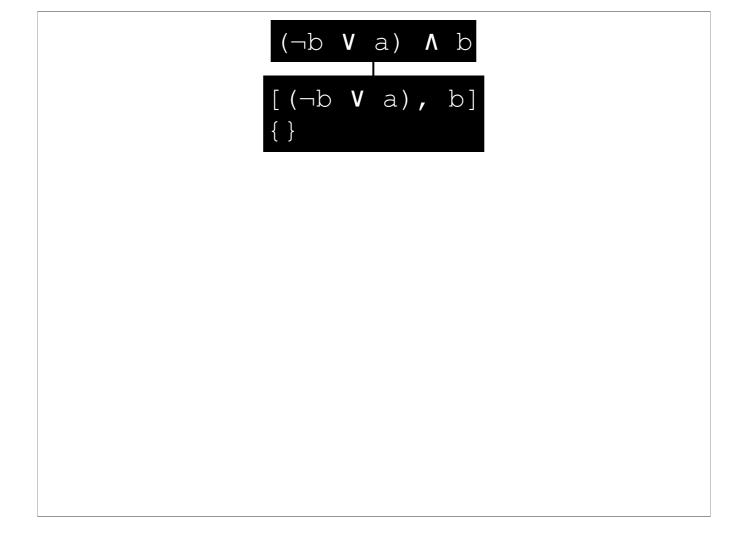


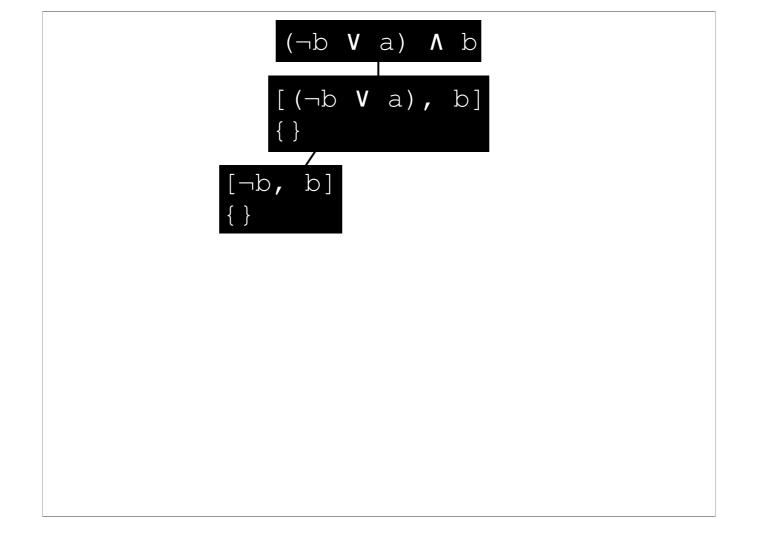


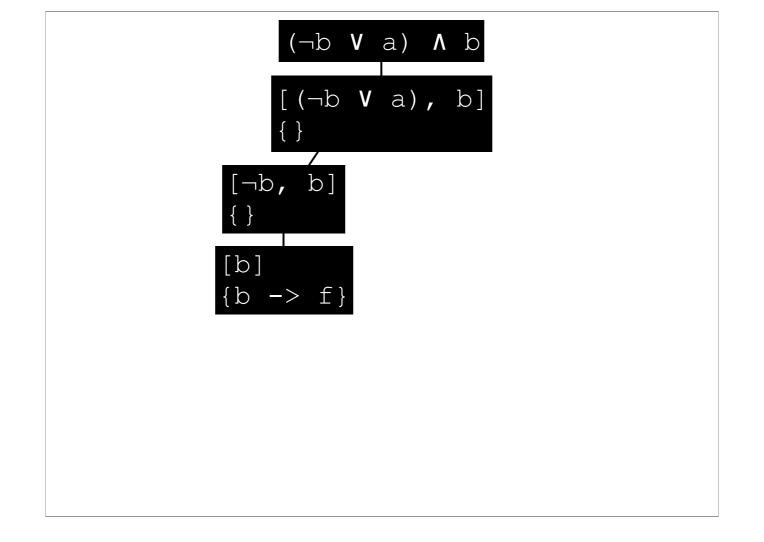
Example 1:

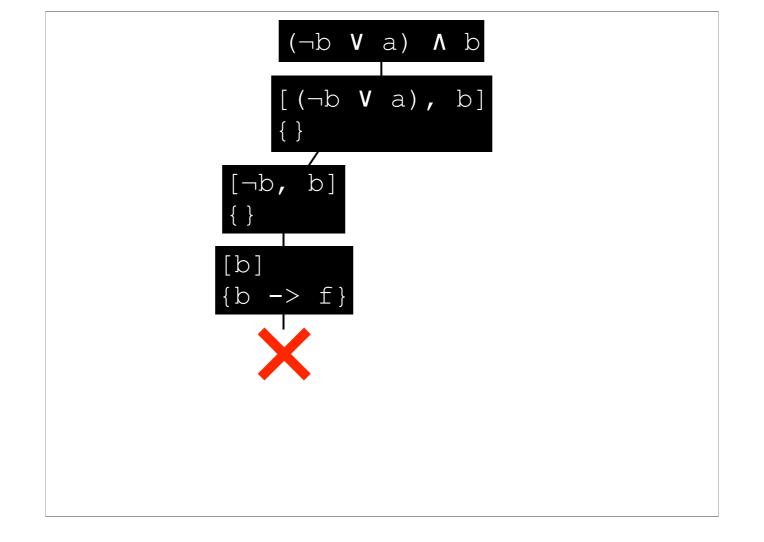
 $(\neg b \ V \ a) \ \Lambda \ b$ 

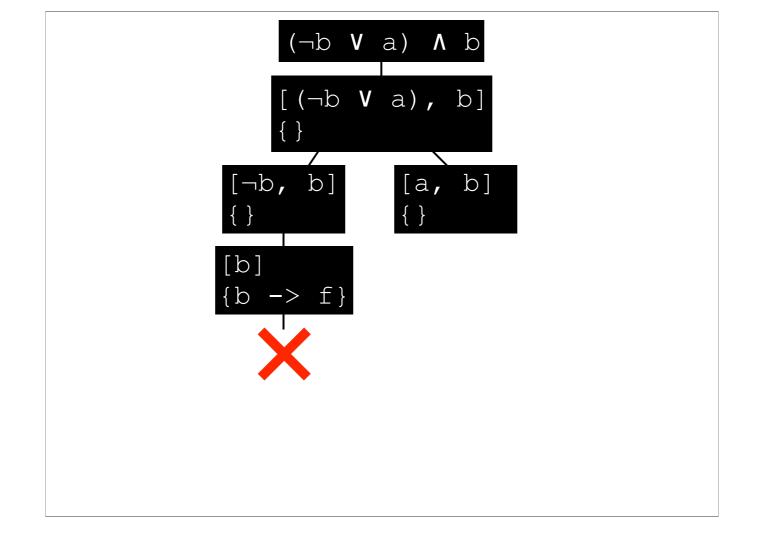
(¬b V	a) <b>\</b>	b	

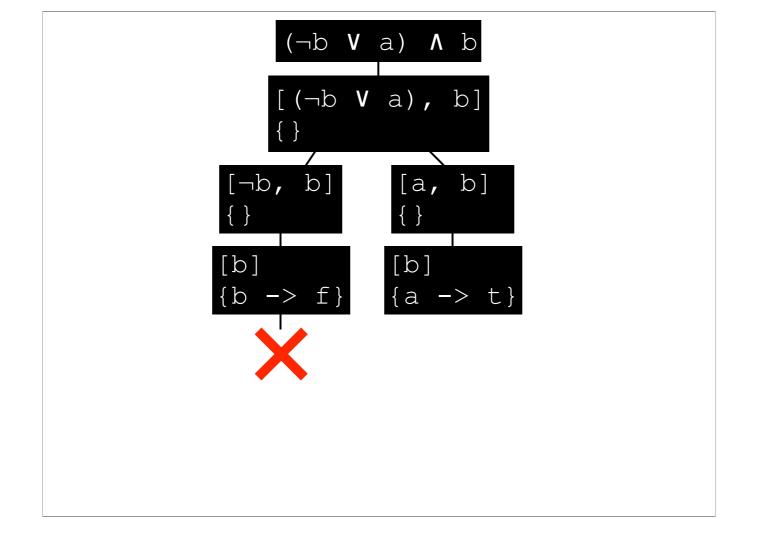


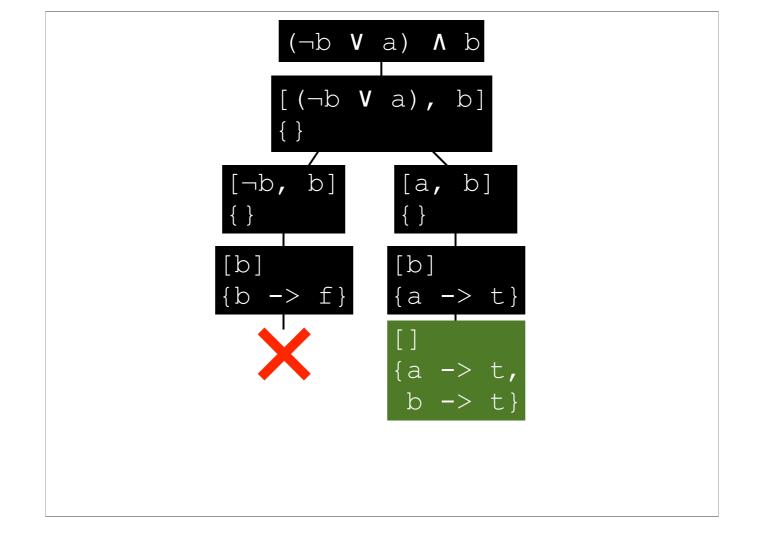








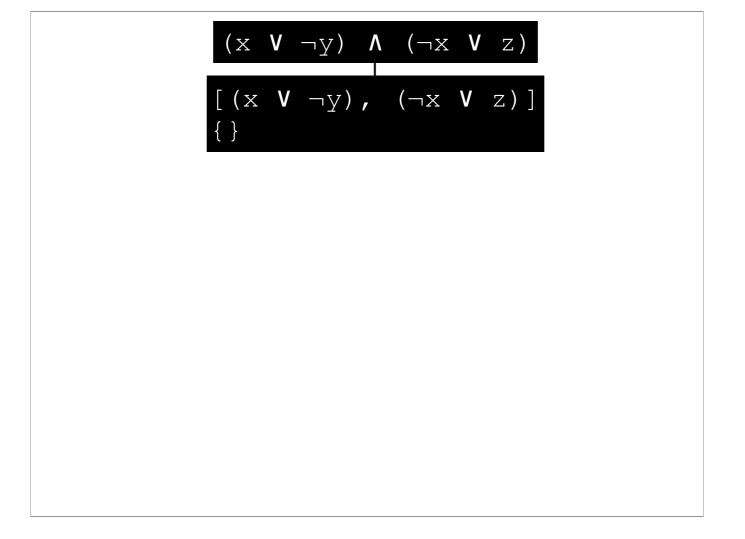


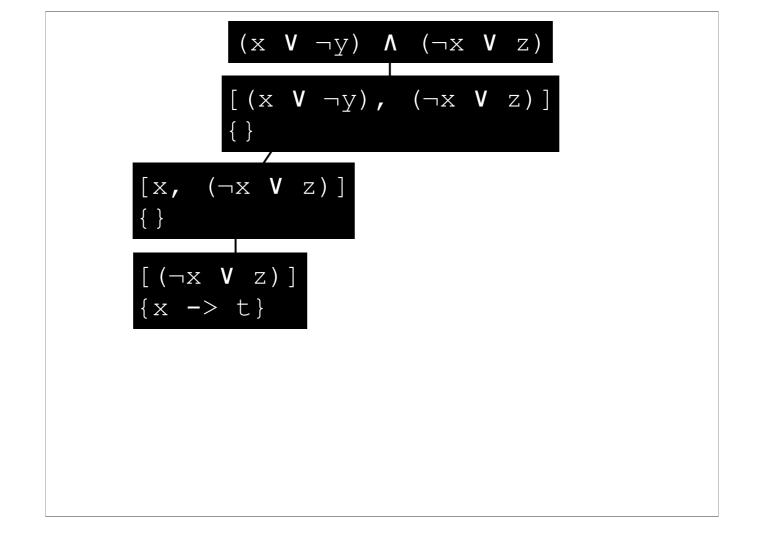


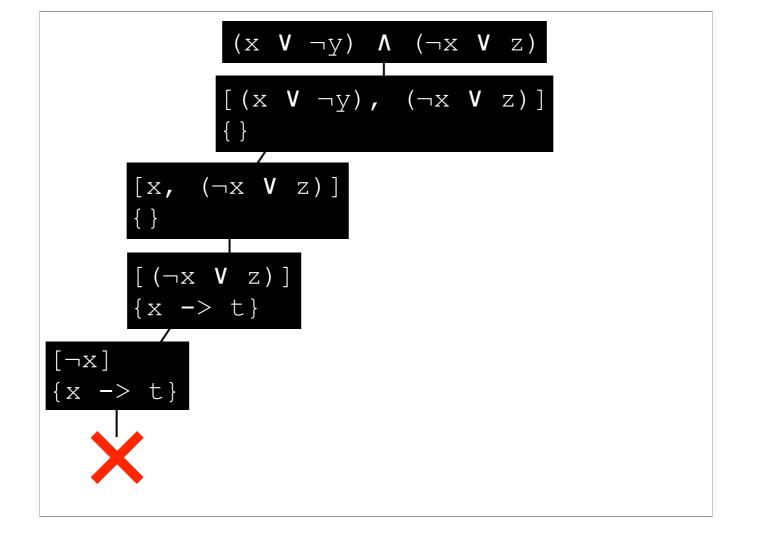
Example 2:

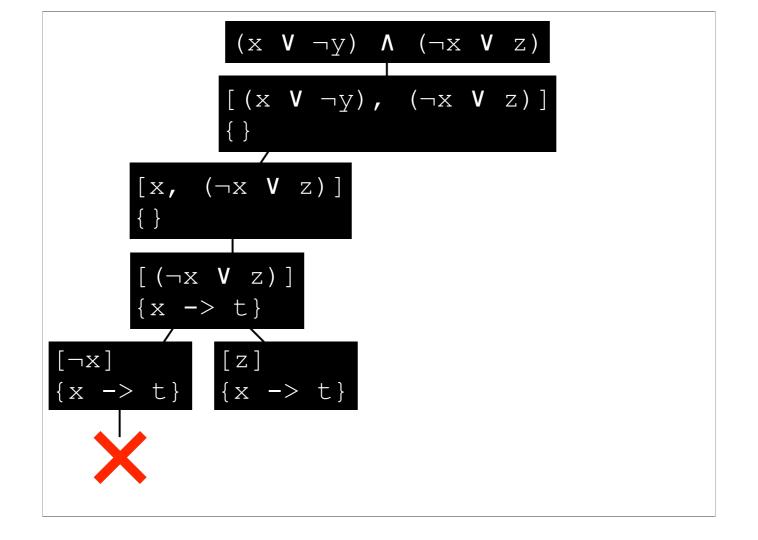
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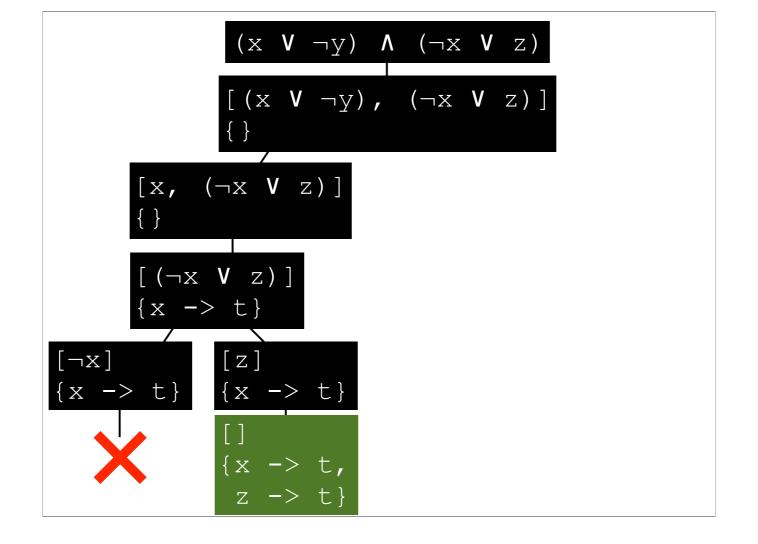
(X	<b>V</b> ¬y)	٨	(¬x	<b>V</b> Z	)	

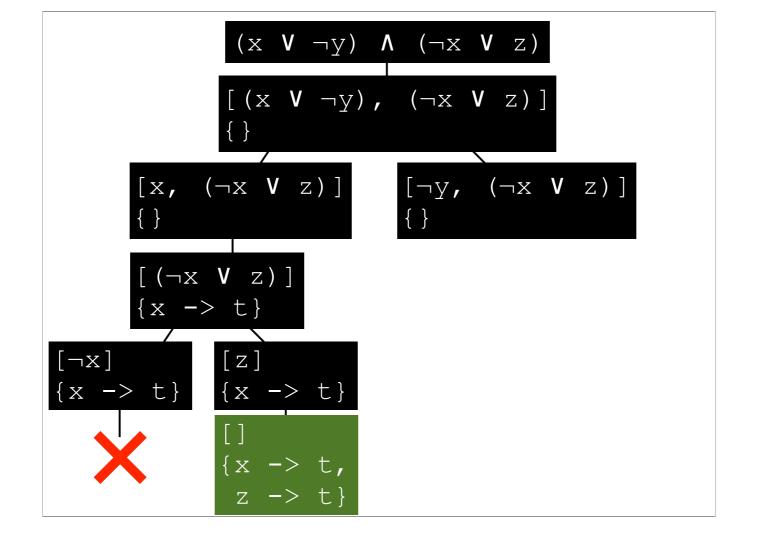


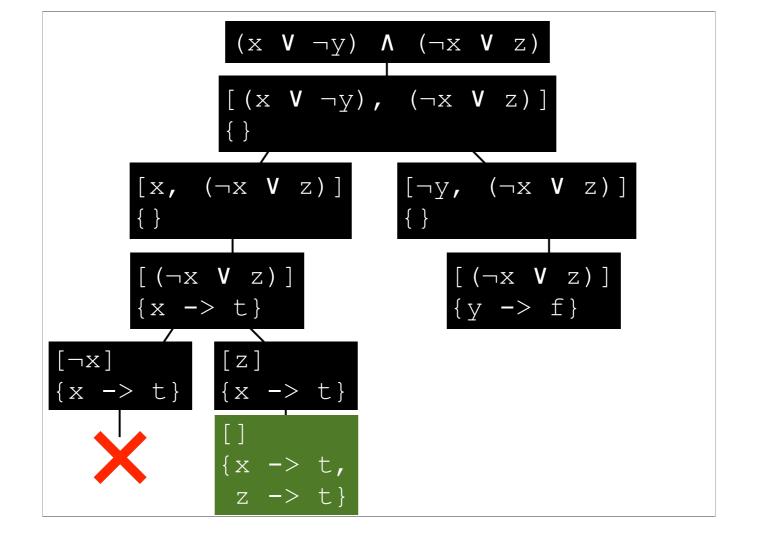


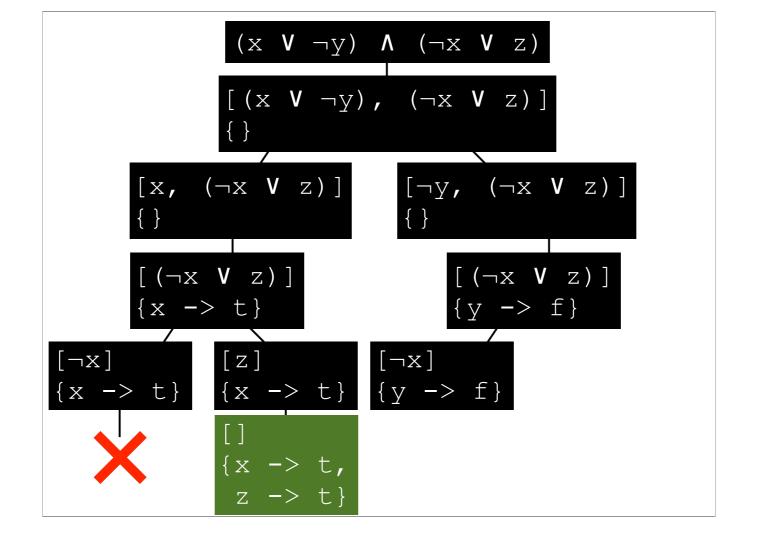


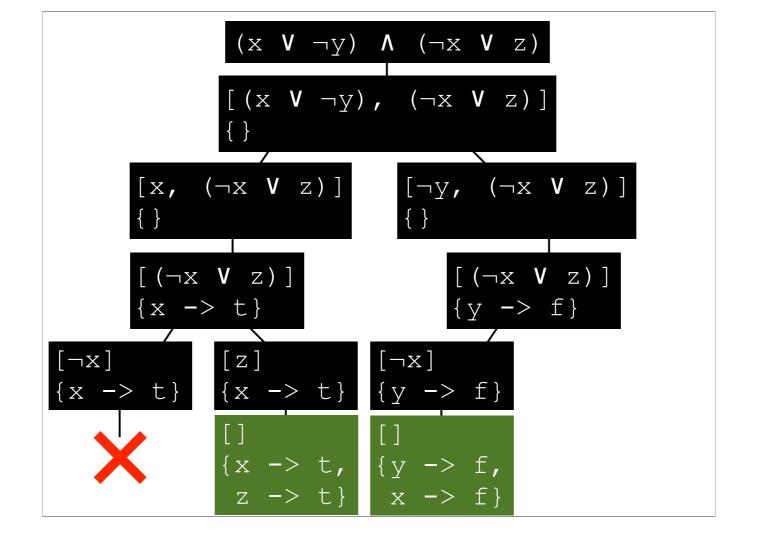


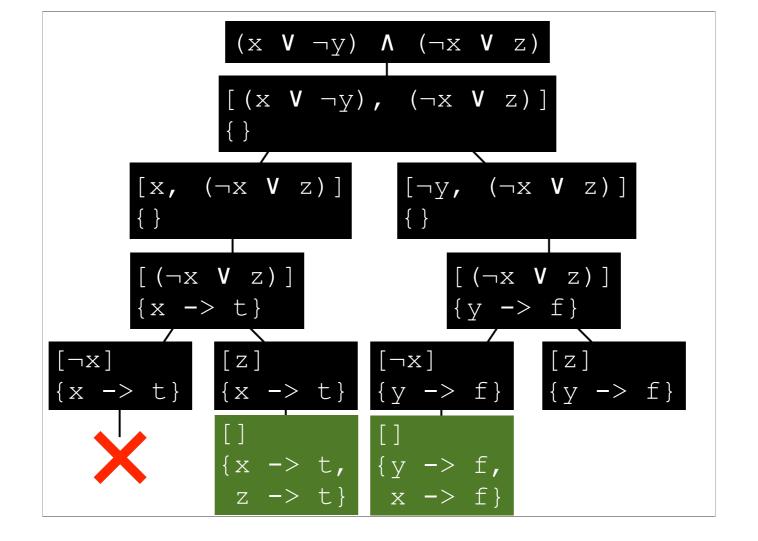


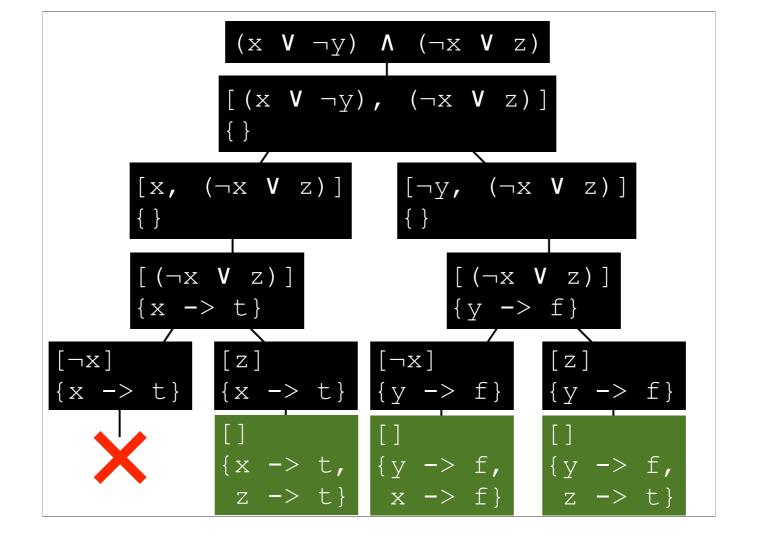












## Exercise: Second Side of SAT Sheet