COMP 410 Lecture I

Kyle Dewey

About Me

- I research automated testing techniques and their intersection with CS education
- My dissertation used logic programming extensively
- This is my second semester at CSUN
- First time dedicating a whole course to logic programming

About this Class

- See something wrong? Want something improved? Email me about it! (kyle.dewey@csun.edu)
- I generally operate based on feedback

Bad Feedback

- This guy sucks.
- This class is boring.
- This material is useless.

-I can't do anything in response to this

Good Feedback

- This guy sucks, I can't read his writing.
- This class is boring, it's way too slow.
- This material is useless, I don't see how it relates to anything in reality.
- I can't fix anything if I don't know what's wrong

-I can actually do something about this!

-Major programming paradigm - a way of thinking about problems -Emphases thinking about exactly _what_ the problem is, as opposed to exactly _how_ to solve it. This is called declarative programming.

-For example: it's generally easier to say what constraints must hold for a valid Sudoku solution, as opposed to directly finding a valid Sudoku solution.

-Somewhat related to functional programming – we generally lack mutable state -Unlike any other major paradigm, the distinction between inputs and outputs is intentionally blurred. You can take advantage of this.

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Programming, programming, programming

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- Thinking in a logic programming way

- Programming, programming, programming
- Thinking in a logic programming way
- Applying logic programming without a logic programming language

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- Thinking in a logic programming way
- Applying logic programming without a logic programming language
- Little bit of theory later on

• Artificial intelligence

-"Artificial intelligence" used to refer to search techniques, which is relevant to logic programming. Now the term largely refers to machine learning. What it means is a moving target.

-Machine learning (we won't do any sort of statistics)

-You can spend a career on the theory behind this stuff. I know some, but it's not my speciality.

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Syllabus

Outline

- Abstract Syntax Trees and evaluation
- SAT and Semantic Tableau

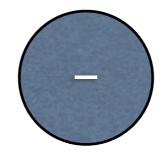
Abstract Syntax Trees and Evaluation

Abstract Syntax Tree

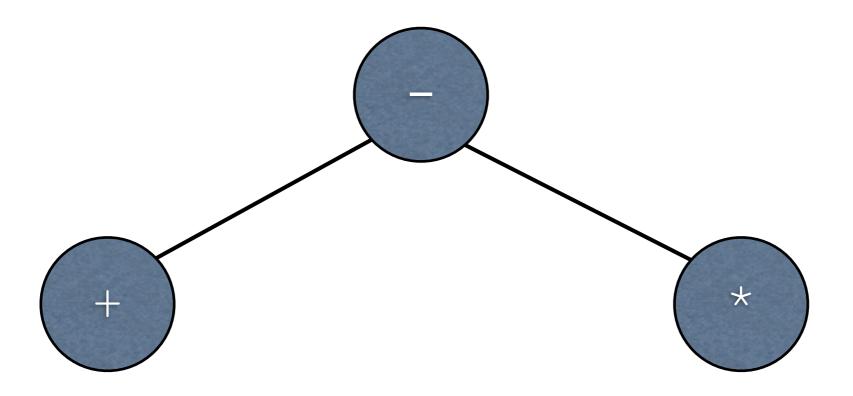
- Abbreviation:AST
- Unambiguous tree-based representation of a sentence in a language
- Very commonly used in compilers, interpreters, and related software

-Generally we work with ASTs instead of Strings or any other code representation

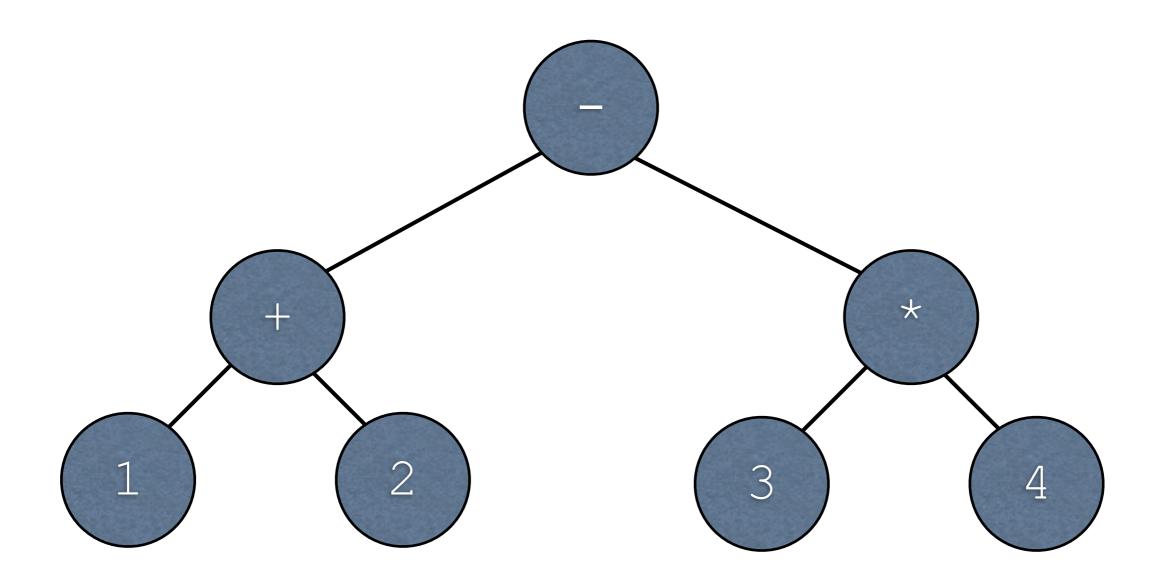
-Key parts: we need parentheses to direct that 1 + 2 happens first. We know that the 3 * 4 should happen after the part in parentheses from PEMDAS rules



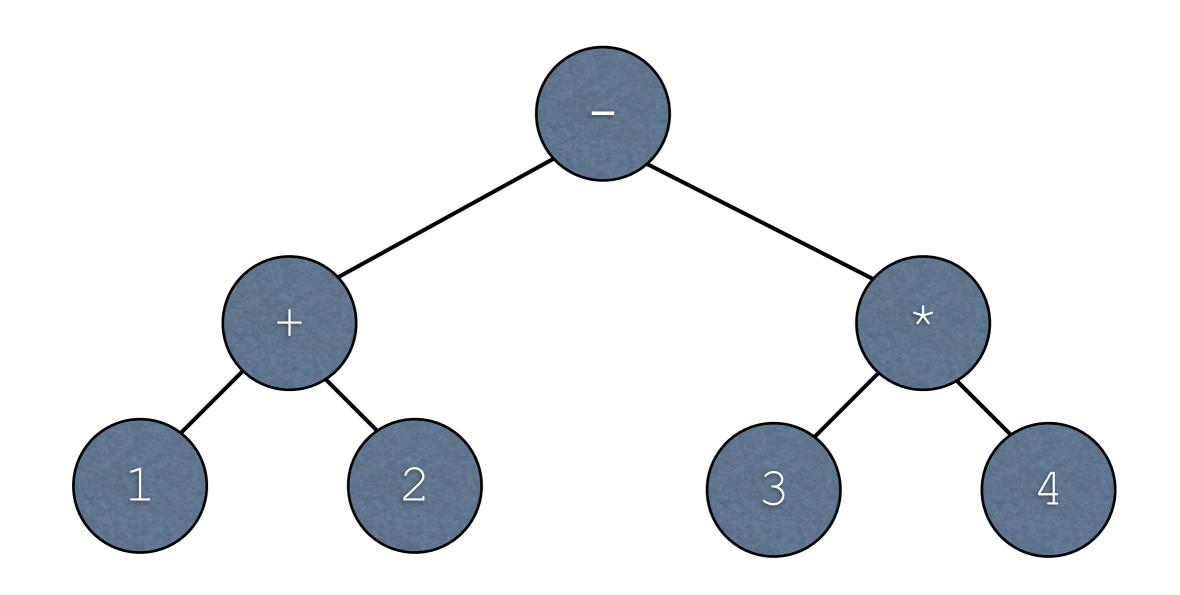
-Lowest priority thing ends up in the top of the tree



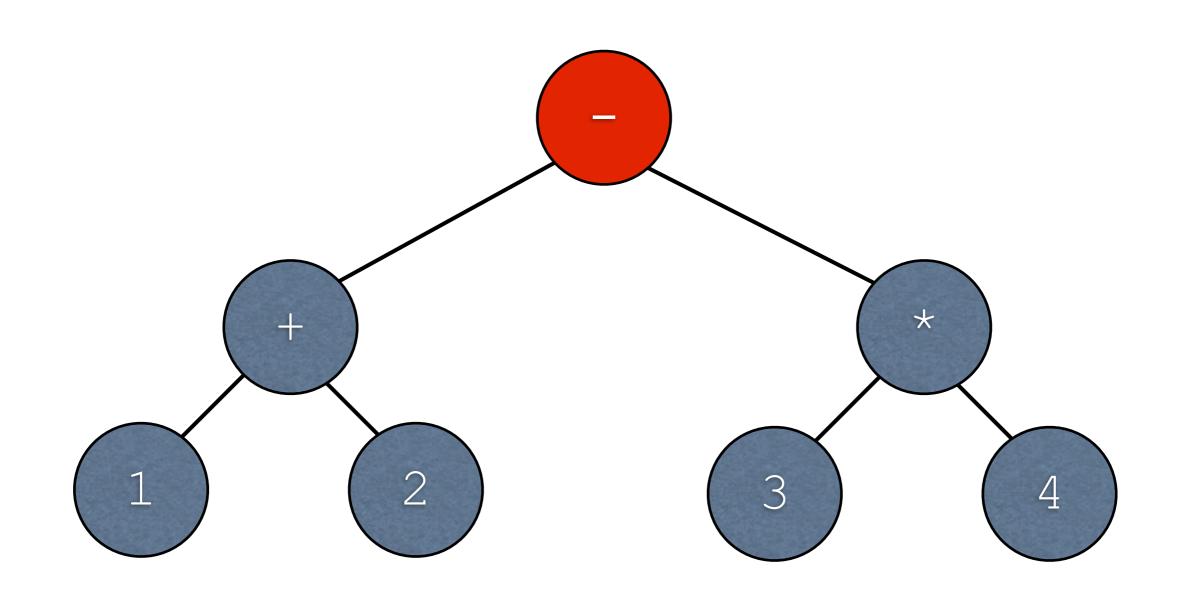
-Next level of priority



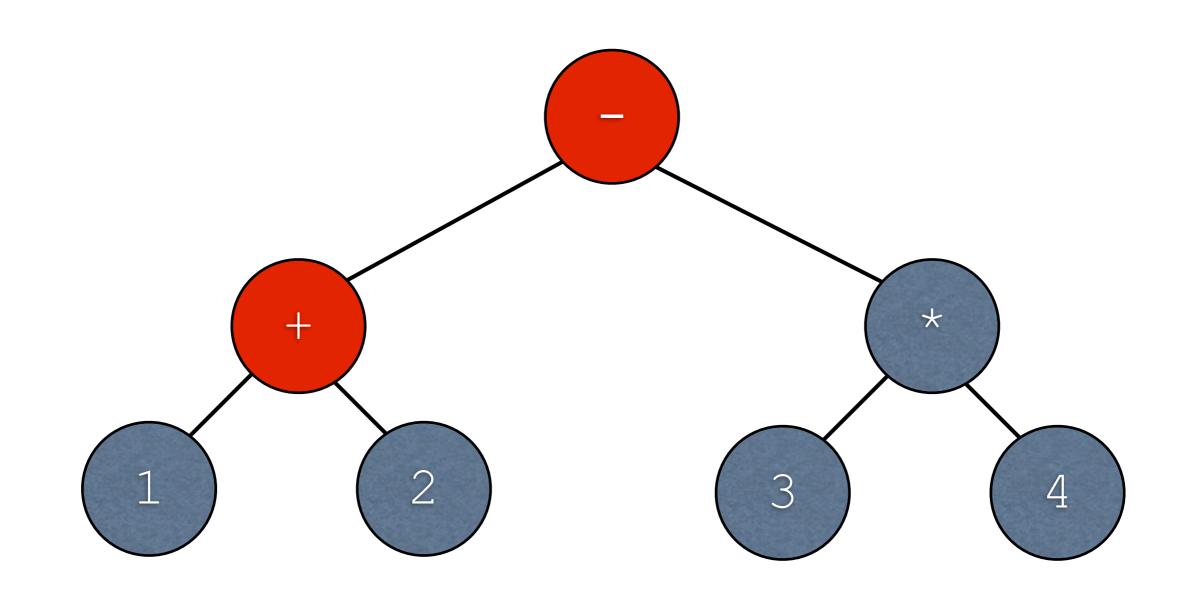
-Next level of priority



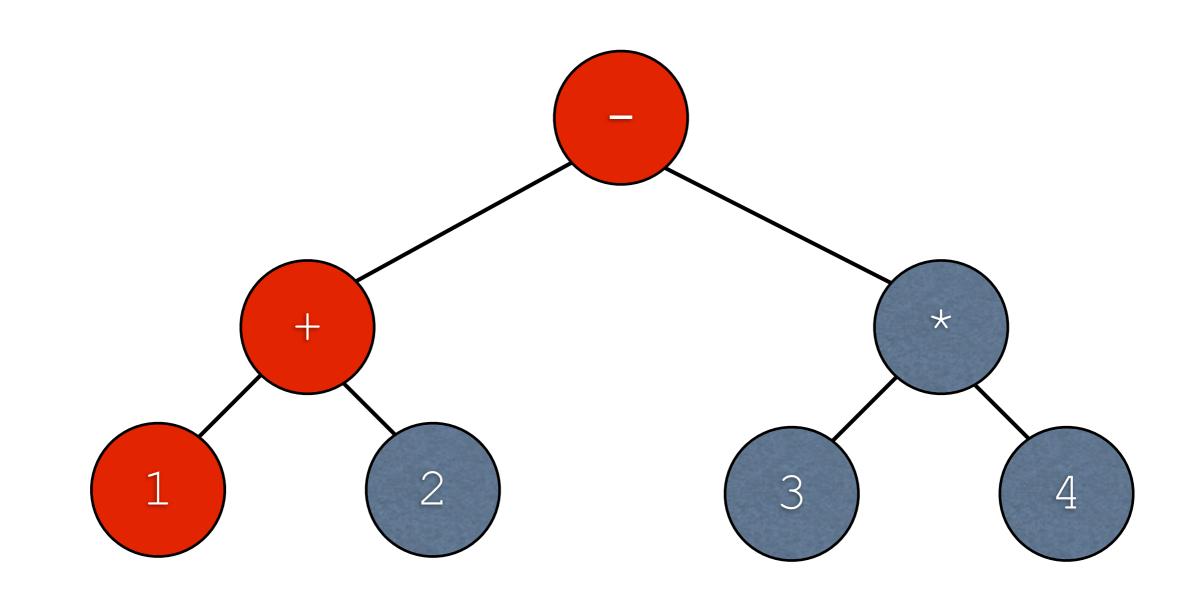
-Key point: bubble-up values from the leaves -This can be implemented in code via a recursive function starting from the root (code in a bit later)



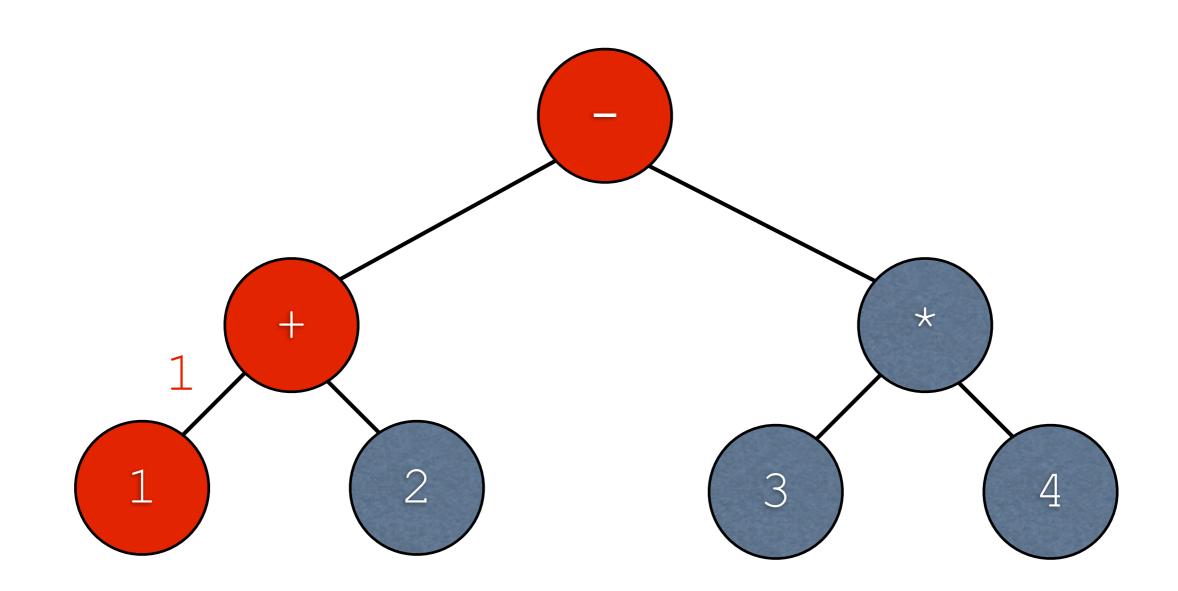
-We start evaluation from the root...



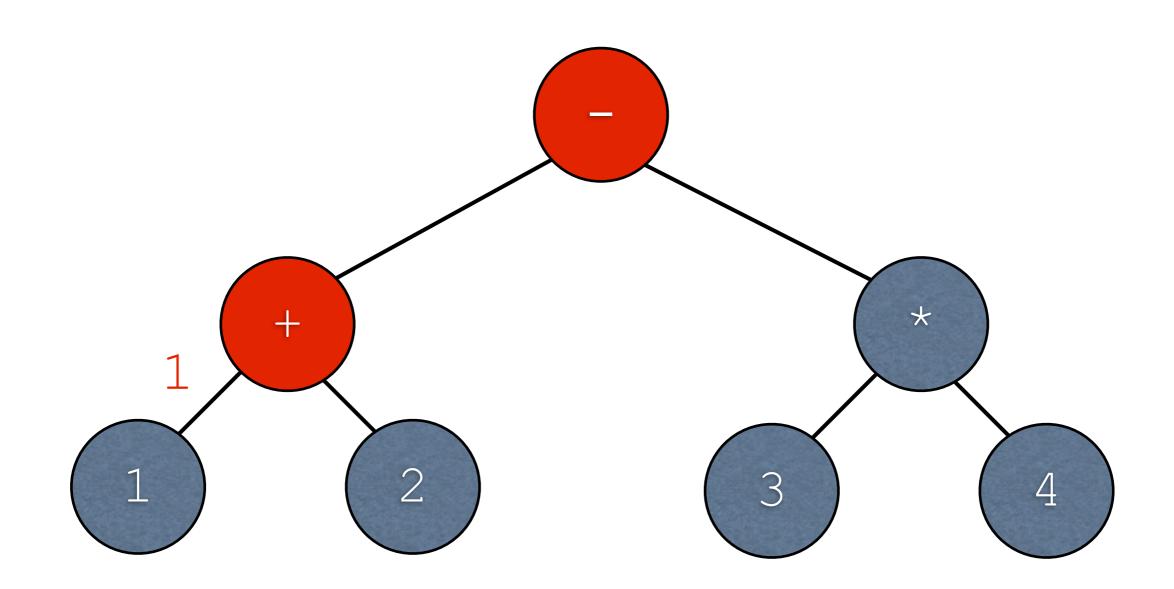
-In order to evaluate the root, we need to evaluate the left subtree of the root (+)



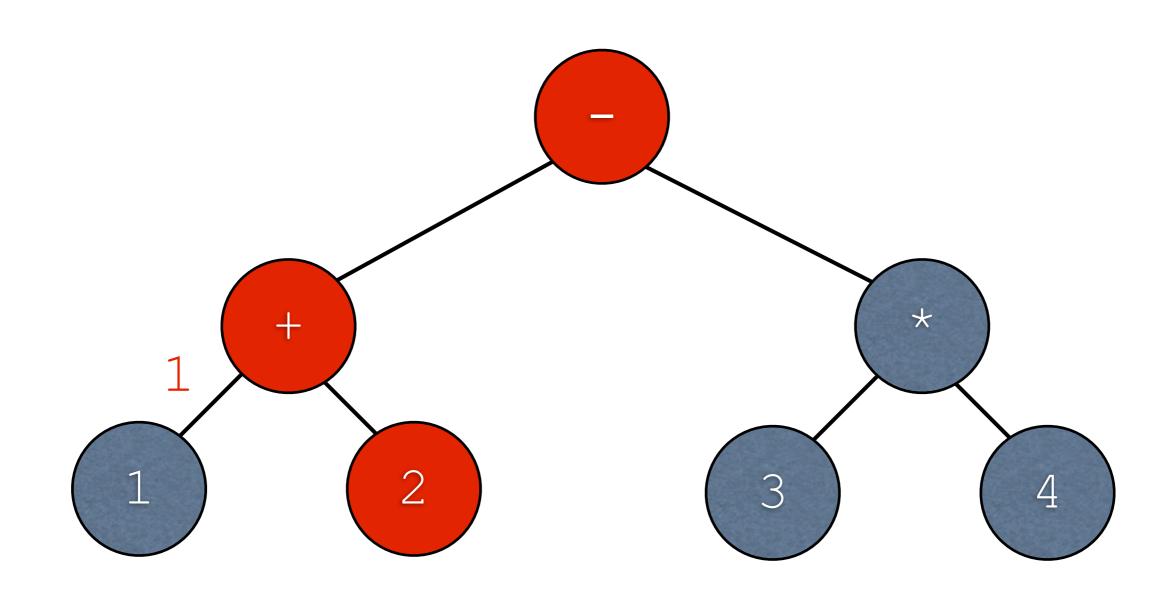
-In order to evaluate +, we need to evaluate the left subtree (as with the root)



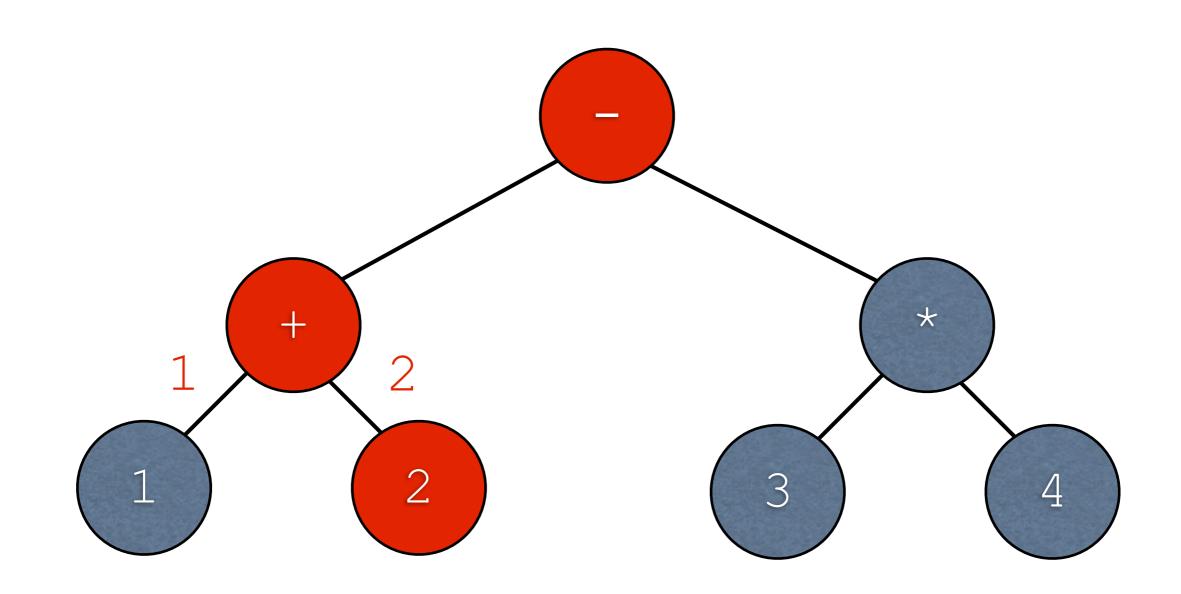
-For arithmetic, leaves are simply numbers -Evaluating a leaf returns the number held within



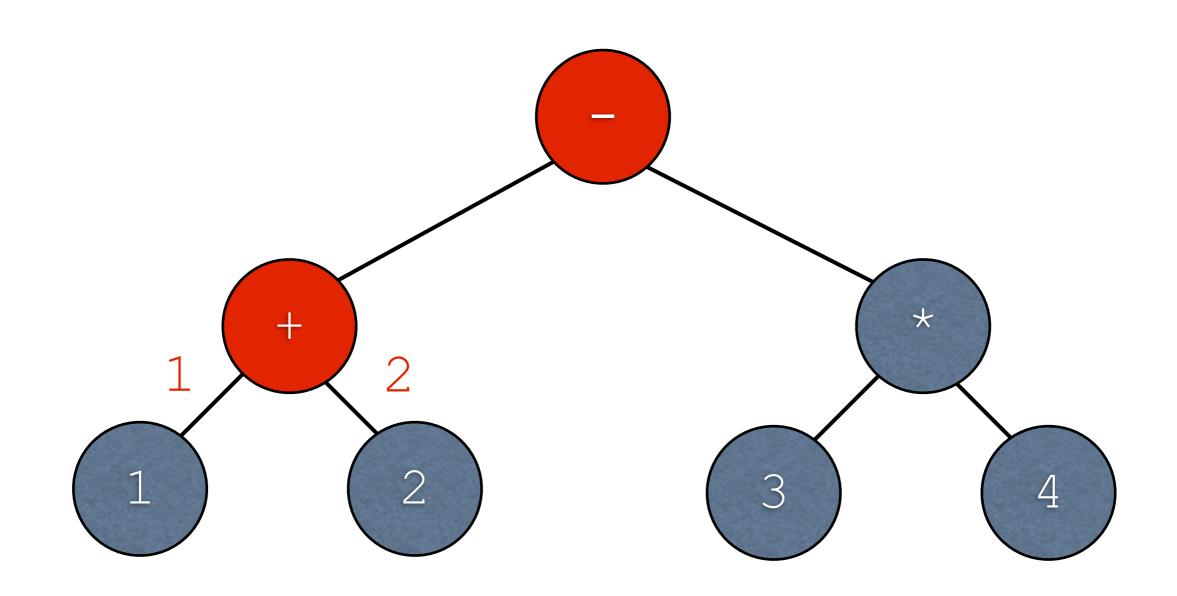
-The left subtree of + has now been evaluated -Now + needs the value of the right subtree



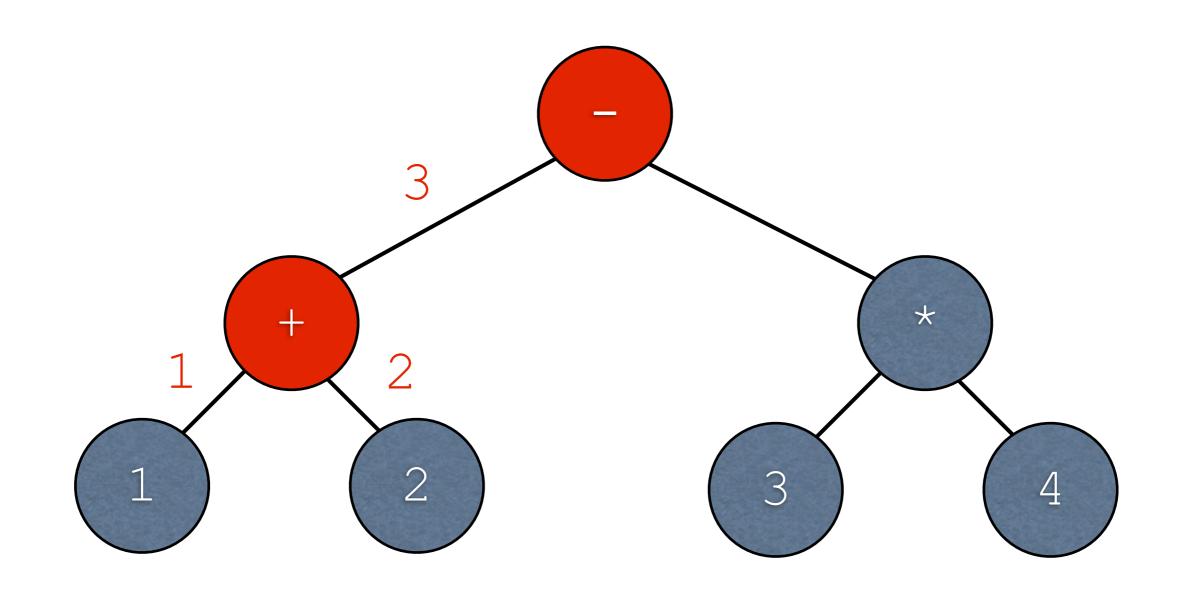
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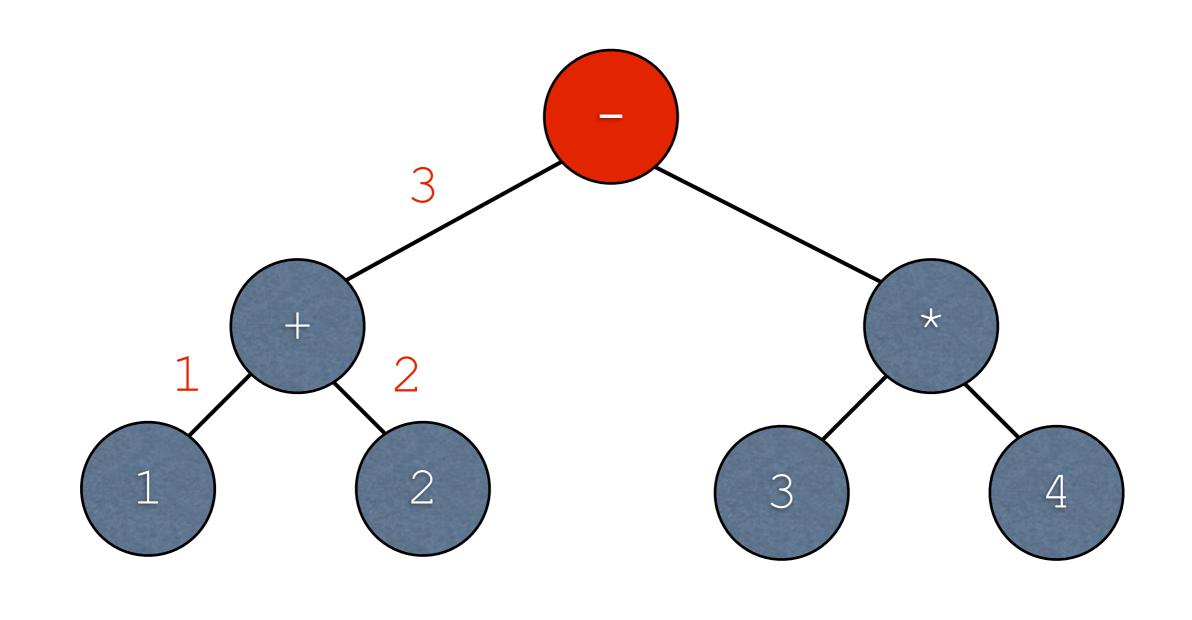
-As before, leaves just return the value held within



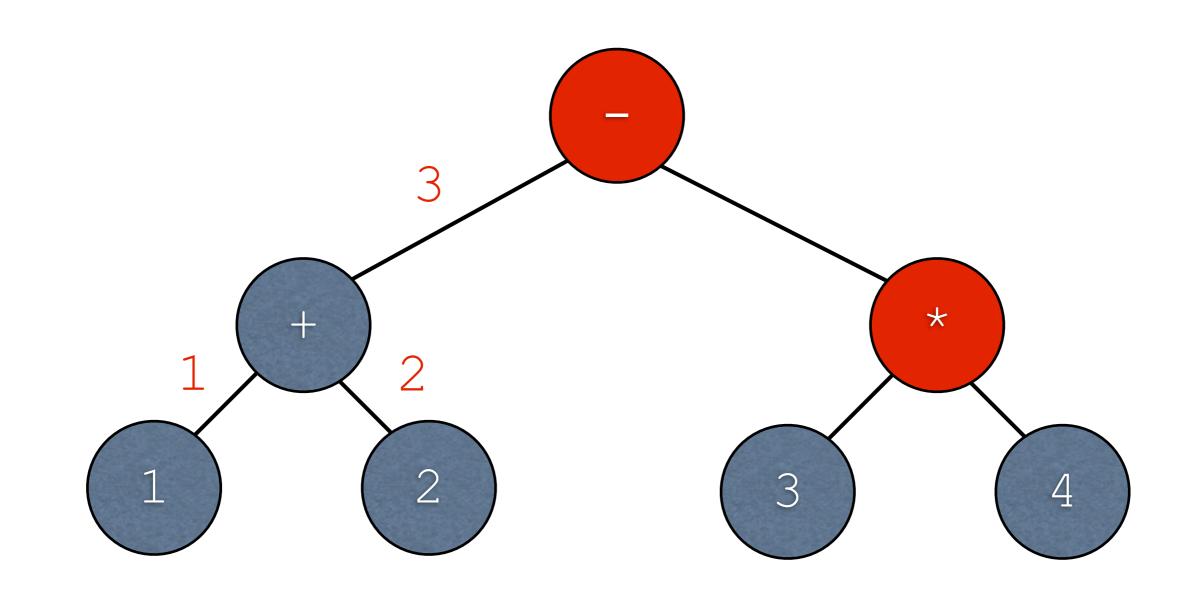
-Subtrees of + are now taken care of -Now + has two values that it needs to work with...



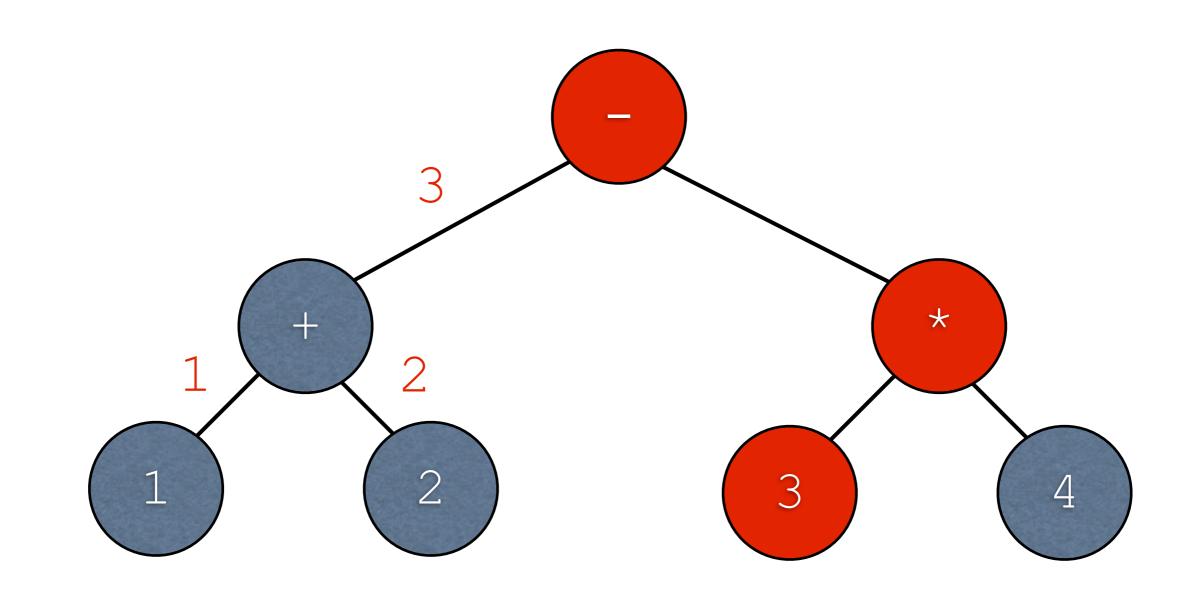
-+ performs the actual addition



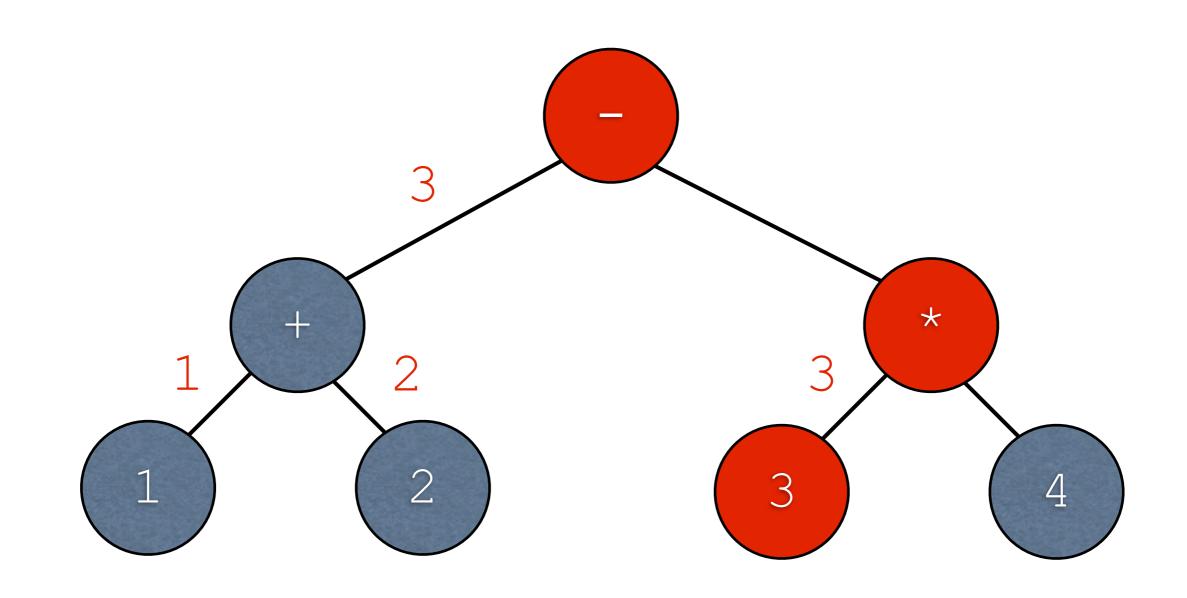
-Now + is taken care of -Going back to -, - now has the value of the left subtree, and it needs the value of the right subtree



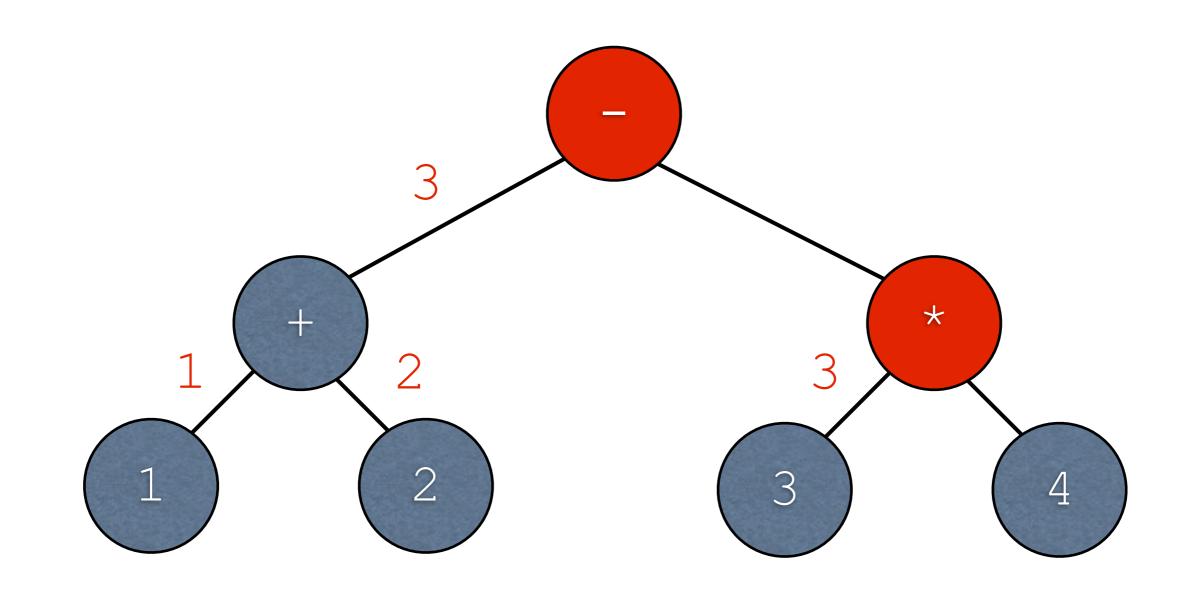
-Now we're on *, which needs the value of the left subtree...



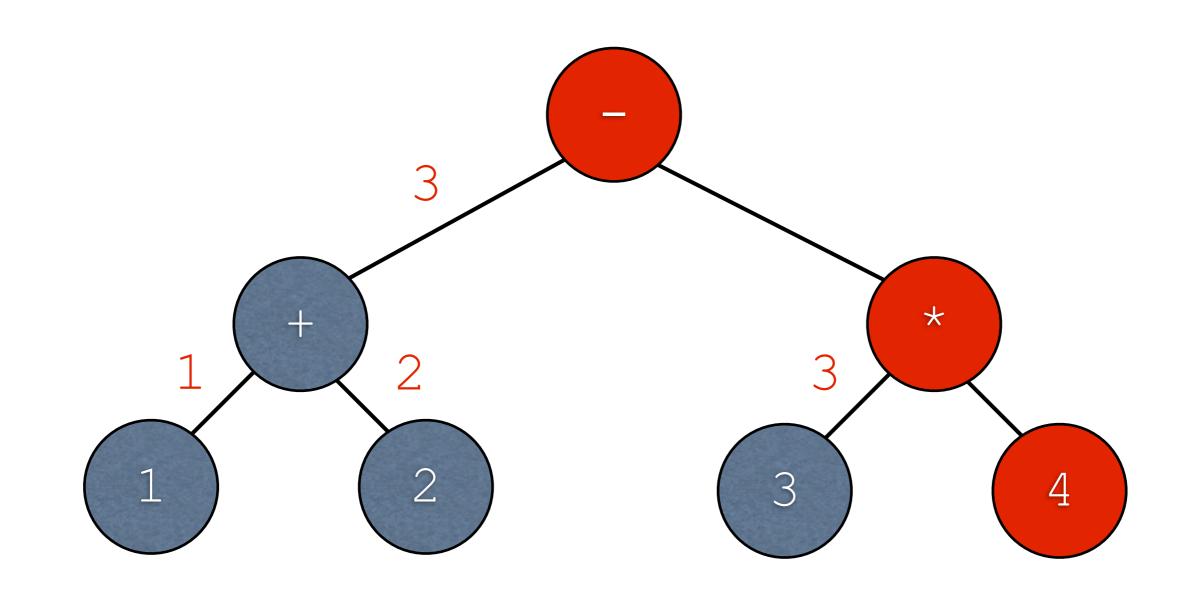
-Now we're on *, which needs the value of the left subtree...



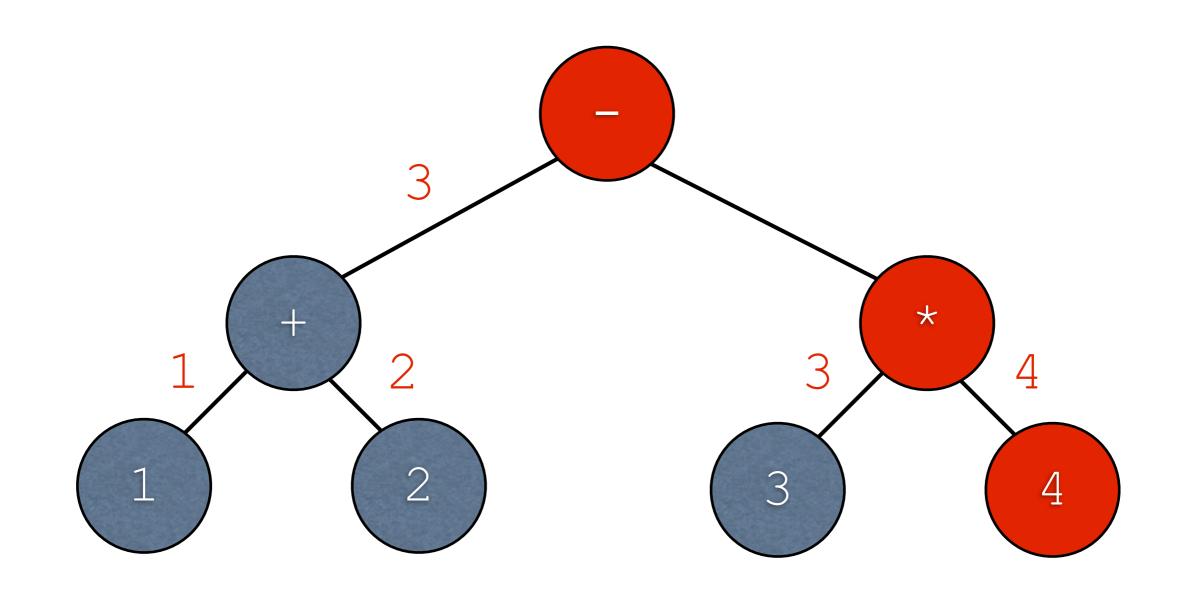
-Leaves again return the values held within...



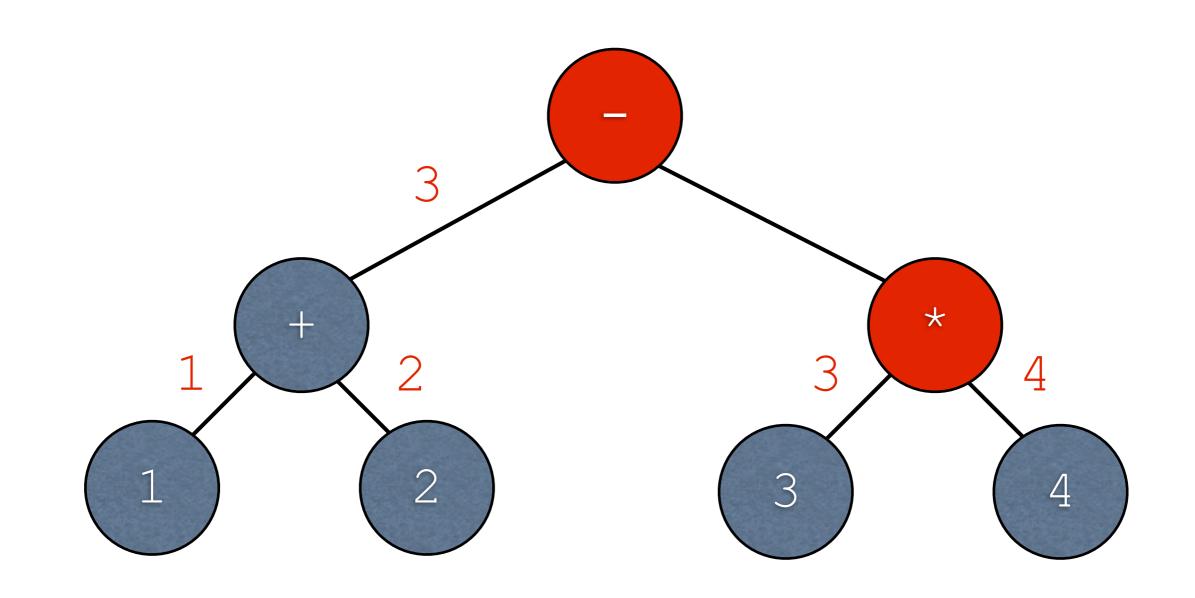
-Left subtree done; * now needs the value of the right subtree...



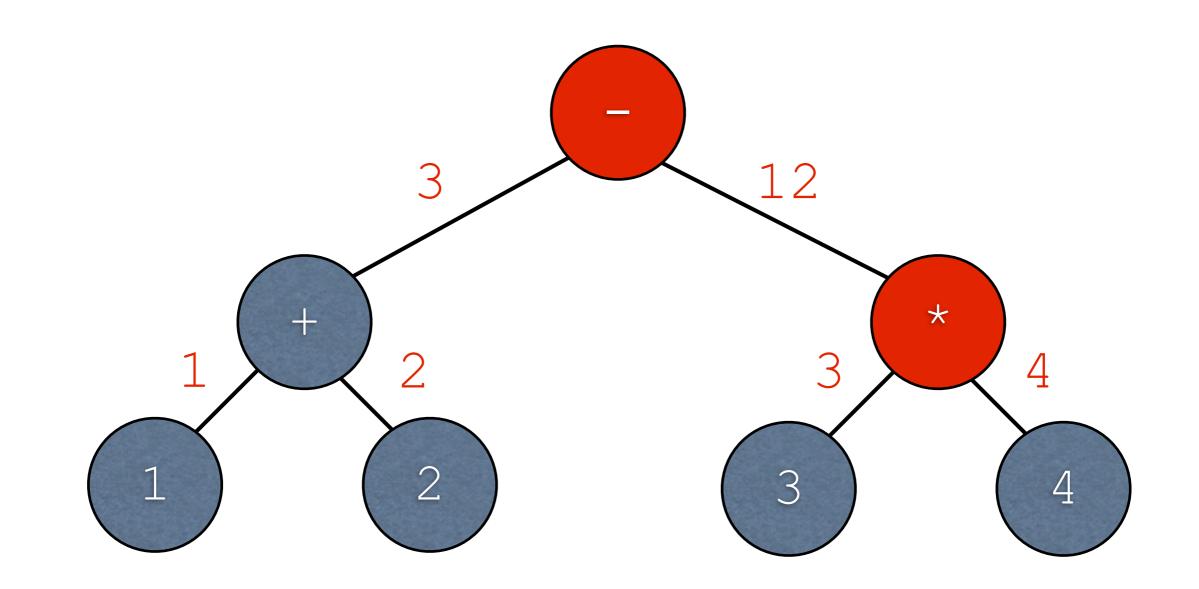
-Left subtree done; * now needs the value of the right subtree...



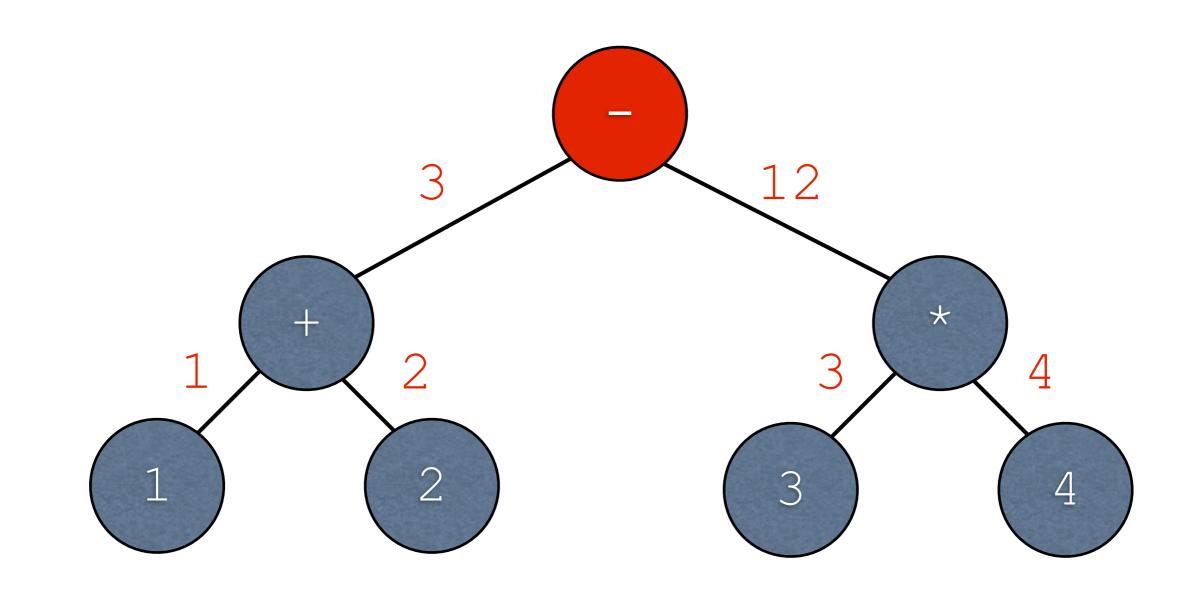
-Leaf returns value held within



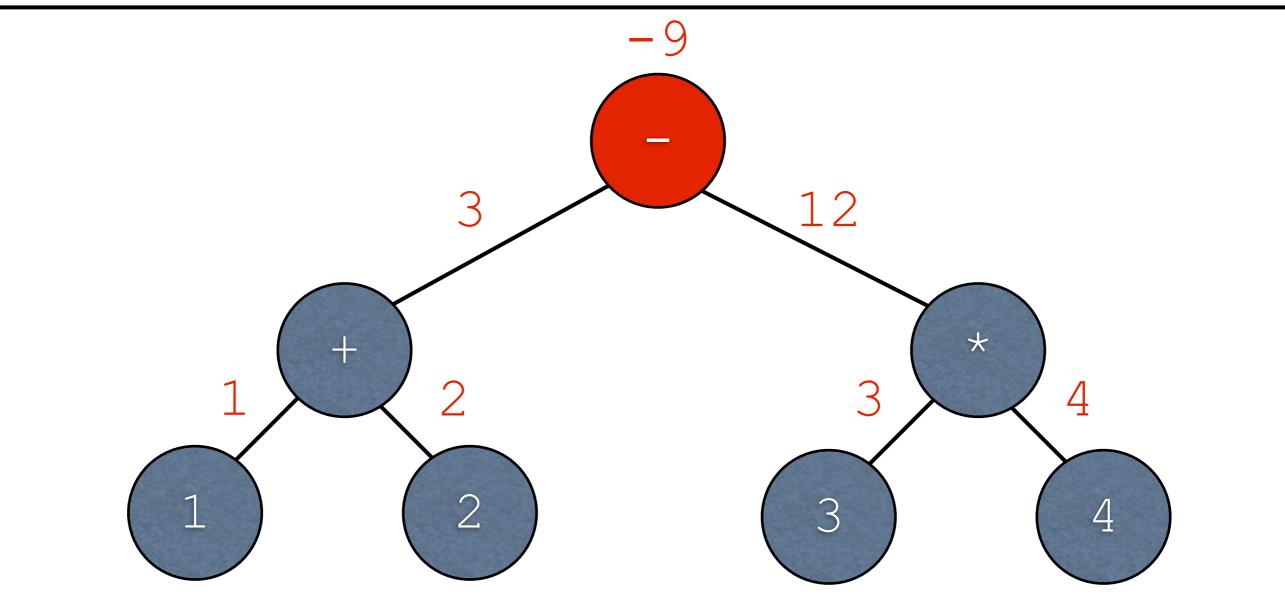
-Leaf is done. * now has both operands it needs...



-* performs the multiplication and returns the value



-The root - node now has both operands...



-...and it returns the result of the subtraction

Evaluator Example: arithmetic_evaluator.rkt

-Complete example online; we'll live-code this in class

SAT and Semantic Tableau

SAT Background

- Short for the Boolean satisfiability problem
- Given a Boolean formula with variables, is there an assignment of true/false to the variables which makes the formula true?

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Yes: x is true, z is true

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$$(X \land \neg X)$$

- Short for the Boolean satisfiability problem
- Given a Boolean formula with variables, is there an assignment of true/false to the variables which makes the formula true?

$$(x \ V \ \neg y) \ \land \ (\neg x \ V \ z)$$

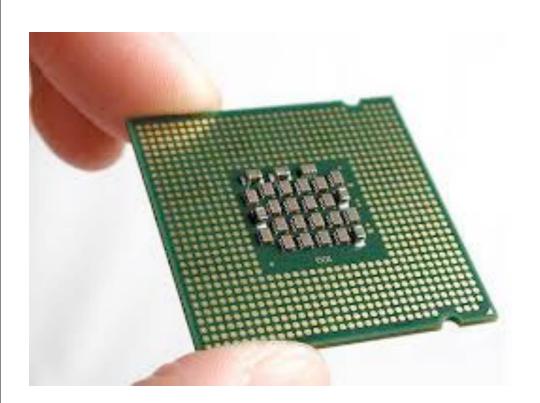
Yes: x is true, z is true
$$(x \ \land \ \neg x)$$

No

Widespread usage in hardware and software verification

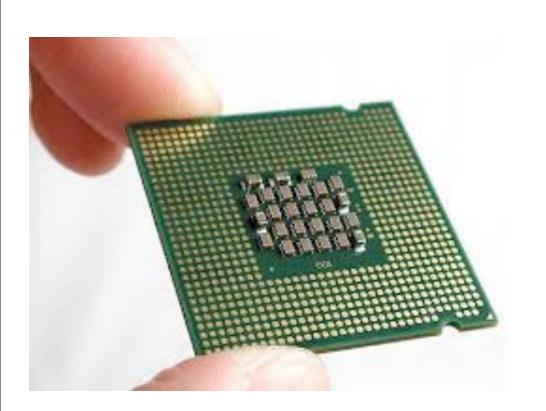
-Verification as in _proving_ the system does what we intend -Much stronger guarantees than testing -Testing can prove the existence of a bug (a failed test), whereas verification proves the absence of bugs (relative to the theorems proven)

Widespread usage in hardware and software verification



-Circuits can be represented as Boolean formulas -Can basically phrase proofs as Circuit ^ BadThing. If unsatisfiable, then BadThing cannot occur. If satisfiable, then the solution gives the circumstance under which BadThing occurs. -Many details omitted (entire careers are based on this stuff)

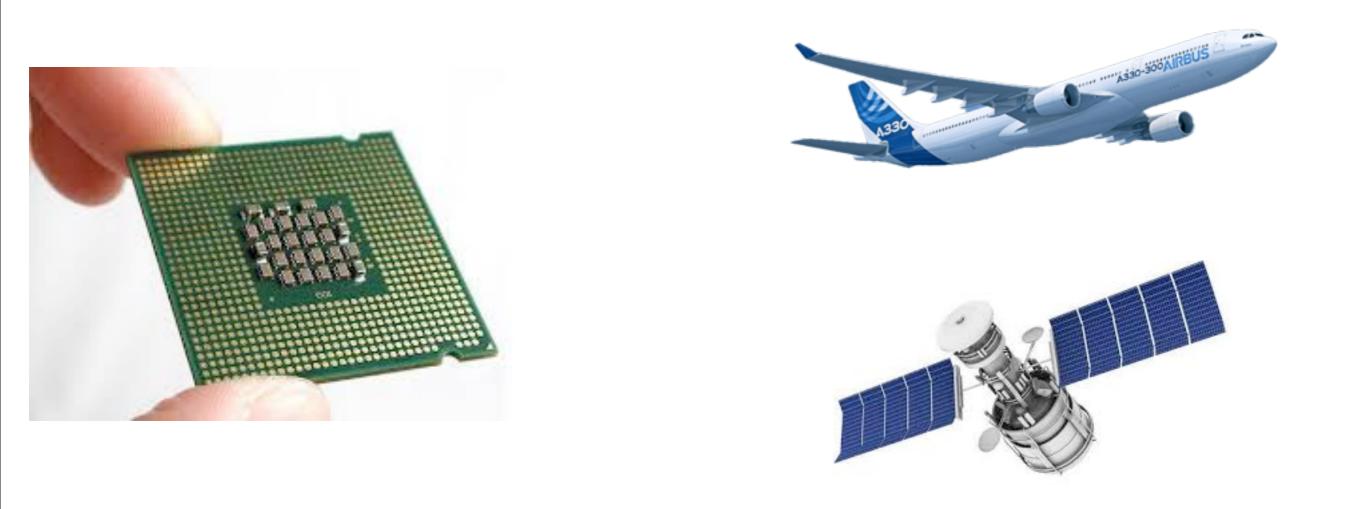
Widespread usage in hardware and software verification





-(Likely) used by AirBus to verify that flight control software does the right thing -Lots of proprietary details so it's not 100% clear how this verification works, but SAT is still relevant to the problem

Widespread usage in hardware and software verification



-Nasa uses software verification for a variety of tasks; SAT is relevant, though other techniques are used, too

Relevance to Logic Programming

- Methods for solving SAT can be used to execute logic programs
- Logic programming can be phrased as SAT with some additional stuff

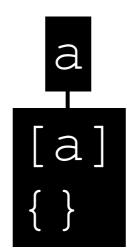
Semantic Tableau

- One method for solving SAT instances
- Basic idea: iterate over the formula
 - Maintain subformulas that must be true
 - Learn which variables must be true/false
 - Stop at conflicts (unsatisfiable), or when no subformulas remain (have solution)

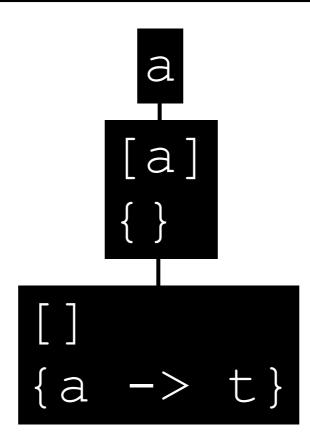
-There are many methods to this



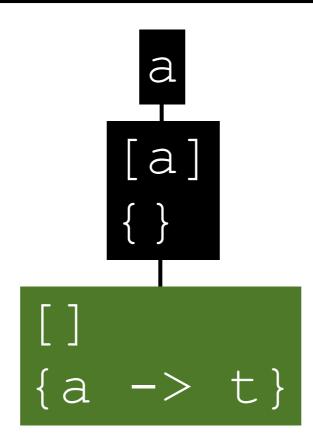
-As in, the input formula is simply "a"



-One subformula must be true: a -Initially, we don't know what any variables must map to



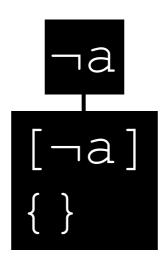
-For formula "a" to be true, it must be the case that a is true



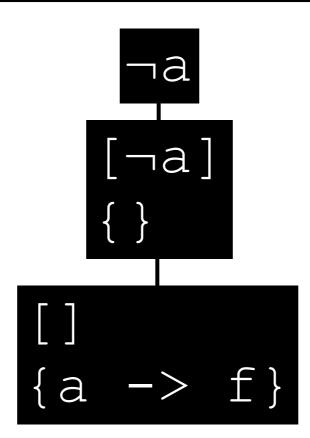
-No subformulas remain, so we are done. The satisfying solution is that a must be true.



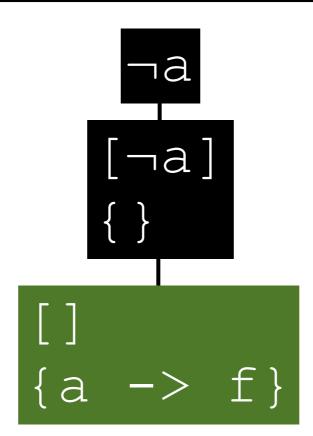
-As in, the input formula is simply "¬a"



-One subformula must be true: ¬a -Initially, we don't know what any variables must map to



-For subformula " \neg a" to be true, it must be the case that a is false

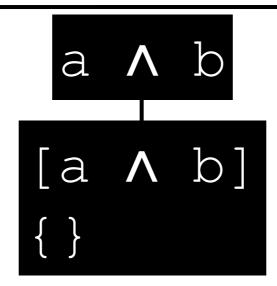


-No subformulas remain, so we are done. The satisfying solution is that "a" must be false.

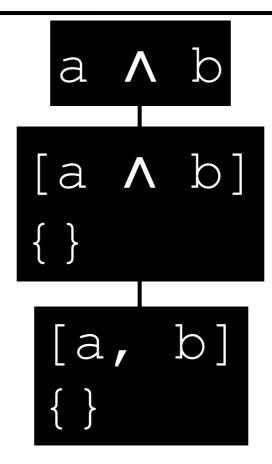
Logical And



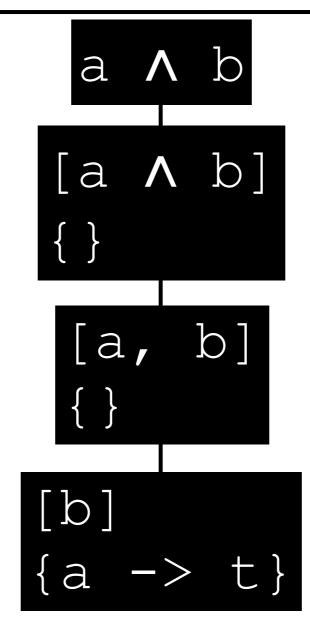
Logical And



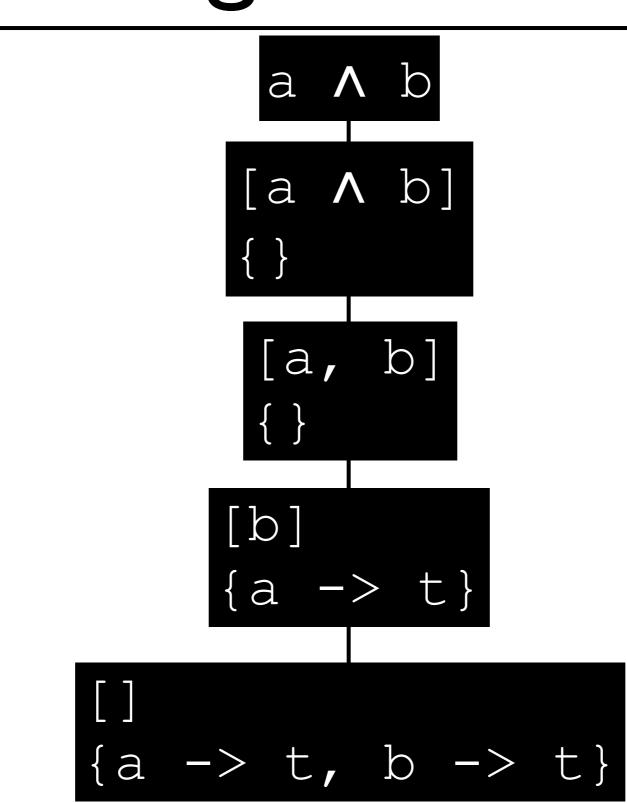
-Initially, one subformula must be true: $a \land b$ -Initially, we don't know what any variable must map to



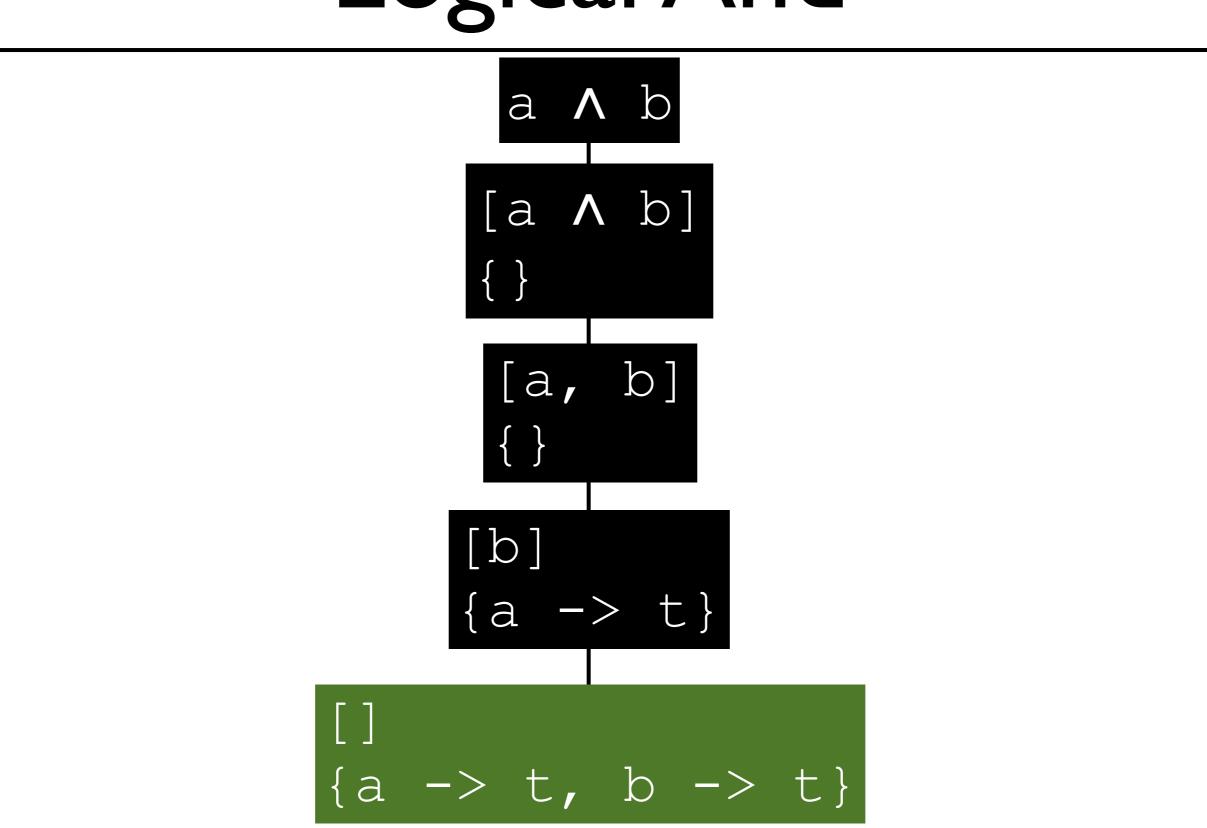
-For a \wedge b to be true, subformulas a and b must both be true



-From the positive literal case, for formula a to be true, variable a must be true



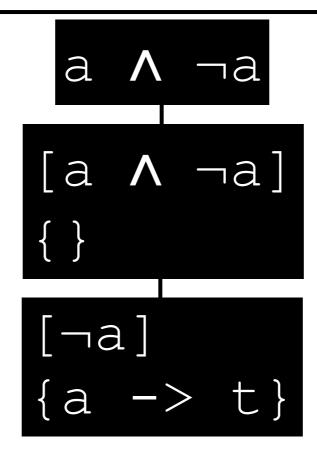
-From the positive literal case, for formula b to be true, variable b must be true

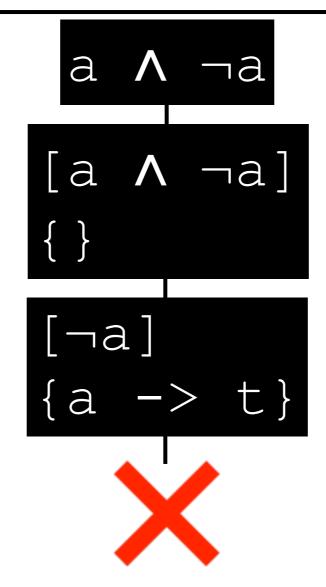


-No subformulas remain, so we are done with the solution that both a and b must be true



-Alternative example, showing a conflict



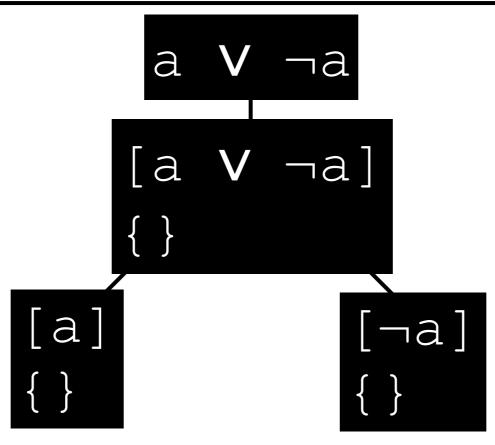


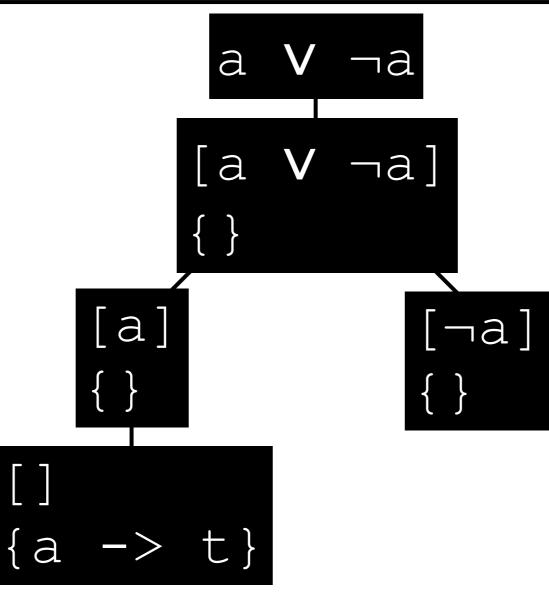
-Now we have a problem: for formula $\neg a$ to be true, it must be the case that variable a is false

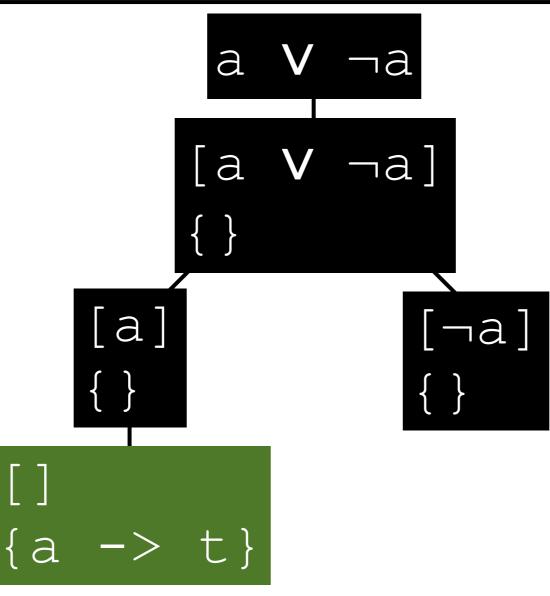
-We've already recorded that variable a must be true, which is the opposite of what we expect.

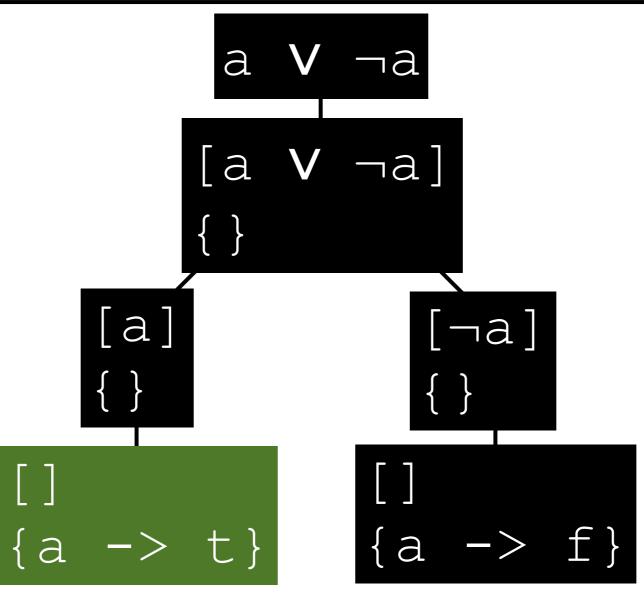
-As such, we have a conflict - this formula is unsatisfiable

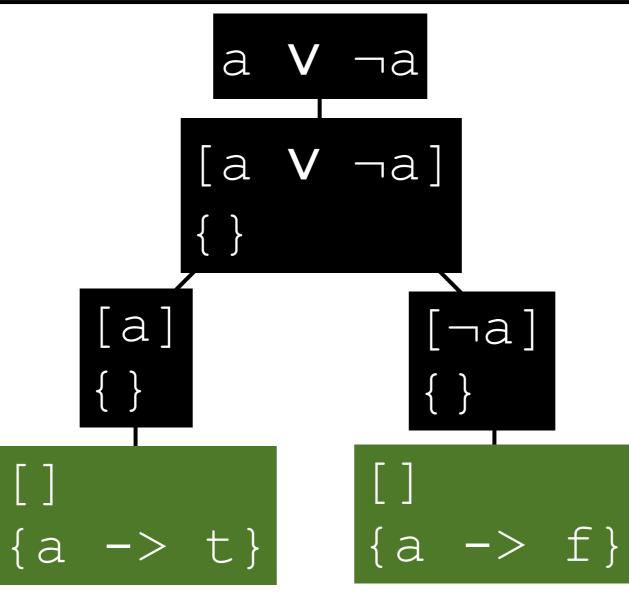








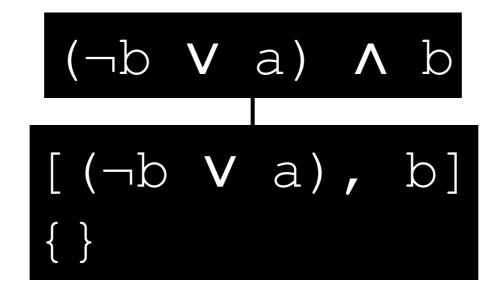


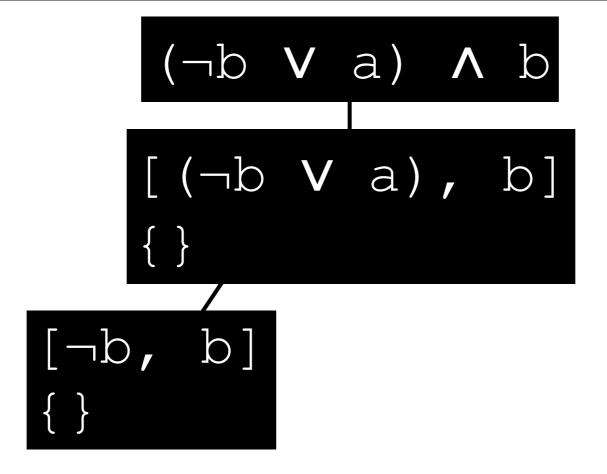


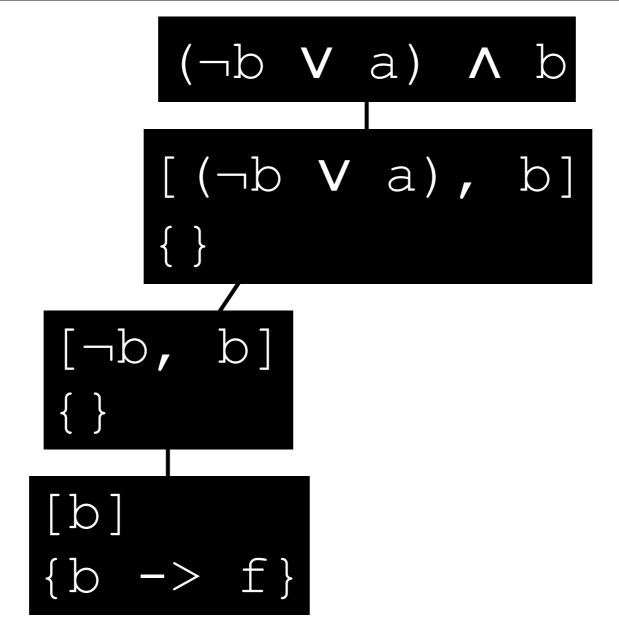
Examples

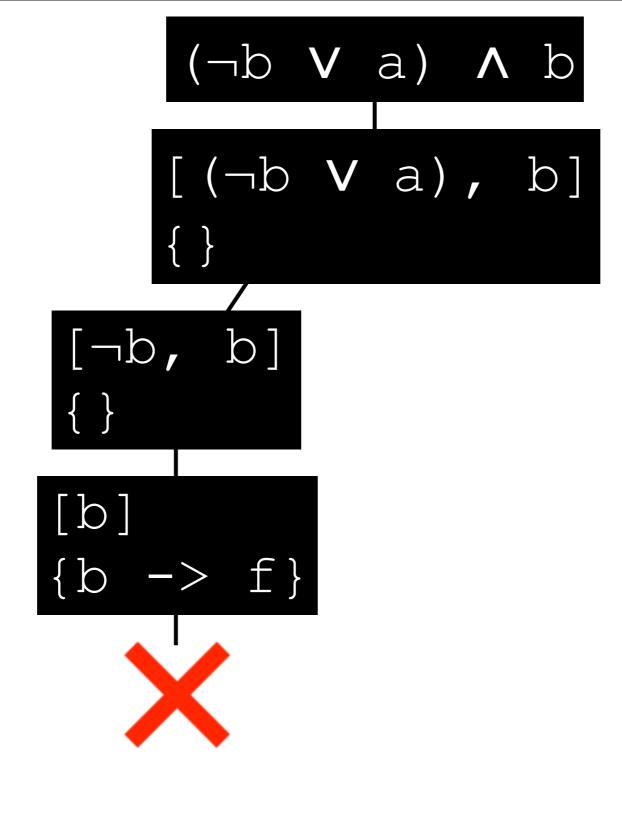
Example I: $(\neg b V a) \land b$

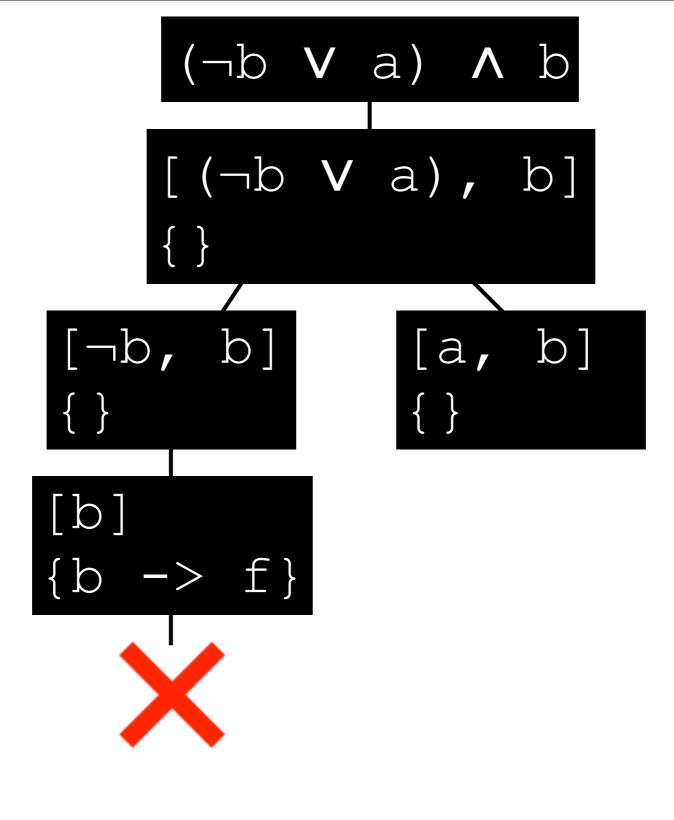


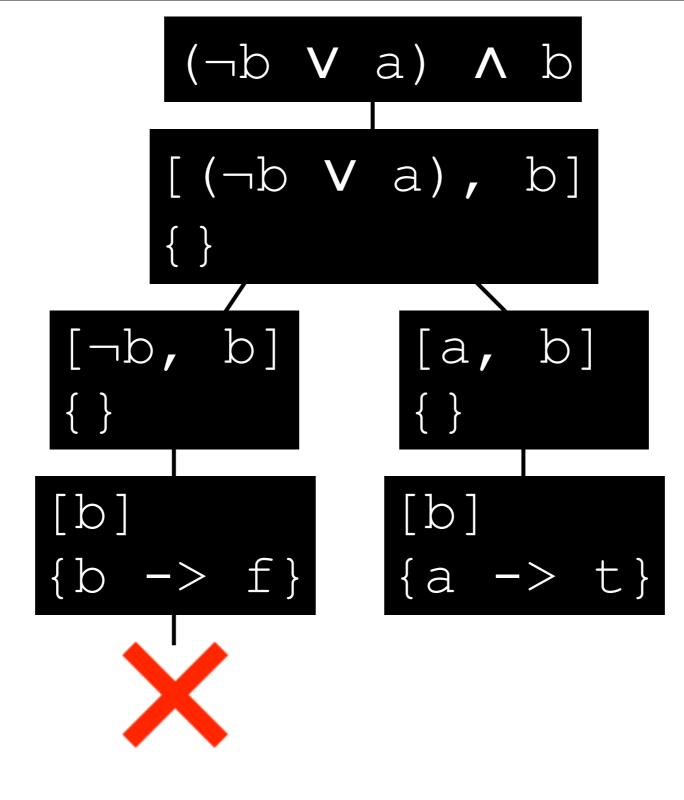


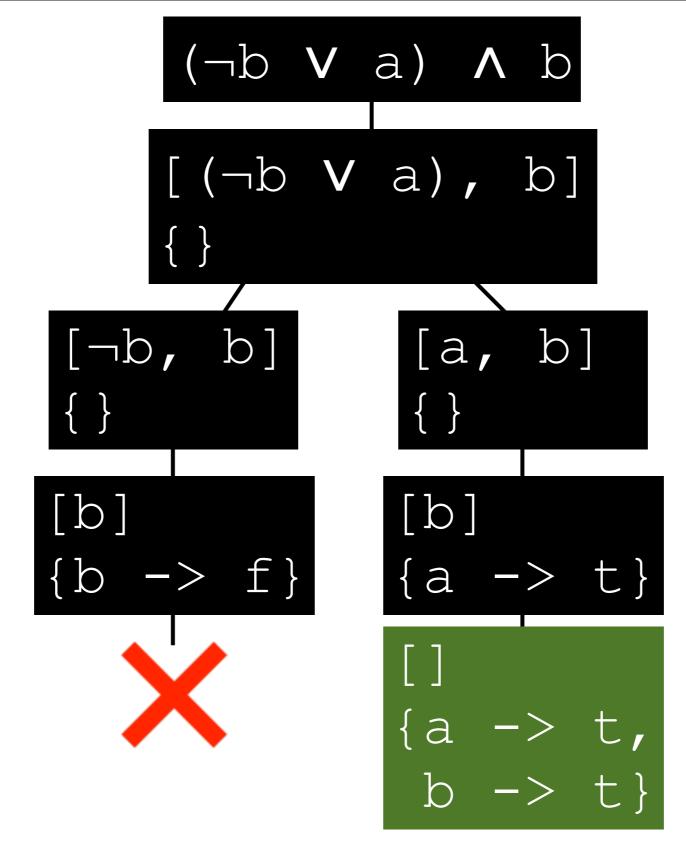












Example 2: (x V \neg y) \land (\neg x V z)

 $(x V \neg y) \land (\neg x V z)$

 $(X V \neg Y) \land (\neg X V Z)$ $[(X V \neg Y), (\neg X V Z)]$ { }

$$(x \lor \neg y) \land (\neg x \lor z)$$

$$[(x \lor \neg y), (\neg x \lor z)]$$

$$\{\}$$

$$[x, (\neg x \lor z)]$$

$$\{$$

$$[(\neg x \lor z)]$$

$$\{x \rightarrow t\}$$

