

COMP 410
Summer 2025
Midterm Practice Exam #1

This is representative of the kinds of topics and kind of questions you may be asked on the midterm. This practice exam, along with assignments 1-3 and the first 5 in-class worksheets (everything through Recursive Procedures), are intended to be comprehensive of everything on the exam. That is, I will not ask anything that's not somehow covered by those sources.

You are permitted to bring two 8.5 x 11 sheets of paper into the exam with you, and these may have anything on them, either printed or handwritten. Both sides of both sheets can be used.

Abstract Syntax Trees

In Boolean expressions, \neg has the highest precedence, followed by \wedge and \vee . With this in mind, write out the ASTs corresponding to each of the following Boolean expressions:

1.) $\neg a \wedge b \vee c$

2.) $(a \vee b) \wedge c$

3.) $\neg (a \wedge b) \wedge (b \vee c)$

Arithmetic expressions can be used to form Boolean expressions with the help of arithmetic comparisons (e.g., $<$, \leq , $>$, \geq , $==$). These comparisons have the lowest possible precedence. With this in mind, write out the ASTs corresponding to each of the following expressions:

4.) $1 * 2 + 3 == 4$

$$5.) (2 + 2 < 4) \wedge \neg a$$

6.) Consider the following Python class definitions, which are adapted from assignment 1's boolean evaluator. These classes are used to represent AST nodes.

```
class And:
    def __init__(self, left, right):
        self.left = left
        self.right = right
```

```
class Or:
    def __init__(self, left, right):
        self.left = left
        self.right = right
```

Assume that Boolean true is represented as an AST with Python's `True`, and Boolean false is represented as an AST with Python's `False`. With all this in mind, represent the following Boolean expressions in Python using `And`, `Or`, `True`, and `False` as appropriate.

6.a) `true ∧ false`

6.b.) `false ∨ true`

6.c.) `false ∧ true ∨ true`

6.d.) `false ∨ true ∧ true`

Semantic Tableau

For each of the following Boolean formulas, write out the complete semantic tableau tree. **Circle** the nodes in the tree representing solutions. If a tree has no solutions, say so. **Be sure to write all steps.**

7.) $\neg a \wedge a$

8.) $(a \vee \neg a) \wedge a$

9.) $(\neg x \wedge \neg y) \vee (x \wedge y)$

Prolog - Modeling the World

10.a)

For this problem, you need to write a clause database encapsulating pricing information for a convenience store. Write Prolog code accurately reflecting the following:

- Soda costs \$2
- Chips cost \$3
- Hot dogs cost twice as much as soda (do not hardcode \$4)
- Soda chips, and hot dogs are food
- Pencils and pens are office supplies
- All office supplies cost \$2
- Cold medicine costs \$7

Using the clause database you previously wrote, write queries to determine the following:

10.b.) Which items cost exactly \$2?

10.c.) Which items cost more than \$3?

10.d.) Which foods cost less than \$3?

10.e.) Which foods are also office supplies?

Unification

Consider each of the following unification attempts. If the unification succeeds, record any values any variables take. If the unification fails, say so.

11.) $\text{foo}(1, X) = \text{foo}(Y, 2)$

12.) $\text{foo}(1, X) = \text{foo}(X, 2)$

13.) $\text{foo}(1, _) = \text{foo}(X, 2)$

14.) $\text{foo}(1, _) = \text{foo}(1, _)$

15.) $\text{foo}(1, 2, \text{bar}) = \text{foo}(X, _, _, _)$

16.) $\text{foo}(\text{bar}(\text{baz}), X) = \text{foo}(Y, Z), Y = \text{bar}(A)$

Recursion

17.) Consider the following mathematical definition of a recursive function:

$$f_n = \begin{cases} 2 & \text{if } n = 0 \\ 3 & \text{if } n = 1 \\ (3 \times f_{n-1}) + (4 \times f_{n-2}) & \text{otherwise} \end{cases}$$

Write an equivalent definition in Prolog.

18.) Write a procedure named `evensBetween`, which will nondeterministically produce all the even numbers within an inclusive range. As a hint, a number `N` is even if and only if the clause `0 is mod(N, 2)` is true. An example query is below:

```
?- evensBetween(1, 4, Even).  
Even = 2 ;  
Even = 4.
```

19.) Define a procedure named `isPrime` which will determine if a given input number is prime. You may introduce any helpers you wish. Example queries follow:

```
?- isPrime(2).  
true .  
?- isPrime(3).  
true .  
?- isPrime(4).  
false.
```

As a hint, the following Java-like code:

```
int x = y % z;
```

...is equivalent to the following Prolog code:

```
X is mod(Y, Z)
```