

# CS 162 Week 8

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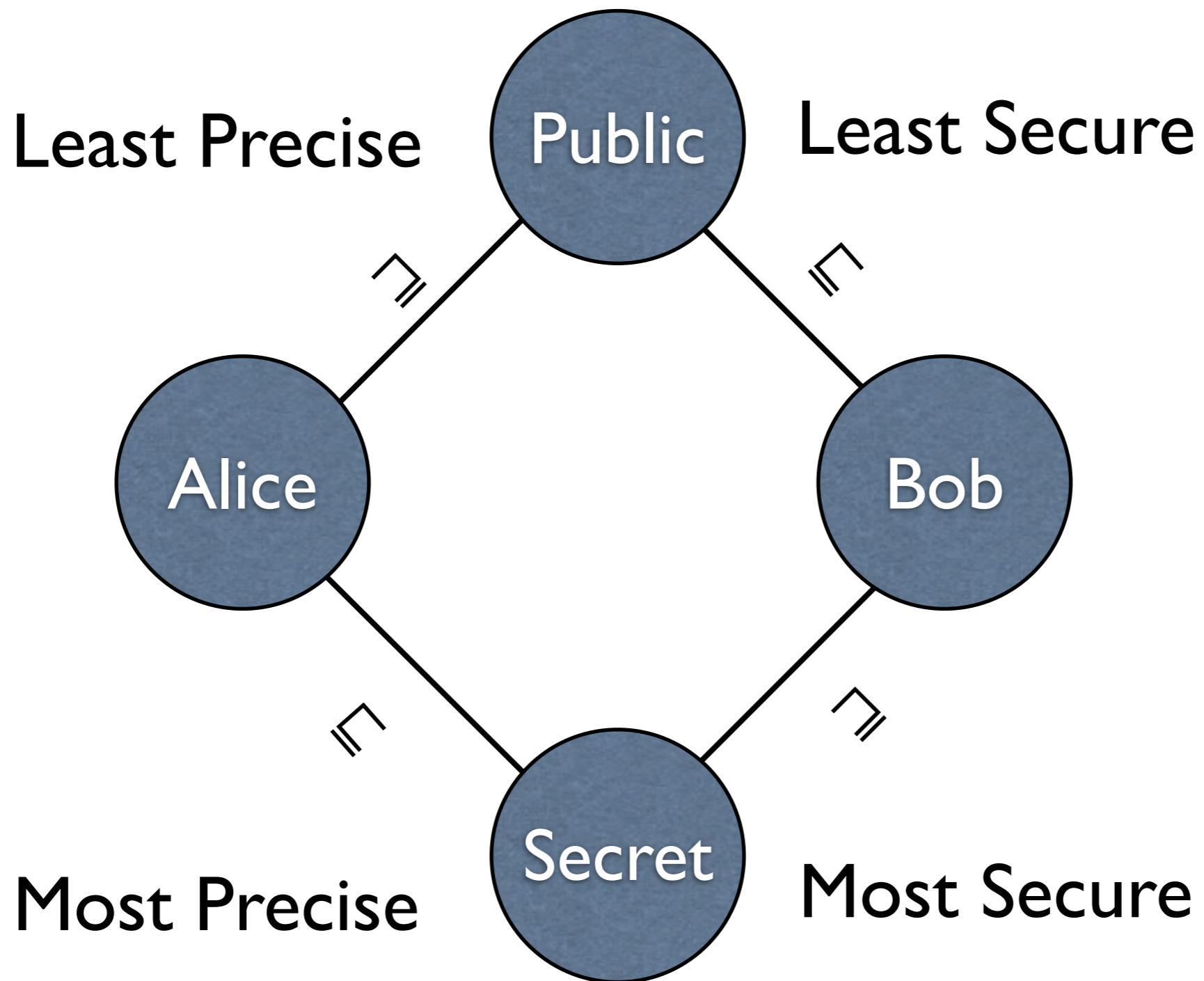
# Overview

- Example online going over `fail03.not` (from the test suite) in depth
- A type system for secure information flow
- Implementing said type system

# Flashback: Assignment 2

- Implemented dynamically enforced secure information flow via label tracking
- Each `Storable` is labeled with a tag describing its security level
- Security levels interact in well-defined ways

# Security Levels



# Basic Idea

- Specify which channel we output to (public, secure, etc.)
- Only output values of equal or lesser security than the specified value (i.e. do not output something secure on a public channel)
- When values interact to produce new values, the new values take the security level of the most secure thing they touched

# Example

```
var x, y in
```

```
output secret "enter secret number: ";
```

```
x := input secret num;
```

```
y := x;
```

```
output public y
```

# Issues

- This system works, but there are two major issues with it (well, 1.5 major issues)
- What's problematic?

# #1: Termination Leaks

- Whether or not a program halts can leak a bit to an attacker
- In a dynamic system, certain kinds of leaks are transformed into termination leaks
  - I.e. instead of outputting a secret value to public, throw an exception and terminate instead



# #2: Dynamic

```
var x, y in
  x := input secret num;
  y := input public num;
  if (y = 42) {
    output public x
  }
```

# A Solution

- A static type system and type checker, specifically for secure information flow
- If a program typechecks, then it is **guaranteed** that it is secure
- Type systems being type systems, if it does not typecheck, it still *might* be secure

# Assignment 5

- Implement a type checker for secure information flow for miniJS
  - Same syntax from assignment 2
  - Implicitly typed
- The type system, along with all the necessary rules, is provided
- Overall very similar to the type system coverage in the lecture

# Major Difference from Lecture

- Lecture is using equivalence constraints
  - Solved using the union-find data structure
- This assignment will use subset constraints
  - These slides cover how to solve these

# Three Core Challenges

1. Understanding the math
2. Implementing the math
3. Solving the constraints

# #1 Understanding The Math

- Basics needed to understand it covered extensively in lecture
- Biggest difference from lecture:  $L$  is used as a type variable instead of  $T$ , since  $L$  is a security level

# #2 Implementing Math

- General rule: implement as close to the math as possible
- The more it deviates, the more difficult it is to reason about whether or not they are equivalent
- ...and the more difficult it becomes to track down bugs

# Implementing Math

$$\frac{\ell_w \sqsubseteq L \quad \ell \sqsubseteq L}{\rho \cdot \ell_w \vdash \mathbf{input} \ell \text{ typ} : L}$$

```
case In(typ, l) => {  
  val L = LevelVariable()  
  lw ∈ L  
  l ∈ L  
  L  
}
```



# #3: Solving the Constraints

# Constraint Generation

- Very similar to how constraints were generated in lecture
- Based on subsets instead of equality

$$\frac{\ell_w \sqsubseteq L \quad \ell \sqsubseteq L}{\rho \cdot \ell_w \vdash \mathbf{input} \ell \text{ typ} : L}$$

# Constraint Generation

Once all the rules have completed, we end up with a bunch of constraints like these:

`Public ⊆ L1`

`Public ⊆ L2`

`Public ⊆ Secret`

`Public ⊆ L3`

`L3 ⊆ L1`

`L2 ⊆ L4`

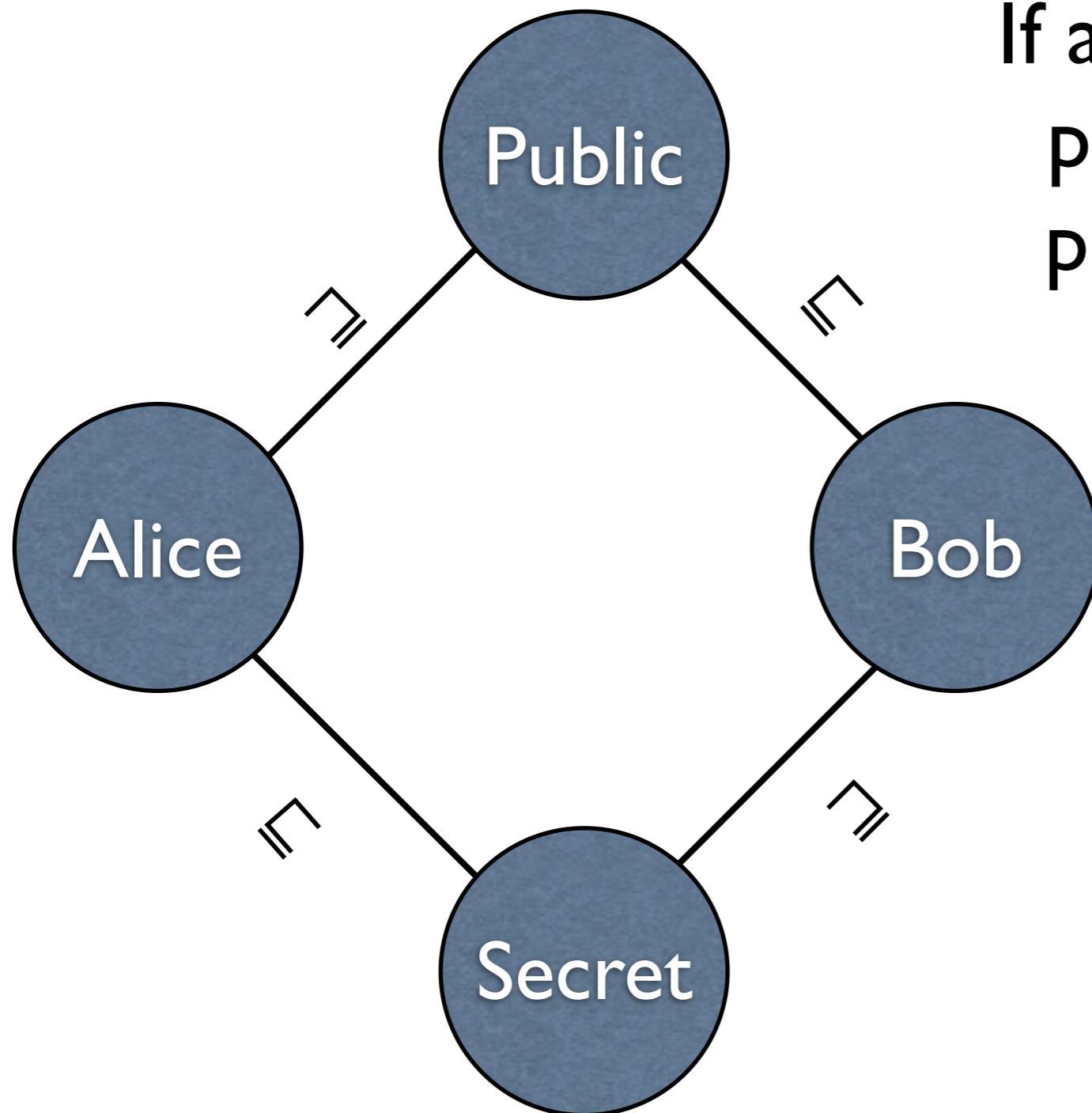
`Secret ⊆ L4`

**...where `L1`, `L2`, and `L3`  
are type variables**

# Constraint Meaning

- These constraints show what the syntax of the program says about the security lattice
- We already know what the security lattice looks like
- If the two are consistent, the program typechecks
- If there are inconsistencies, the program fails to typecheck

# Finding Inconsistencies



If any constraints violate this partial order, it means the program is not well-typed

Secret ~~⊑~~ Public  
Secret ~~⊑~~ Bob  
Secret ~~⊑~~ Alice  
Bob ~~⊑~~ Public  
Alice ~~⊑~~ Public  
Bob ~~⊑~~ Alice  
Alice ~~⊑~~ Bob

# Not that Easy

- What about type variables?
- Need a way to map these back to concrete types

Public  $\sqsubseteq$  L1

Public  $\sqsubseteq$  L2

Public  $\sqsubseteq$  Secret

Public  $\sqsubseteq$  L3

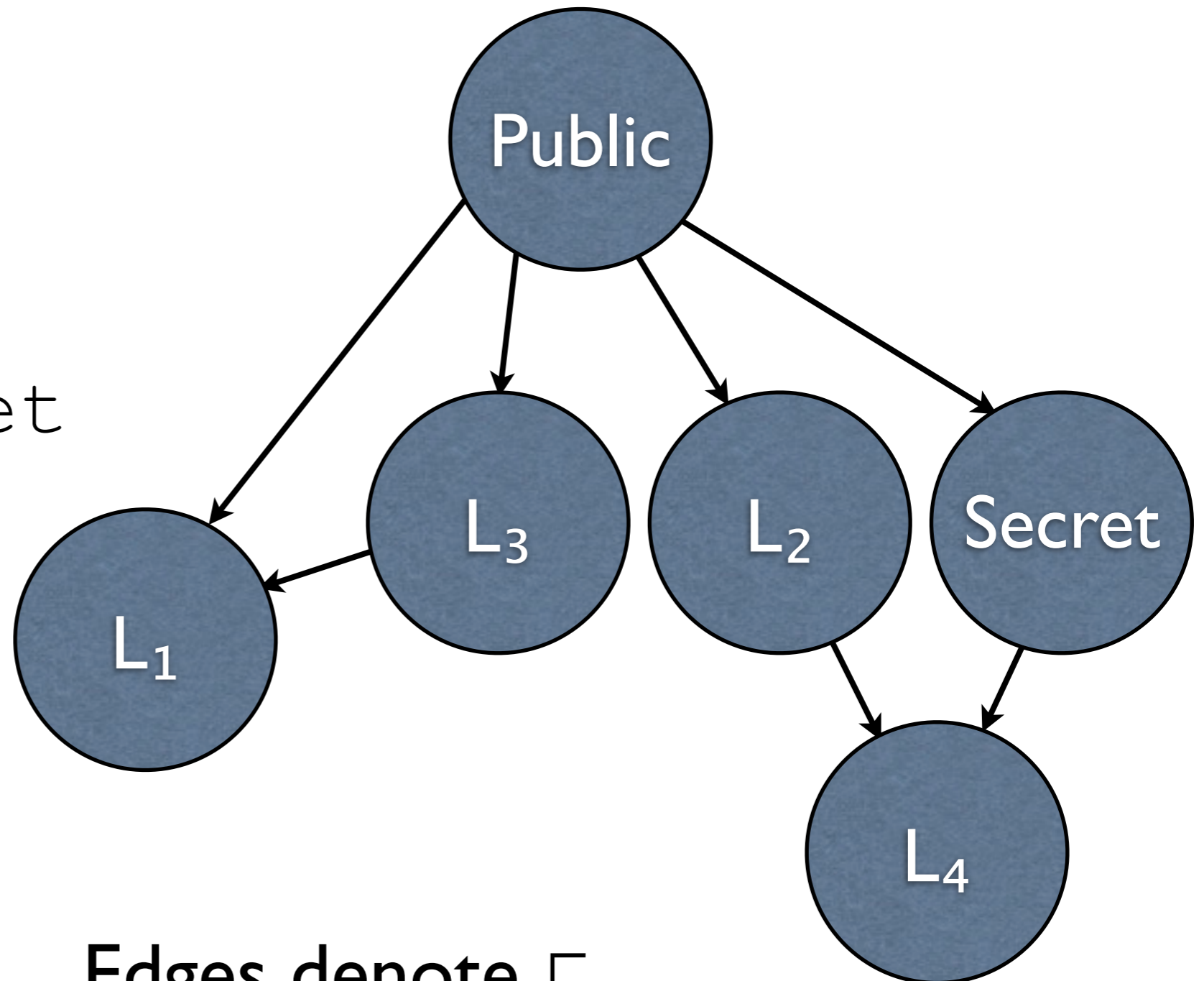
L3  $\sqsubseteq$  L1

L2  $\sqsubseteq$  L4

Secret  $\sqsubseteq$  L4

# Coalescing Constraints

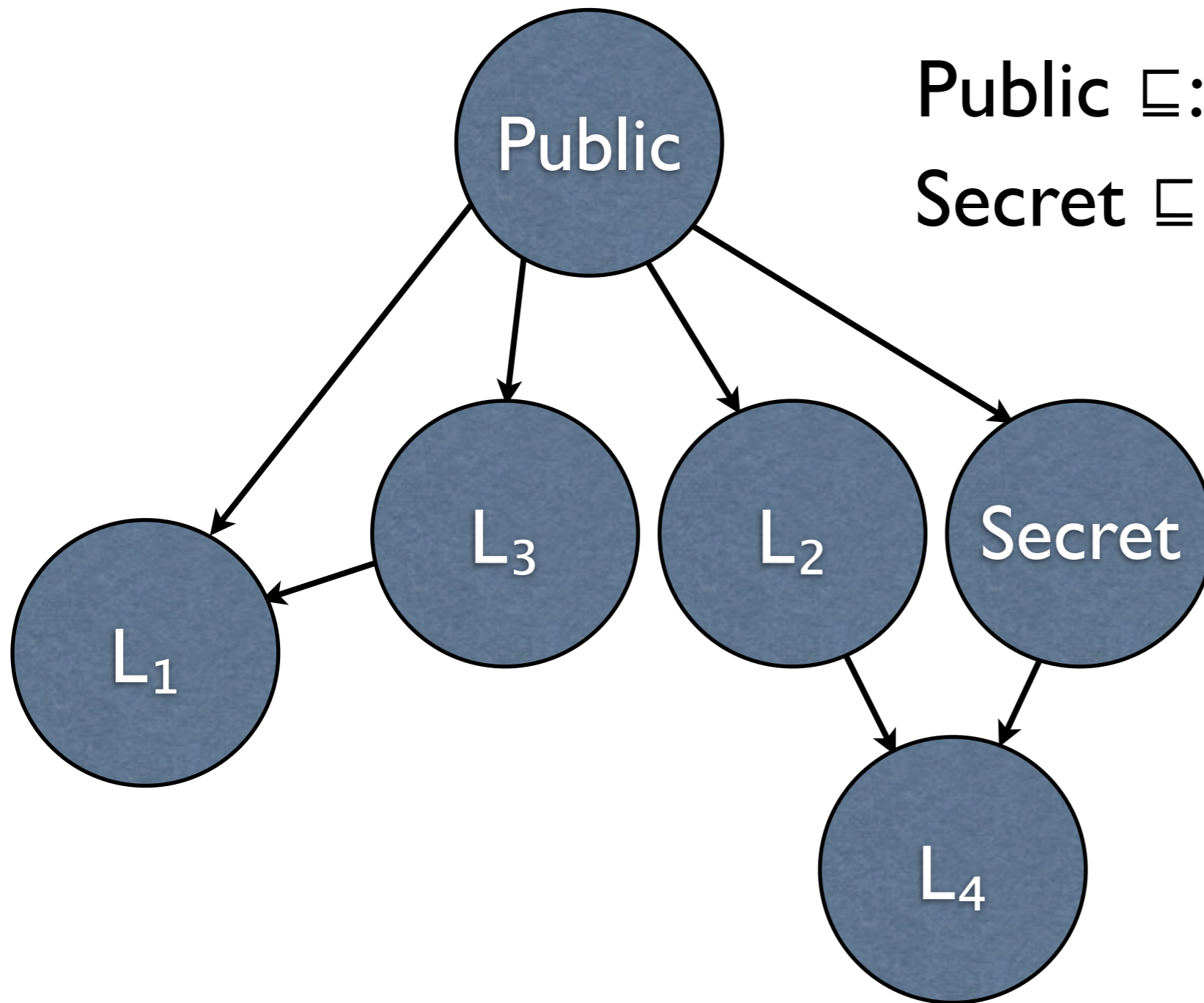
Public  $\sqsubseteq$  L1  
Public  $\sqsubseteq$  L2  
Public  $\sqsubseteq$  Secret  
Public  $\sqsubseteq$  L3  
L3  $\sqsubseteq$  L1  
L2  $\sqsubseteq$  L4  
Secret  $\sqsubseteq$  L4



Edges denote  $\sqsubseteq$

# Getting the Full $\sqsubseteq$

If node  $n_1$  can reach node  $n_2$ , then  $n_1 \sqsubseteq n_2$

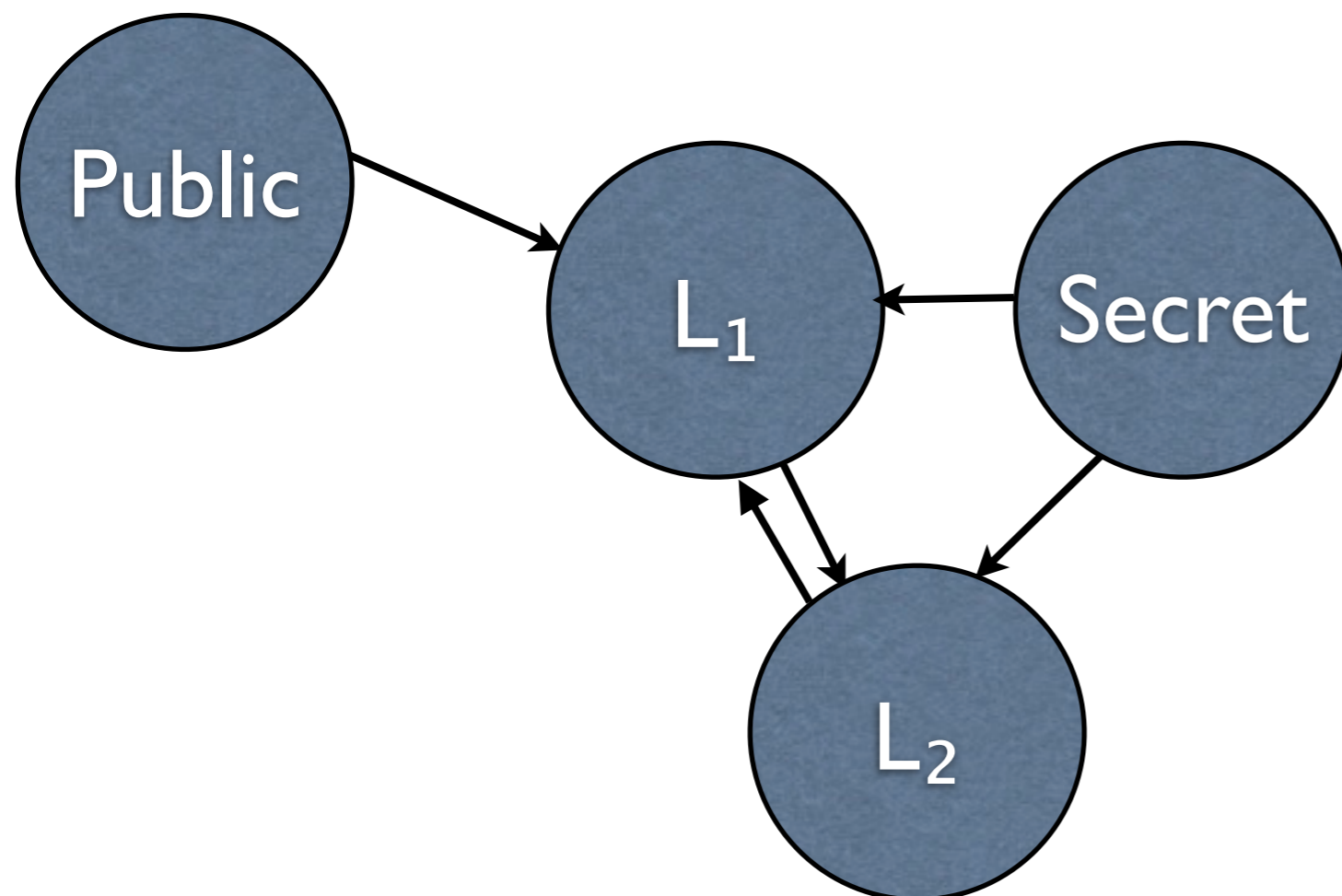


Public  $\sqsubseteq$ :  $\{L_1, L_2, L_3, L_4, \text{Secret}\}$   
Secret  $\sqsubseteq$ :  $\{L_4\}$



# Cycles

- The graph can contain cycles
- This should not break anything



Public  $\sqsubseteq$ :  $\{L_1, L_2\}$

Secret  $\sqsubseteq$ :  $\{L_1, L_2\}$

# Final Step

- Verify the full sets are consistent
- Only need to consider concrete security levels (public, secure, etc.)

Secret ~~⊇~~ Public

**Secret cannot reach Public**

Secret ~~⊇~~ Bob

**Secret cannot reach Bob**

Secret ~~⊇~~ Alice

**Secret cannot reach Alice**

Bob ~~⊇~~ Public

**Bob cannot reach Public**

Alice ~~⊇~~ Public

**Alice cannot reach Public**

Bob ~~⊇~~ Alice

**Bob cannot reach Alice**

Alice ~~⊇~~ Bob

**Alice cannot reach Bob**

# Constraint Solver Implementation

- Free to use mutability
- It is not necessary to make an explicit graph, but you are free to do so if you wish
  - It is likely easier to avoid it if possible
- For each constraint, add an edge and possibly nodes to this graph
- A global counter will be needed for generating unique type variables

# Removed for Simplicity

- Each node should have an edge pointing to itself
- Since the definition of  $\sqsubseteq$  includes equality, for all levels  $l$ ,  $l \sqsubseteq l$
- Hint: this can be exploited in implementations that do not have an explicit graph

# The Math in Depth

fail03.not **Example**