## COMP 410 Fall 2024 Midterm Practice Exam #2

This is representative of the kinds of topics and kind of questions you may be asked on the midterm. This practice exam, along with assignments 3-6 and the in-class handouts from weeks 4-9, are intended to be comprehensive of everything on the exam. That is, I will not ask anything that's not somehow covered by those sources.

You are permitted to bring two 8.5 x 11 sheets of paper into the exam with you, and these may have anything on them, either printed or handwritten. Both sides of both sheets can be used.

## **Unification with Lists**

Consider each of the following unification attempts involving lists. If the unification succeeds, record any values any variables take. If the unification fails, say so.

1.) 
$$[1, 2, ] = [A, B, C|D]$$

$$2.) A = [1, 2|B], B = [4]$$

3.) 
$$[[A|B], C] = [[1, 2]|D]$$

4.) 
$$X = [A | [2]]$$

6.) Consider the following inductive list definition, which makes use of Prolog atoms and structures:

$$e \in ListElement$$
  $\ell \in List ::= cons(e, \ell) \mid nil$ 

Now consider the following unifications, using Prolog lists. Rewrite these unifications using the above definition.

6.a.) 
$$X = [1, 2, 3]$$

6.b.) 
$$X = [Y | Z]$$

6.c.) 
$$X = [A | [2]]$$

6.d.) 
$$X = [1, [2, [3]]]$$

## Recursion

7.) Consider the following mathematical definition of a recursive function:

$$f_n = \begin{cases} 2 & \text{if } n = 0 \\ 3 & \text{if } n = 1 \\ (3 \times f_{n-1}) + (4 \times f_{n-2}) & \text{otherwise} \end{cases}$$

Write an equivalent definition in Prolog.

8.) Write a procedure named <code>evensBetween</code>, which will nondeterministically produce all the even numbers within an inclusive range. As a hint, a number N is even if and only if the clause 0 <code>is mod(N, 2)</code> is true. An example query is below:

```
?- evensBetween(1, 4, Even).
Even = 2;
Even = 4.
```

9.) Write a procedure named <code>allEqual</code> which will succeed if all list elements are equal to each other according to unification (=). You may introduce any helpers you wish. Example calls are below:

```
?- allEqual([]).
true.
?- allEqual([1, 1, 1]).
true.
?- allEqual([1, 2, 3]).
false.
?- allEqual([1, X, 1]).
X = 1.
?- allEqual([A, B]).
A = B.
?- allEqual([X, 1, 2]).
false.
```

10.) Write a procedure named zip, which takes two lists of the same length, an output list of the same length. The output list is a list of pair structures, where each pair holds an element from each list, preserving order. If the lists are not the same length, zip should fail, though you shouldn't need to explicitly check the length. Example calls are below:

```
?- zip([], [], Output).
Output = [].
?- zip([hello], [goodbye], Output).
Output = [pair(hello, goodbye)].
?- zip([1, 2, 3], [a, b, c], Output).
Output = [pair(1, a), pair(2, b), pair(3, c)].
?- zip([A, B], [C, D], Output).
Output = [pair(A, C), pair(B, D)].
?- zip([foo], [bar, baz], Output).
false.
?- zip([foo, bar], [baz], Output).
false.
```

- 11.) We can represent a binary tree in Prolog using the following:
- leaf: At atom representing a leaf node
- internal (tree, value, tree): A structure recursively containing two trees and some integer value

Write a procedure named sumTree that will compute the sum of all the elements in a given binary tree. Leaf nodes are defined to have a sum of 0. Example queries are shown below:

12.)	Consider	the fo	ollowing	code,	com	puting	the	length	of a	list:

```
len([], 0).
len([_|T], Len) :-
        len(T, TLen),
        Len is TLen + 1.
```

12.a) This procedure is not very efficient when it comes to memory. Why is it inefficient?

12.b) Rewrite this procedure to be more efficient with memory. You may introduce a helper procedure if desired.

13.)	Consider	the	following	code	which	appends	two	lists	together	r:

```
append([], List, List).
append([H|T], List, Result) :-
  append(T, List, Rest),
  Result = [H|Rest].
```

13.a) This procedure is not very efficient when it comes to memory. Why is it inefficient?

13.b) Rewrite this procedure to be more efficient with memory. You may introduce a helper procedure if desired.

14.) Define a procedure named isPrime which will determine if a given input number is prime. You may introduce any helpers you wish. Example queries follow:

```
?- isPrime(2).
true .
?- isPrime(3).
true .
?- isPrime(4).
false.
```

As a hint, the following Java-like code:

```
int x = y % z;
```

...is equivalent to the following Prolog code:

```
X \text{ is } mod(Y, Z)
```

## **Test Case Generation**

15.) Consider the following grammar-based definition of simplistic SQL queries:

$$c \in ColumnName \quad t \in TableName$$
  
 $q \in SQLQuery ::= select \ c \ from \ t;$ 

15.a) Assume the only possible columns are named c1 and c2, and the only possible tables are named t1 and t2. Write a generator of valid SQL query ASTs. An example of a valid AST is select(c1, t1). Do not simply hardcode all possible ASTs.

15.b) Bounds or related mechanisms are not necessary for this problem, at least as described. Why?

15.c) Name a change to this problem which would necessitate adding a bound or a related mechanism, and explain why such a change would add this necessity.

<ol><li>16.) Consider the following gramma</li></ol>	16.)	Consider	the	following	gramma
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```
tree ::= `node(` tree `,` tree `)` | `leaf`
```

16.a.) Write a generator for `tree` below. It's ok if the generator gets "stuck" generating similar values over and over again.

16.b.) Write a modified version of your prior generator, which takes an additional depth bound, and will only generate values that are no deeper than this bound.